# Algorithm - Consensus in the Fail-Stop Model 

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Algorithm 1 Hierarchical Consensus
Implements:
    Consensus, instance \(c\).
Uses:
    BestEffortBroadcast, instance beb.
    PerfectFailureDetector, instance \(P\).
upon event \(\langle\) Init \(\rangle\) do
    detectedranks \(:=\emptyset\)
    round \(:=1\)
    proposal \(:=\perp\)
    proposer \(:=0\)
    \(\forall_{p \in \Pi}\) delivered \([p]:=\) FALSE
    broadcast \(:=\) FALSE
upon event \(\langle P\), Crash \(\mid p\rangle\) do
    detectedranks \(:=\) detectedranks \(\cup\{\operatorname{RANK}(p)\}\)
upon event \(\langle c\), Propose \(\mid v\rangle\) do
    if proposal \(=\perp\) then
            proposal \(:=v\)
upon event \(\langle b e b\), Deliver \(\mid p,[\operatorname{DECIDED}, v]\rangle\) do
    \(r:=\operatorname{RANK}(p)\)
    if \(r<\operatorname{RANK}(\) self \() \wedge r>\) proposer then
        proposal \(:=v\)
        proposer \(:=r\)
    delivered \([p]:=\) TRUE
```

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upon event \(\langle\) round \(=\operatorname{RANK}(\) self \() \wedge\) proposal \(\neq \perp \wedge \neg\) broadcast \(\rangle\) do
        broadcast := TRUE
        trigger \(\langle\) beb, Broadcast \(|\) [DECIDED, proposal] \(\rangle\)
        trigger \(\langle c\), Decide \(|\) proposal \(\rangle\)
    upon event \(\left\langle\right.\) round \(\in\) detectedranks \(\vee\) delivered \(\left[\right.\) RANK \(^{-1}(\) round \(\left.\left.)\right]\right\rangle\) do
        round \(:=\) round +1
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Note: Where RANK ${ }^{-1}$ be the inverse function to Rank (which exists since RaNk is a bijection between $\Pi$ and $\{1, \ldots,|\Pi|\} \subseteq \mathbb{N}$ ).

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Algorithm 2 Hierarchical Uniform Consensus
Implements:
        UniformConsensus, instance \(u c\).
Uses:
    BestEffortBroadcast, instance beb.
    ReliableBroadcast, instance beb.
    PerfectPointToPointLinks, instance \(p p 2 p\).
    PerfectFailureDetector, instance \(P\).
upon event \(\langle\) Init \(\rangle\) do
    detectedranks := \(\emptyset\)
    ackranks := Ø
    round \(:=1\)
    proposal \(:=\perp\)
    decision \(:=\perp\)
    \(\forall_{p \in \Pi}\) proposed \([p]:=\perp\)
    upon event \(\langle P\), Crash \(\mid p\rangle\) do
    detectedranks \(:=\) detectedranks \(\cup\{\operatorname{RaNK}(p)\}\)
    upon event \(\langle u c\), Propose \(\mid v\rangle\) do
        if proposal \(=\perp\) then
            proposal \(:=v\)
```

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upon event \(\langle b e b\), Deliver \(| p,[\) Proposal, \(v]\rangle\) do
    proposed \([p]:=v\)
        if \(\operatorname{RANK}(p) \geq\) round then
            trigger \(\langle p p 2 p\), Send \(| \mathrm{p}\), Ack \(\rangle\)
    upon event \(\langle p p 2 p\), Deliver \(| p\), Ack \(\rangle\) do
        ackranks \(:=\) ackranks \(\cup\{\operatorname{RANK}(p)\}\)
    upon event \(\langle r b\), Deliver \(| p,[\) DECIDED, \(v]\rangle\) do
        if decision \(\neq \perp\) then
            decision \(:=v\)
            trigger \(\langle u c\), Decide \(|\) decision \(\rangle\)
    upon event \(\langle\) round \(=\operatorname{RANK}(\) self \() \wedge\) proposal \(\neq \perp \wedge\) decision \(=\perp\rangle\) do
        trigger \(\langle\) beb, Broadcast \(|\) [PROPOSAL, proposal \(]\rangle\)
    upon event \(\langle\) round \(\in\) detectedranks \(\rangle\) do
        if proposed \(\left[\right.\) RANK \(^{-1}(\) round \(\left.)\right] \neq \perp\) then
            proposal \(:=\) proposed \(\left[\mathrm{RANK}^{-1}(\right.\) round \(\left.)\right]\)
        round \(:=\) round +1
    upon event \(\langle\) detectedranks \(\cup\) ackranks \(=\{1, \ldots,|\Pi|\}\rangle\) do
        trigger \(\langle r b\), Broadcast \(|\) [DECIDED, proposal \(]\rangle\)
```

