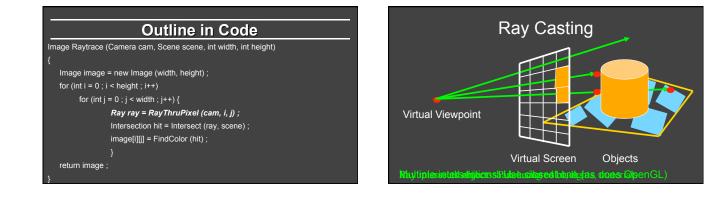
Foundations of Computer Graphics

Online Lecture 10: Ray Tracing 2 – Nuts and Bolts Camera Ray Casting

Ravi Ramamoorthi

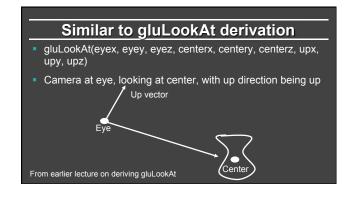
Outline

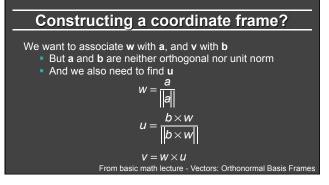
- Camera Ray Casting (choose ray directions)
- Ray-object intersections
- Ray-tracing transformed objects
- Lighting calculations
- Recursive ray tracing

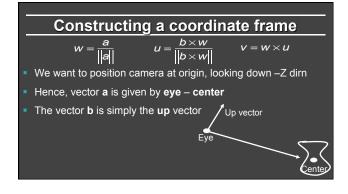


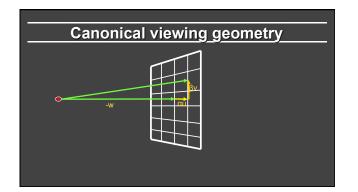
Finding Ray Direction

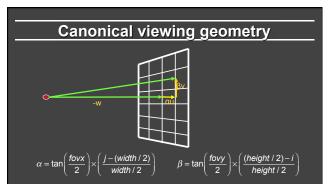
- Goal is to find ray direction for given pixel i and j
- Many ways to approach problem
 - Objects in world coord, find dirn of each ray (we do this)
 - Camera in canonical frame, transform objects (OpenGL)
- Basic idea
 - Ray has origin (camera center) and direction
 - Find direction given camera params and i and j
- Camera params as in gluLookAt
 Lookfrom[3], LookAt[3], up[3], fov

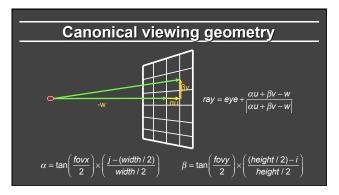


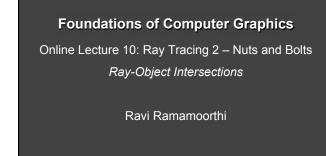








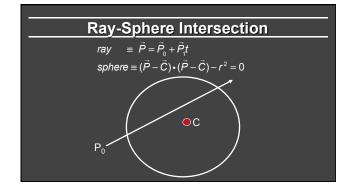




Outline

- Camera Ray Casting (choosing ray directions)
- Ray-object intersections
- Ray-tracing transformed objects
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Outline in Code
Image Raytrace (Camera cam, Scene scene, int width, int height)
{
Image image = new Image (width, height) ;
for (int i = 0 ; i < height ; i++)
for (int j = 0 ; j < width ; j++) {
Ray ray = RayThruPixel (cam, i, j) ;
Intersection hit = Intersect (ray, scene) ;
image[i][j] = FindColor (hit) ;
}
return image ;
}



Ray-Sphere Intersection $ray \equiv \vec{P} = \vec{P}_0 + \vec{P}_1 t$ $sphere \equiv (\vec{P} - \vec{C}) \cdot (\vec{P} - \vec{C}) - r^2 = 0$ Substitute

Ray-Sphere Intersection

 $\begin{aligned} ray &\equiv \vec{P} = \vec{P}_0 + \vec{P}_1 t\\ sphere &\equiv (\vec{P} - \vec{C}) \bullet (\vec{P} - \vec{C}) - r^2 = 0\\ \text{Substitute}\\ ray &\equiv \vec{P} = \vec{P}_0 + \vec{P}_1 t\\ sphere &\equiv (\vec{P}_0 + \vec{P}_1 t - \vec{C}) \bullet (\vec{P}_0 + \vec{P}_1 t - \vec{C}) - r^2 = 0\\ \text{Simplify} \end{aligned}$

$$\begin{array}{rl} \textbf{Ray-Sphere Intersection} \\ ray &\equiv \vec{P} = \vec{P}_0 + \vec{P}_1 t \\ sphere \equiv (\vec{P} - \vec{C}) \boldsymbol{\cdot} (\vec{P} - \vec{C}) - r^2 = 0 \\ \\ \text{Substitute} \\ ray &\equiv \vec{P} = \vec{P}_0 + \vec{P}_1 t \\ sphere \equiv (\vec{P}_0 + \vec{P}_1 t - \vec{C}) \boldsymbol{\cdot} (\vec{P}_0 + \vec{P}_1 t - \vec{C}) - r^2 = 0 \\ \\ \text{Simplify} \\ t^2 (\vec{P}_1 \boldsymbol{\cdot} \vec{P}_1) + 2t \, \vec{P}_1 \boldsymbol{\cdot} (\vec{P}_0 - \vec{C}) + (\vec{P}_0 - \vec{C}) \boldsymbol{\cdot} (\vec{P}_0 - \vec{C}) - r^2 = 0 \end{array}$$

Ray-Sphere Intersection

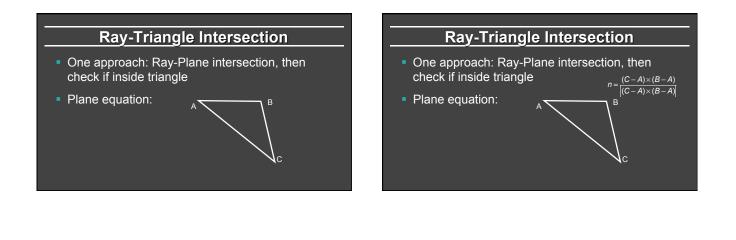
 $t^{2}(\vec{P}_{1} \cdot \vec{P}_{1}) + 2t \vec{P}_{1} \cdot (\vec{P}_{0} - \vec{C}) + (\vec{P}_{0} - \vec{C}) \cdot (\vec{P}_{0} - \vec{C}) - r^{2} = 0$

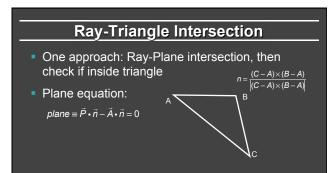
- Solve quadratic equations for t
- 2 real positive roots: pick smaller root
- Both roots same: tangent to sphere
- One positive, one negative root: ray origin inside sphere (pick + root)
- Complex roots: no intersection (checkdiscriminant of equation first)

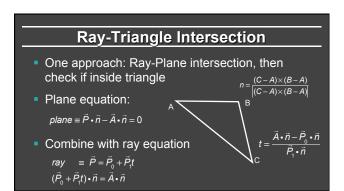
Ray-Sphere Intersection

- Intersection point: ray $\equiv \vec{P} = \vec{P}_0 + \vec{P}_1 t$
- Normal (for sphere, this is same as coordinates in sphere frame of reference, useful other tasks)

normal =
$$\frac{\vec{P} - \vec{C}}{\vec{P} - \vec{C}}$$





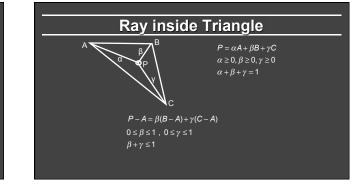


Ray inside Triangle

- Once intersect with plane, need to find if in triangle
- Many possibilities for triangles, general polygons
- We find parametrically [barycentric coordinates]. Also useful for other applications (texture mapping)

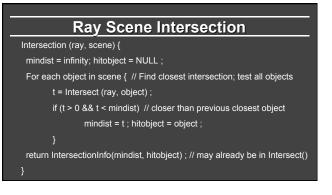
 $P = \alpha A + \beta B + \gamma C$





Other primitives

- Much early work in ray tracing focused on ray-primitive intersection tests
- Cones, cylinders, ellipsoids
- Boxes (especially useful for bounding boxes)
- General planar polygons
- Many more



Outline

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Ray-Tracing Transformed Objects

We have an optimized ray-sphere test • But we want to ray trace an ellipsoid...

Solution: Ellipsoid transforms sphere

- Apply inverse transform to ray, use ray-sphere
- Allows for instancing (traffic jam of cars)
- Same idea for other primitives

Transformed Objects

Consider a general 4x4 transform M (matrix stacks)

Apply inverse transform M⁻¹ to ray

- Locations stored and transform in homogeneous coordinates
- Vectors (ray directions) have homogeneous coordinate set to 0 [so there is no action because of translations]

Do standard ray-surface intersection as modified

Transform intersection back to actual coordinates Intersection point p transforms as Mp

Normals n transform as M^{-t}n. Do all this before lighting

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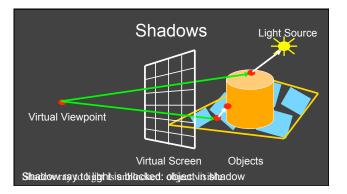
Online Lecture 10: Ray Tracing 2 – Nuts and Bolts Lighting Calculations

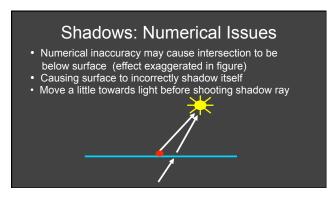
Ravi Ramamoorthi

Outline

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Dutline in Code Image Raytrace (Camera cam, Scene scene, int width, int height) { Image image = new Image (width, height); for (int i = 0; i < height; i++) for (int j = 0; j < width; j++) { Ray ray = RayThruPixel (cam, i, j); Intersection hit = Intersect (ray, scene); image[i][j] = FindColor (hit); } return image; }</pre>





Lighting Model

Similar to OpenGL

- Lighting model parameters (global)
- Ambient r g b
- Attenuation const linear quadratic $L = \frac{1}{const + lin * d + quad * d^2}$

Per light model parameters

- Directional light (direction, RGB parameters)
- Point light (location, RGB parameters)
- Some differences from HW 2 syntax

Material Model

- Diffuse reflectance (r g b)
- Specular reflectance (r g b)
- Shininess s
- Emission (r g b)
- All as in OpenGL

Shading Model

$$I = K_a + K_e + \sum_{i=1}^{n} V_i L_i (K_d \max (I_i \bullet n, 0) + K_s (\max(h_i \bullet n, 0))^s)$$

- Global ambient term, emission from material
- For each light, diffuse specular terms
- Note visibility/shadowing for each light (not in OpenGL)
- Evaluated per pixel per light (not per vertex)

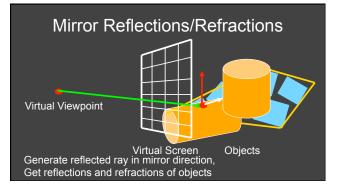
Foundations of Computer Graphics

Online Lecture 10: Ray Tracing 2 – Nuts and Bolts Recursive Ray Tracing

Ravi Ramamoorthi

Outline

- Camera Ray Casting (choosing ray directions)
- Ray-object intersections
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- Recursive ray tracing



Basic idea

For each pixel

- Trace Primary Eye Ray, find intersection
- Trace Secondary Shadow Ray(s) to all light(s)
 Color = Visible ? Illumination Model : 0 ;
- Trace Reflected Ray
 Color += reflectivity * Color of reflected ray

Recursive Shading Model

 $I = K_{a} + K_{e} + \sum_{i} V_{i} L_{i} (K_{d} \max(I_{i} \cdot n, 0) + K_{s} (\max(h_{i} \cdot n, 0))^{s}) + K_{s} I_{R} + K_{T} I_{T}$

- Highlighted terms are recursive specularities [mirror reflections] and transmission (latter is extra)
- Trace secondary rays for mirror reflections and refractions, include contribution in lighting model
- GetColor calls RayTrace recursively (the I values in equation above of secondary rays are obtained by recursive calls)

Problems with Recursion

- Reflection rays may be traced forever
- Generally, set maximum recursion depth
- Same for transmitted rays (take refraction into account)

Some basic add ons

- Area light sources and soft shadows: break into grid of n x n point lights
 - Use jittering: Randomize direction of shadow ray within small box for given light source direction
 Jittering also useful for antialiasing shadows when
 - Jittering also useful for antialiasing shadows when shooting primary rays
- More complex reflectance models
 Simply update shading model
 - But at present, we can handle only mirror global illumination calculations