Algorithm – Causal-Order Broadcast

Algorithm 1 No-Waiting Causal Broadcast

Implements:

CausalOrderReliableBroadcast, $instance \ crb$.

Uses:

ReliableBroadcast, **instance** rb.

```
1: upon event \langle Init \rangle do
 2:
        delivered := \emptyset
        past := []
 3:
 4: upon event \langle crb, Broadcast \mid m \rangle do
        trigger \langle rb, Broadcast \mid [DATA, past, m] \rangle
        past := (self, m) :: past
                                         ▶ List cons instead of append for brevity.
 6:
 7: upon event \langle rb, Deliver \mid p, [DATA, mpast, m] \rangle do
        if m \notin delivered then
             DELIVER DEPS (mpast)
9:
             trigger \langle crb, Deliver \mid p, m \rangle
10:
             delivered := delivered \cup \{m\}
11:
            if (p,m) \notin past then
12:
                 past := (p, m) :: past
13:
14: function DELIVER DEPS ((p, m) :: rest)
        if m \notin delivered then
15:
             DELIVER DEPS (rest)
16:
             trigger \langle crb, Deliver \mid p, m \rangle
17:
             delivered := delivered \cup \{m\}
18:
            if (p,m) \notin past then
19:
                 past := (p, m) :: past
20:
```

Algorithm 2 Broadcast with Sequence Number

Implements:

FIFOReliable Broadcast, **instance** frb.

Uses:

ReliableBroadcast, **instance** rb.

```
1: upon event \langle Init \rangle do
         lsn := 0
 2:
         pending := \emptyset
 3:
         \forall_{p\in\Pi}\ next[p]:=1
 5: upon event \langle frb, Broadcast \mid m \rangle do
         lsn := lsn + 1
 6:
         trigger \langle rb, Broadcast \mid [DATA, self, m, lsn] \rangle
 7:
 8: upon event \langle rb, Deliver \mid p, [DATA, s, m, sn] \rangle do
         pending := pending \cup \{(s, m, sn)\}
 9:
         while \exists_{(s,m',sn')\in pending} \ sn' = next[s] \ do
10:
              next[s] := next[s] + 1
11:
              pending := pending \setminus \{(s, m', sn')\}
12:
             trigger \langle frb, Deliver \mid s, m' \rangle
13:
```

Algorithm 3 No-Waiting Causal Broadcast with FIFO

Implements:

CausalOrderReliableBroadcast, $instance \ crb$.

Uses:

FIFO-ReliableBroadcast, **instance** frb.

```
1: upon event \langle Init \rangle do
         delivered := \emptyset
        l := []
 3:
 4: upon event \langle crb, Broadcast \mid m \rangle do
        trigger \langle frb, Broadcast \mid [DATA, (self, m) :: l] \rangle
        l := []
 6:
 7: upon event \langle frb, Deliver \mid p, [DATA, l_m] \rangle do
        DELIVER DEPS (l_m)
 9: function DELIVER DEPS ((p, m) :: rest)
        if m \notin delivered then
10:
             DELIVER DEPS (rest)
11:
12:
             trigger \langle crb, Deliver \mid p, m \rangle
             delivered := delivered \cup \{m\}
13:
14:
             if (p,m) \notin l then
15:
                 l := (p, m) :: l
```

Algorithm 4 Waiting Causal Broadcast

Implements:

CausalOrderReliableBroadcast, **instance** crb.

Uses:

ReliableBroadcast, **instance** rb.

```
1: upon event \langle Init \rangle do
         \forall_{p \in \Pi} \ V[p] := 0
         lsn := 0
 3:
         pending := \emptyset
 4:
 5: upon event \langle crb, Broadcast \mid m \rangle do
         W := V
         W[self] := lsn
 7:
         lsn := lsn + 1
 8:
         trigger \langle rb, Broadcast \mid [DATA, W, m] \rangle
10: upon event \langle rb, Deliver \mid p, [DATA, W, m] \rangle do
         pending := pending \cup \{(p, W, m)\}
11:
         while \exists_{(p',W',m')\in pending} W' \leq V \mathbf{do}
12:
              pending := pending \setminus \{(p', W', m')\}
13:
             V[p'] := V[p'] + 1
14:
             trigger \langle crb, Deliver \mid p', m' \rangle
15:
```