

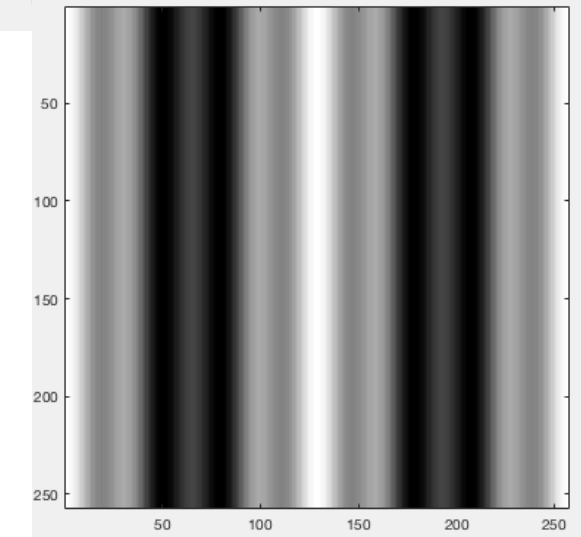
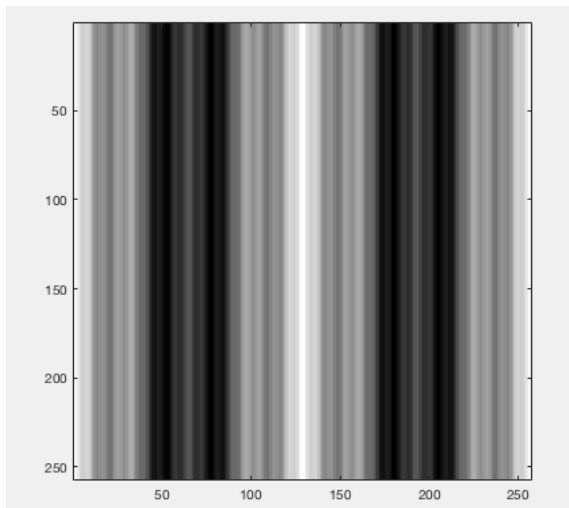
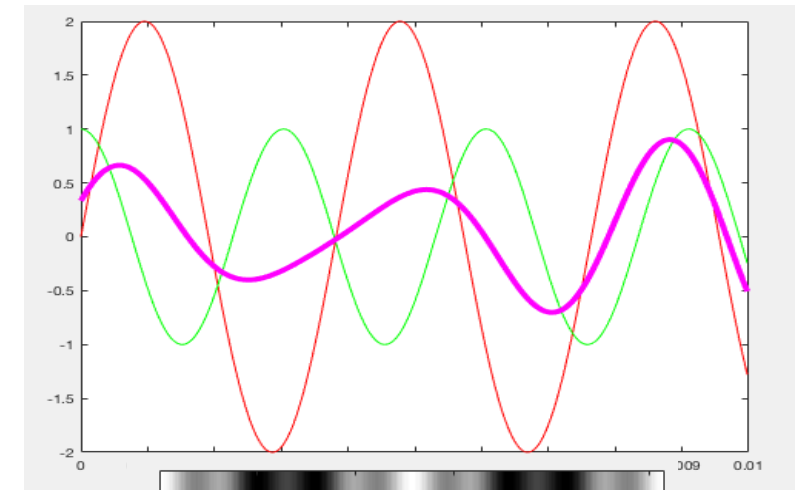
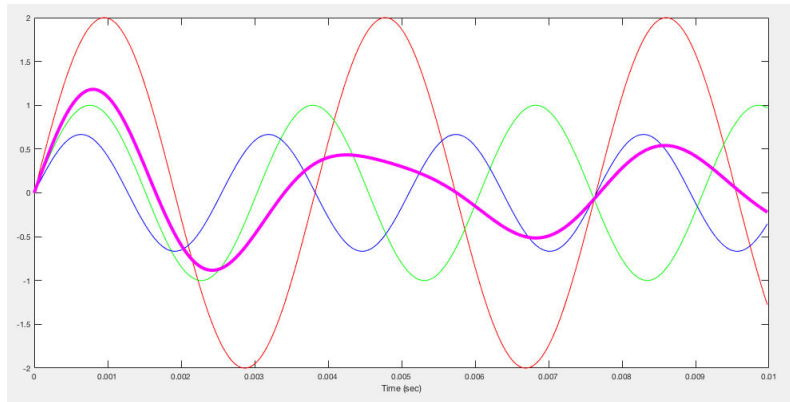


Video 4.1

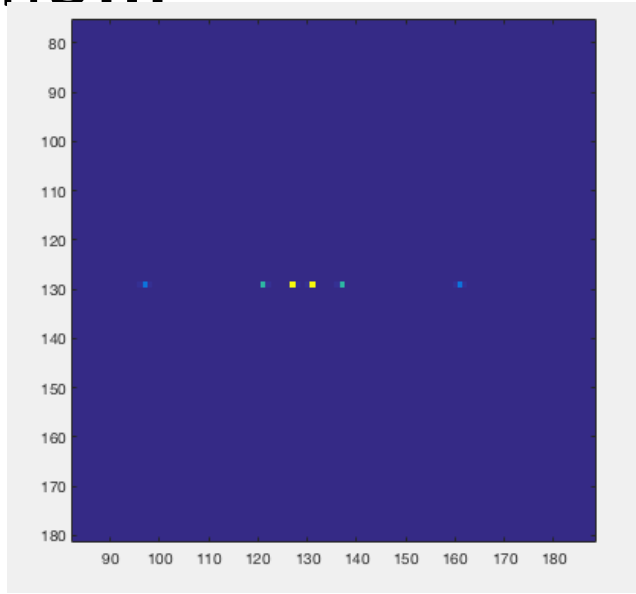
Kostas Daniilidis

Filter selectivity

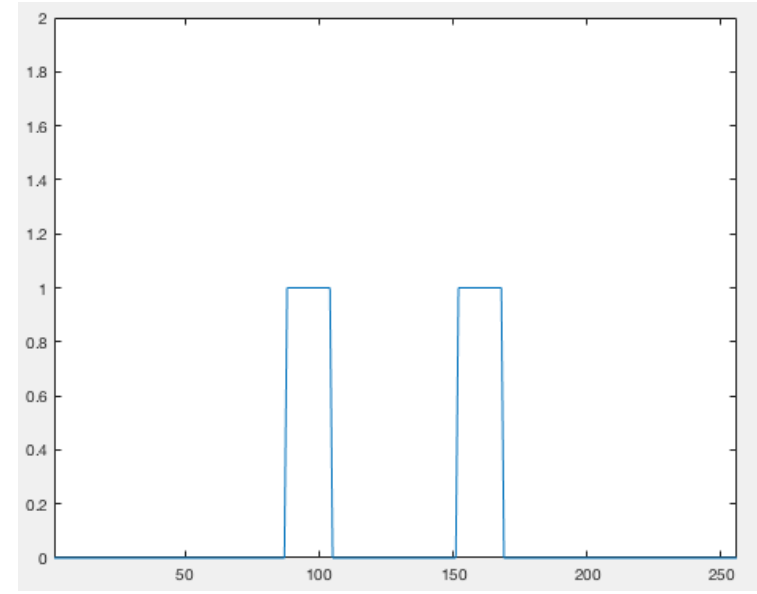
Frequency-selective filters



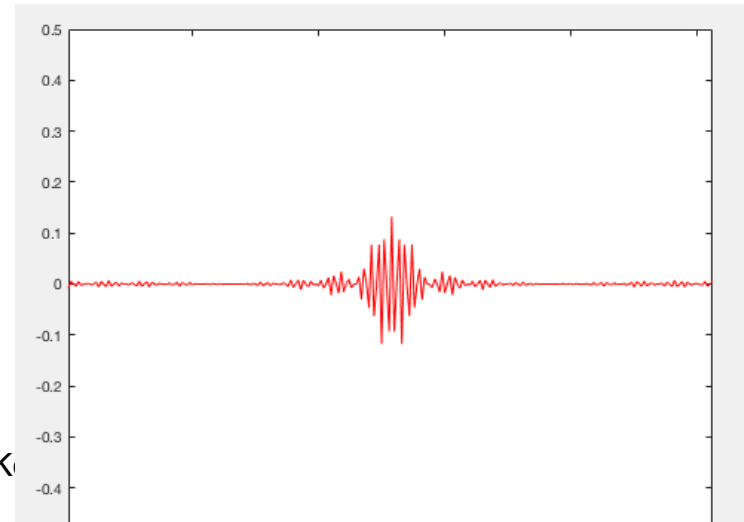
One might think of a **bandpass** filter in frequency like this...



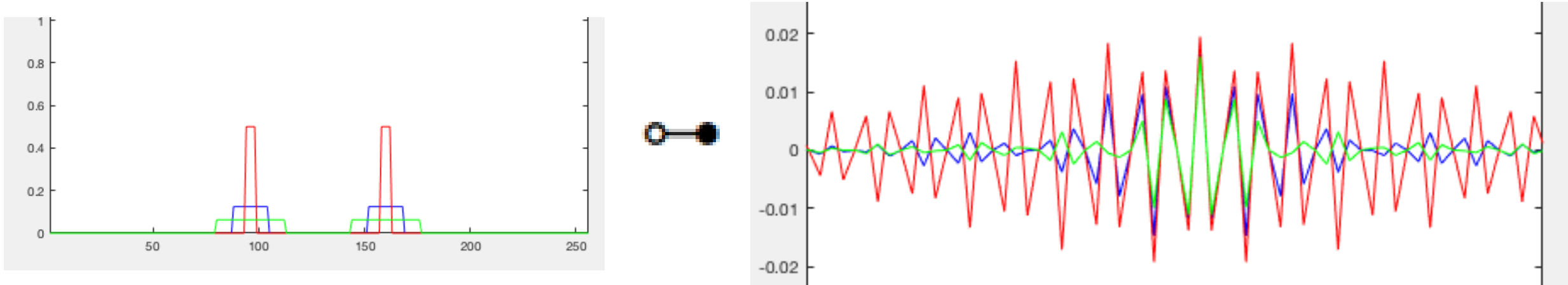
times



Would mean **convolving** with a huge mask:



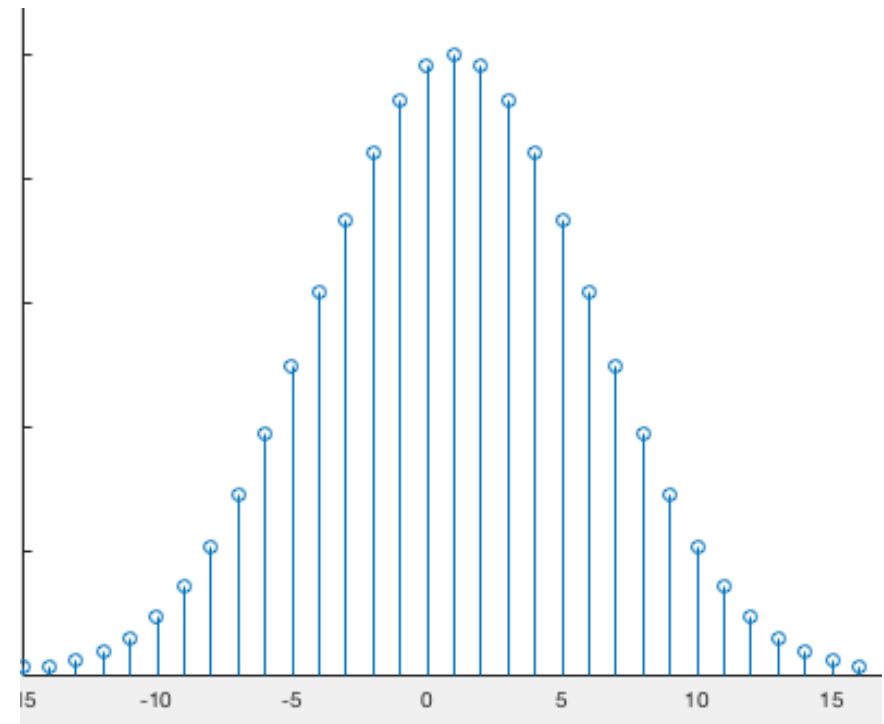
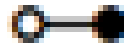
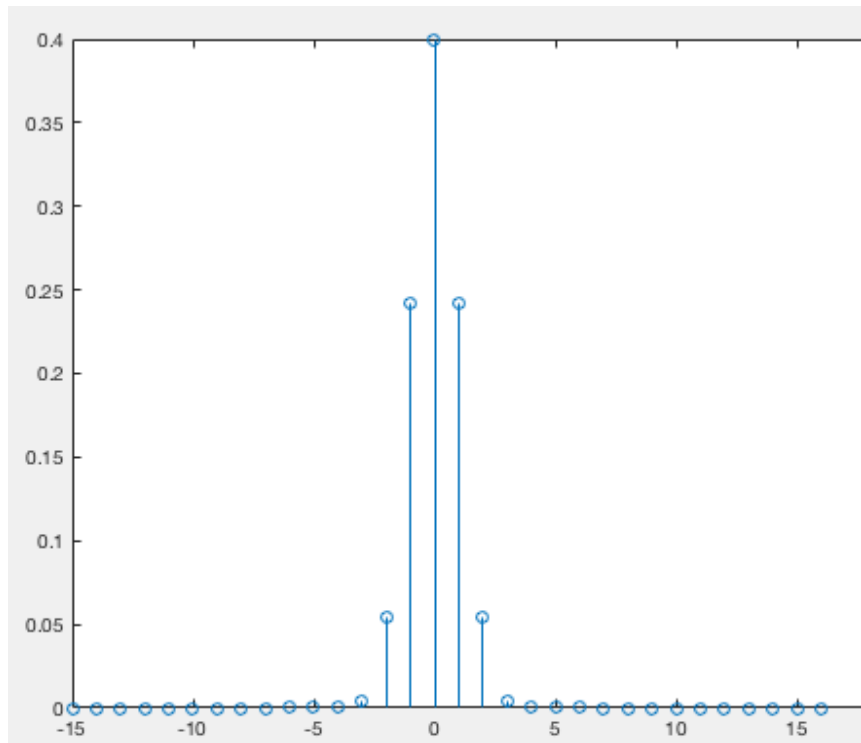
Frequency selectivity inversely proportional to spatial support (and hence location selectivity)



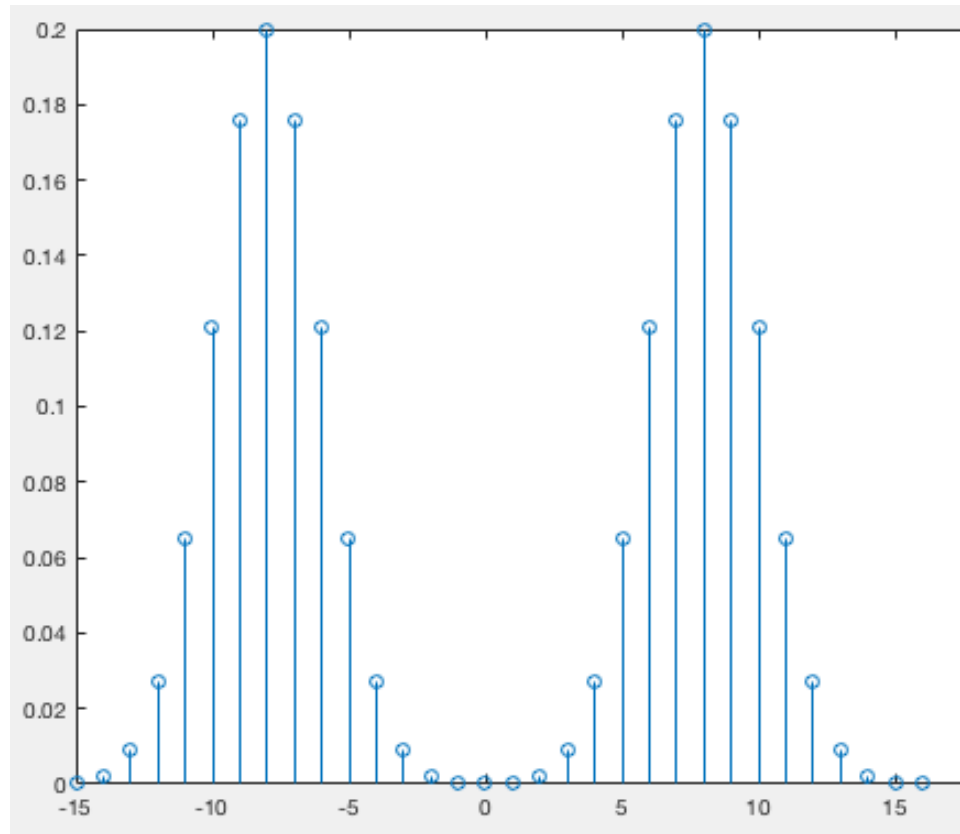
The uncertainty principle of signal processing

Best way to alleviate uncertainty principle....

Replace the rectangle with a Gaussian!!



How to make a bandpass out of a smoother (lowpass) ?



How to make a bandpass out of a smoothing filter (lowpass) ?

By creating two copies!

How?

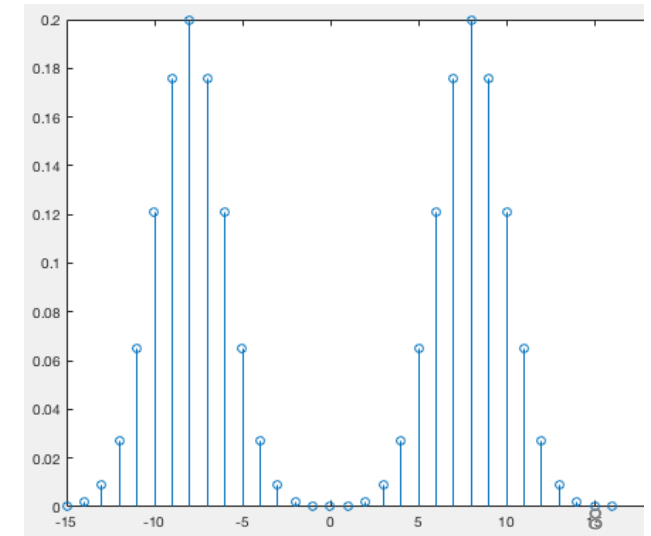
Modulating with a cosine!

Modulation with a cosine means

$$g(t) = \frac{1}{\sigma \sqrt{2\pi}} e^{-t^2/2\sigma^2} \circ \bullet G(\omega) = e^{-\sigma^2 \omega^2/2}$$

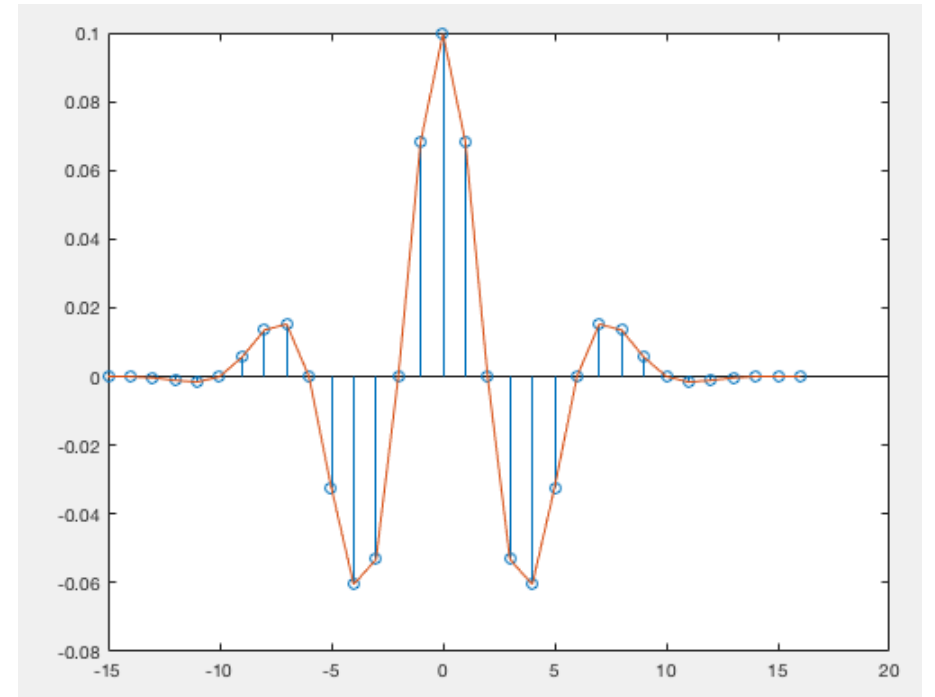
$$f(t) = \cos(\omega_0 t) \circ \bullet \frac{1}{2}(\delta(\omega - \omega_0) + \delta(\omega + \omega_0))$$

$$F(\omega)G(\omega) = e^{-\sigma^2 \omega_0^2/2} \left(\frac{1}{2}(\delta(\omega - \omega_0) + \delta(\omega + \omega_0)) \right)$$



Modulated Gaussian

$$\frac{1}{\sigma \sqrt{2\pi}} e^{-t^2/2\sigma^2} \cos \omega_0 t$$



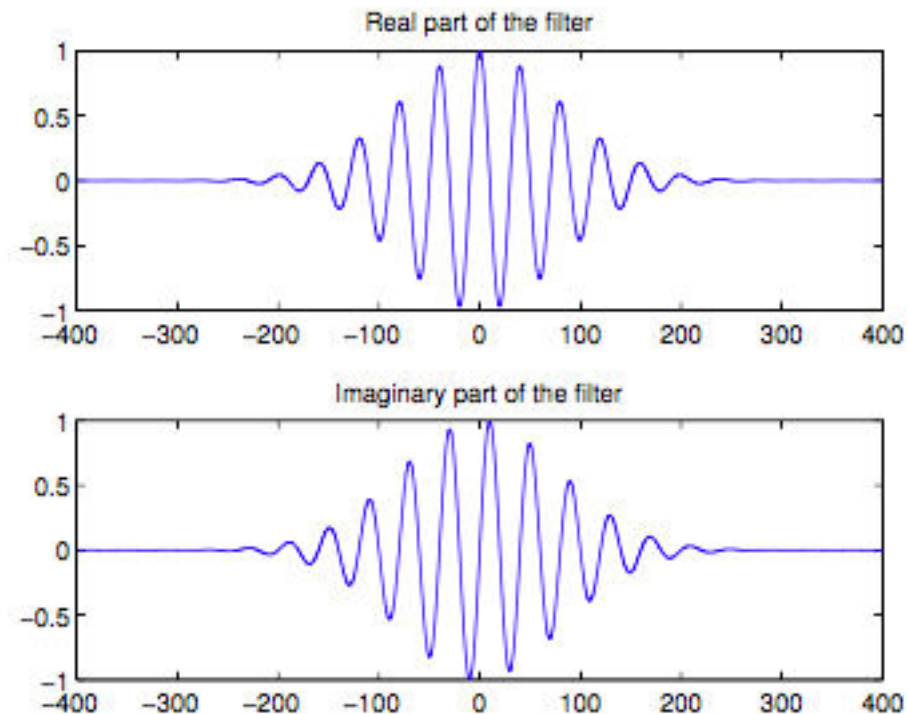
What happened with the phase?

$$\sin(\omega_0 t) \star \frac{1}{\sigma \sqrt{2\pi}} e^{-t^2/2\sigma^2} \cos \omega_0 t \quad =? \quad \sin(\omega_0 t)$$

We need a phase-independent result!

Quadrature: complex filter with $\text{Re}^2 + \text{Im}^2 = 1$

$$e^{-t^2/(2\sigma^2)} (\cos(\omega_0 t) + j \sin(\omega_0 t))$$



The Gabor Function

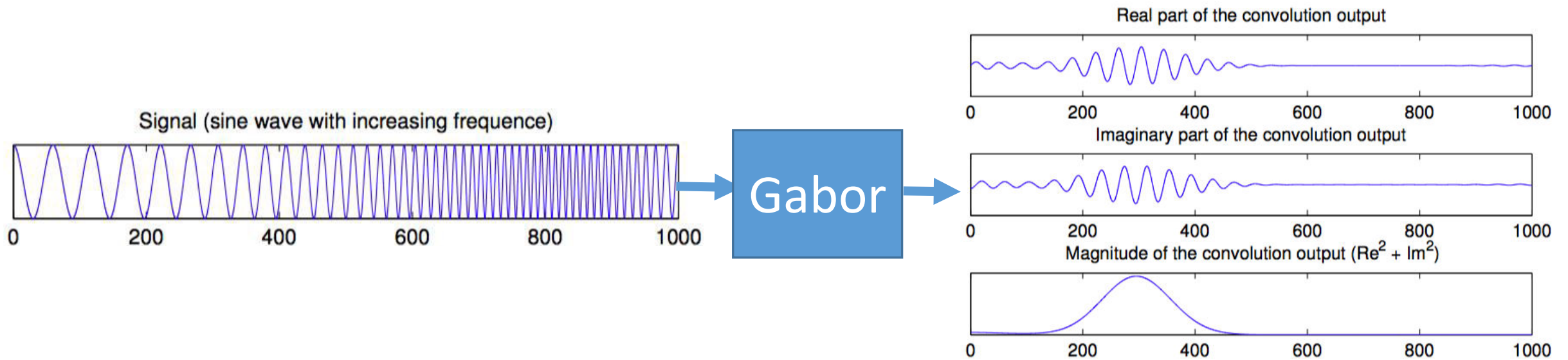
$$\frac{1}{\sigma \sqrt{2\pi}} e^{-t^2 / (2\sigma^2)} e^{j\omega_0 t}$$



$$e^{-\sigma^2 (\omega - \omega_0)^2 / 2}$$



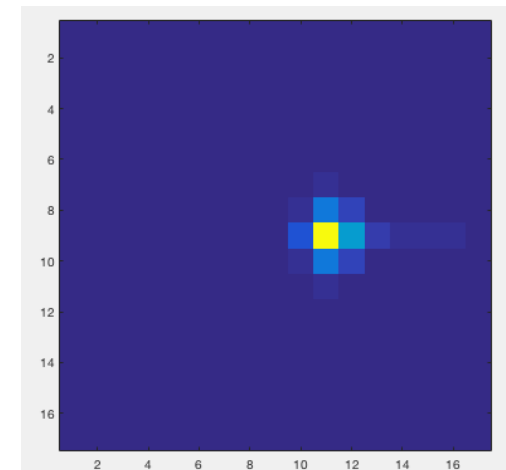
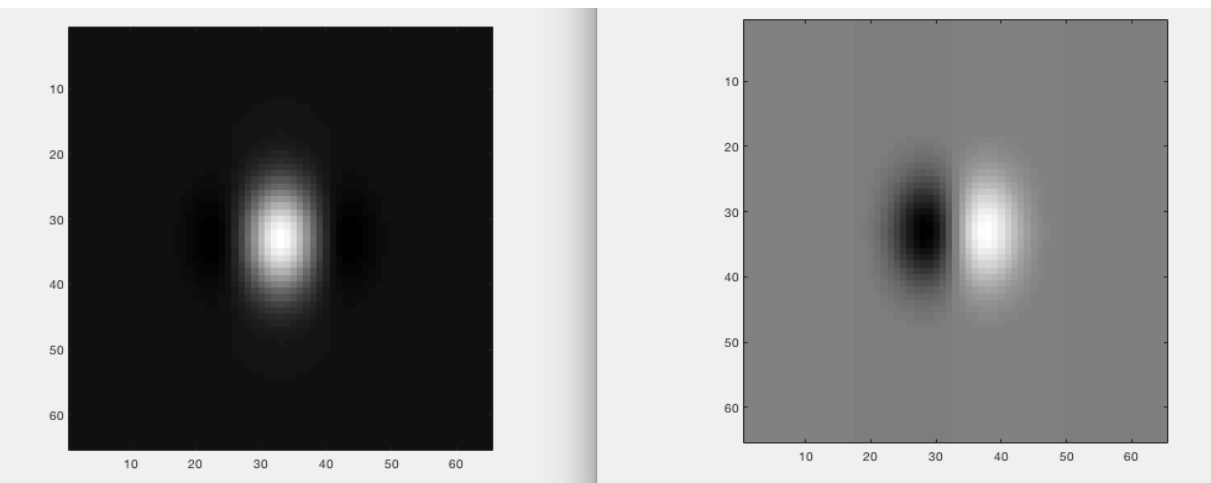
Frequency selectivity



2D Gabor Function: selectivity in frequency and orientation

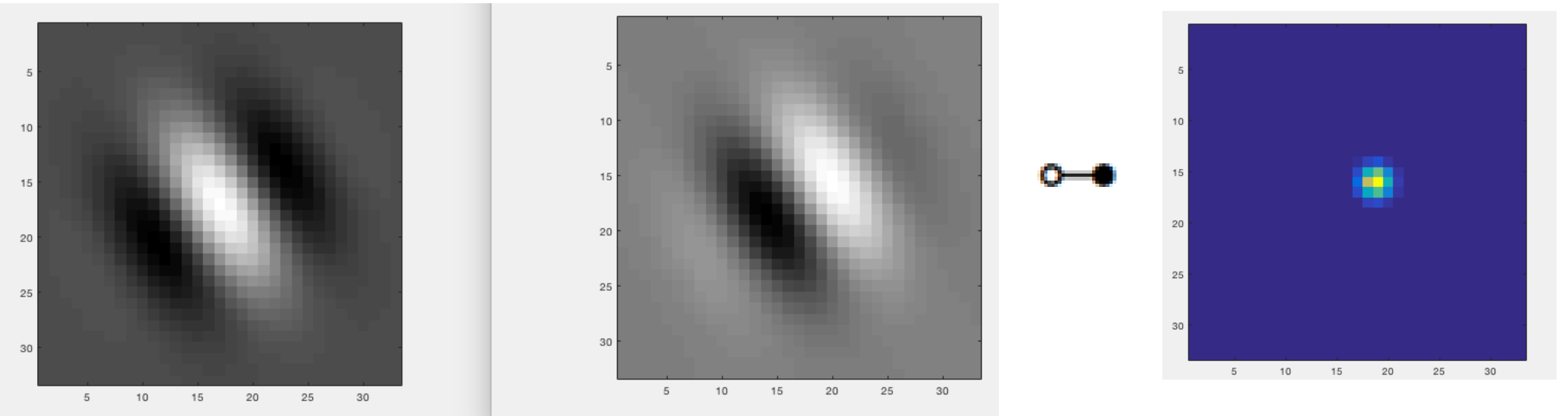
$$h(x, y, \sigma_1, \sigma_2, \omega_1) = \frac{1}{\sigma_1 \sigma_2 2\pi} e^{-(x^2/2\sigma_1^2 + y^2/2\sigma_2^2)} e^{j\omega_1 x}$$

$$e^{-(x^2/2\sigma_1^2 + y^2/2\sigma_2^2)} e^{j\omega_1 x} \rightarrow e^{-(\sigma_1^2(\omega_1 - \omega_x)^2 + \sigma_2^2\omega_y^2)/2}$$



$$e^{-(x^2/2\sigma_1^2 + y^2/2\sigma_2^2)} e^{j\omega_1 x} \longleftrightarrow e^{-(\sigma_1^2(\omega_1 - \omega_x)^2 + \sigma_2^2\omega_y^2)/2}$$

Rotated 2D Gabor Filter





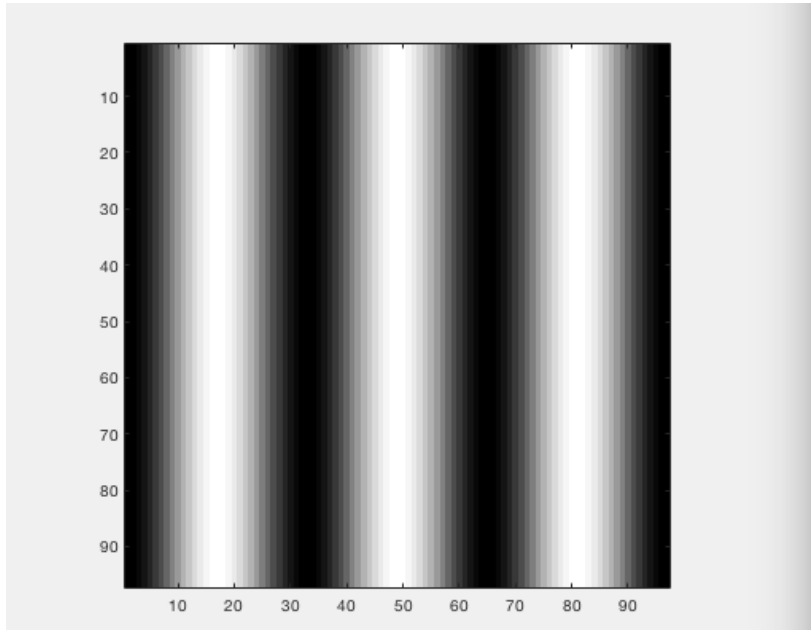
Video 4.2

Kostas Daniilidis

Scale selectivity

Build a system that detects edges and features independent from scale (size)

Let us look at an “unconventional edge”:



$$\cos \omega_0 x$$



$$g'_\sigma(x)$$

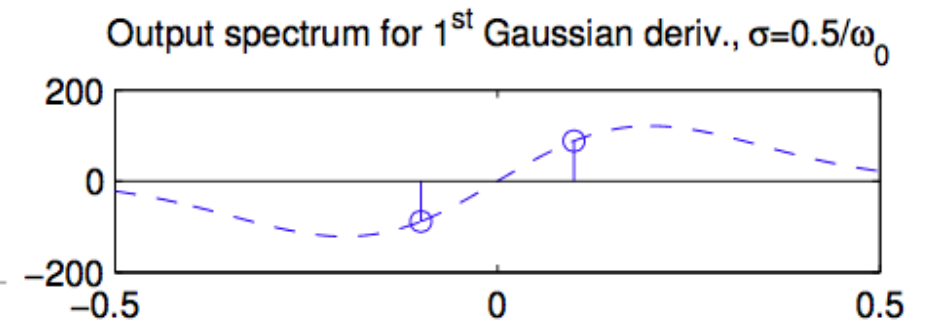
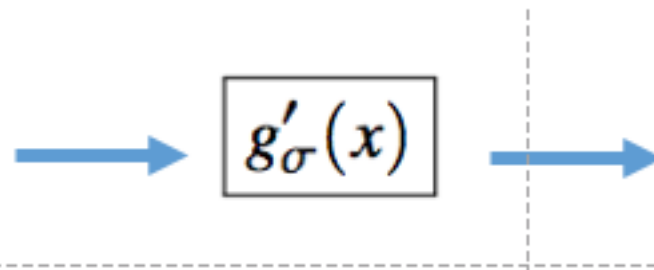
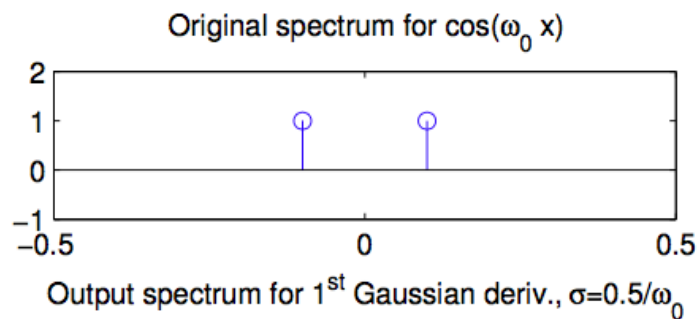


Build a system that detects edges and features independent from scale (size)

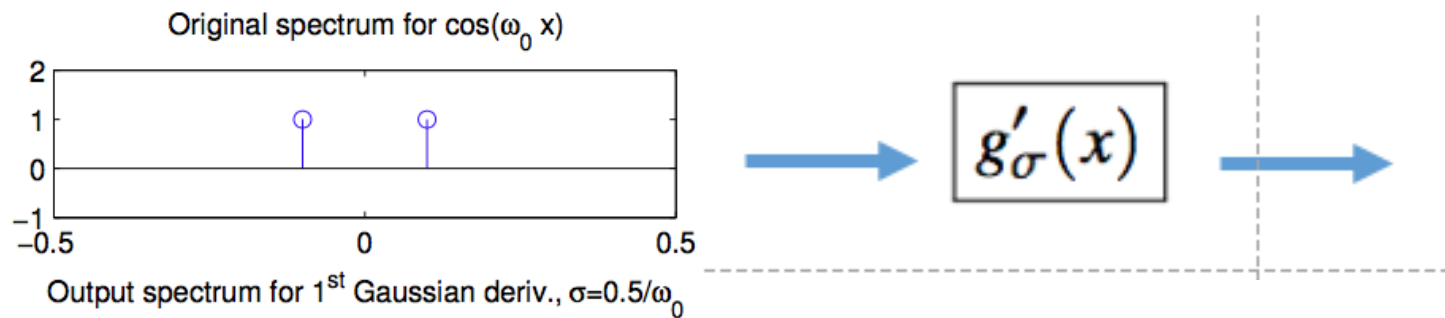
$$\cos \omega_0 x \quad \longrightarrow \quad \boxed{g'_\sigma(x)} \quad \longrightarrow \quad \text{"smoothed derivative"}$$

$$g'_\sigma = \frac{dg_\sigma}{dx} \text{ where } g_\sigma = \frac{1}{\sqrt{2\pi}\sigma} e^{-x^2/2\sigma^2}$$

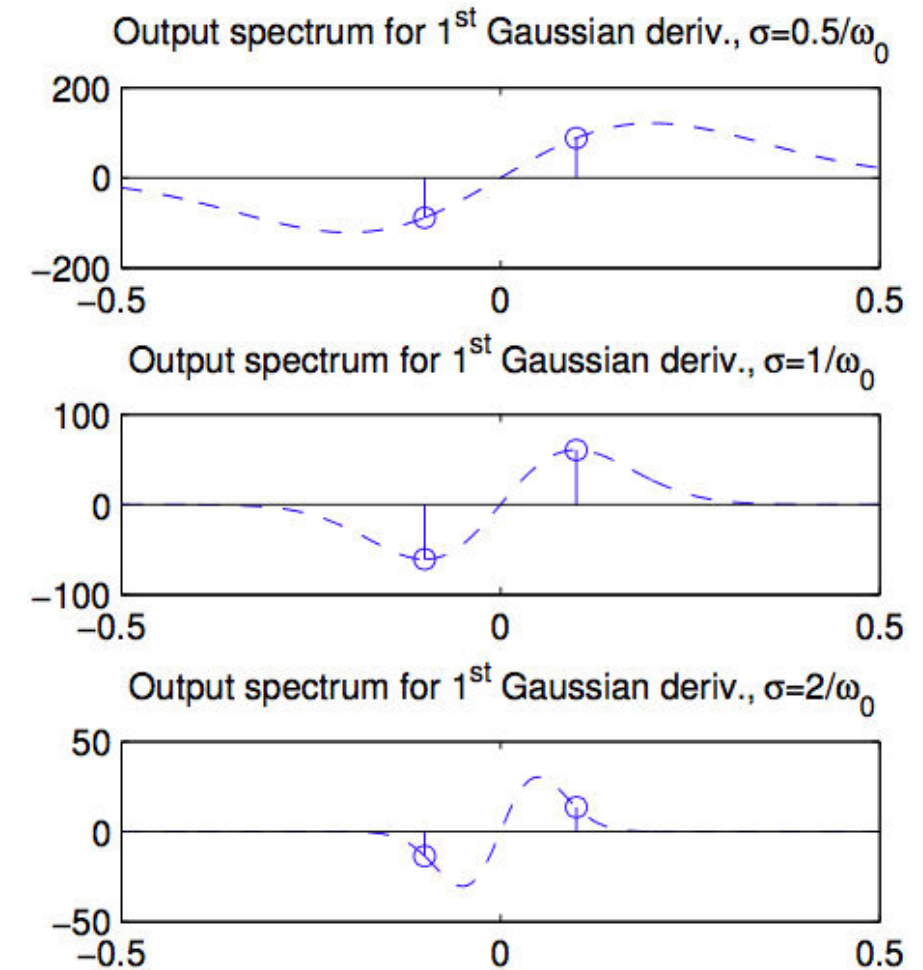
$$\begin{aligned} & \frac{1}{2}(\delta(\omega - \omega_0) + \delta(\omega + \omega_0)) j\omega e^{-\omega^2 \sigma^2 / 2} \\ &= \frac{1}{2}(\delta(\omega - \omega_0) - \delta(\omega + \omega_0)) j\omega_0 e^{-\omega_0^2 \sigma^2 / 2} \end{aligned}$$



Response is maximum when filter scale σ matches incoming scale (ω_0).

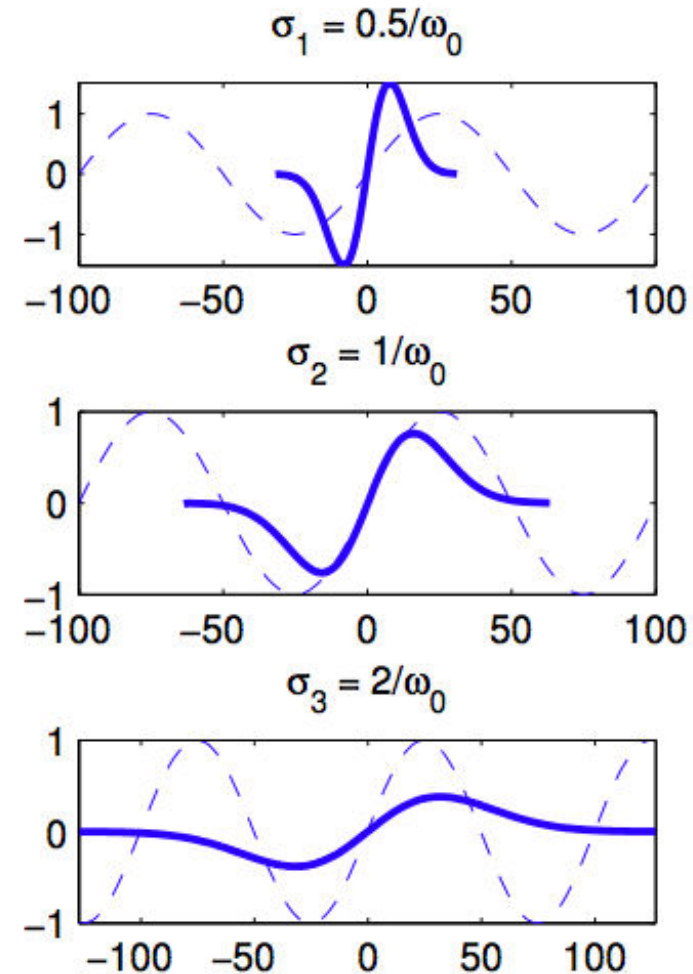


$$j\omega_0 e^{-\omega_0^2 \sigma^2 / 2}$$



Look at edge detection as template matching

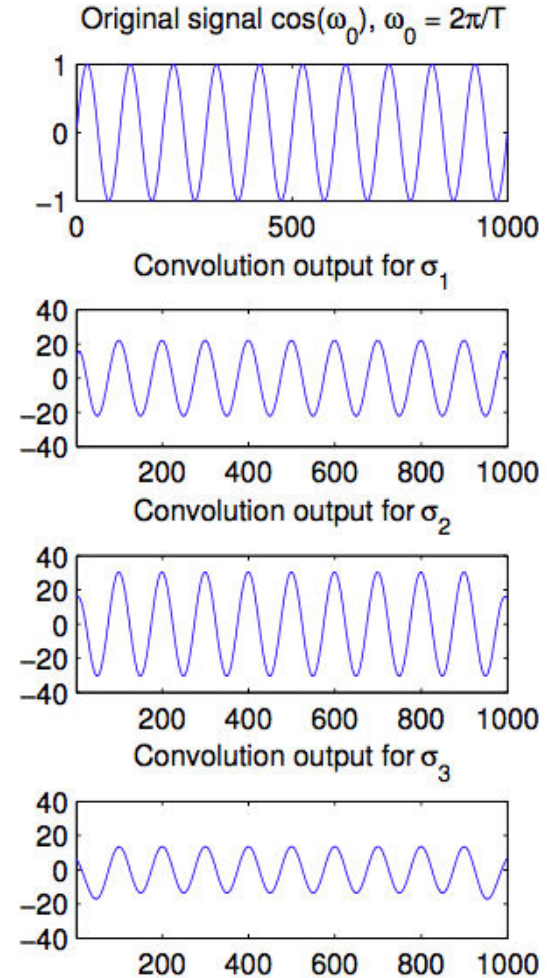
Which size of “edge template” matches the original edge?



Edge detection output for different σ 's:

As σ increases the peaks at the edges weaken!!

$$\omega_0 e^{-\omega_0^2 \sigma^2 / 2}$$

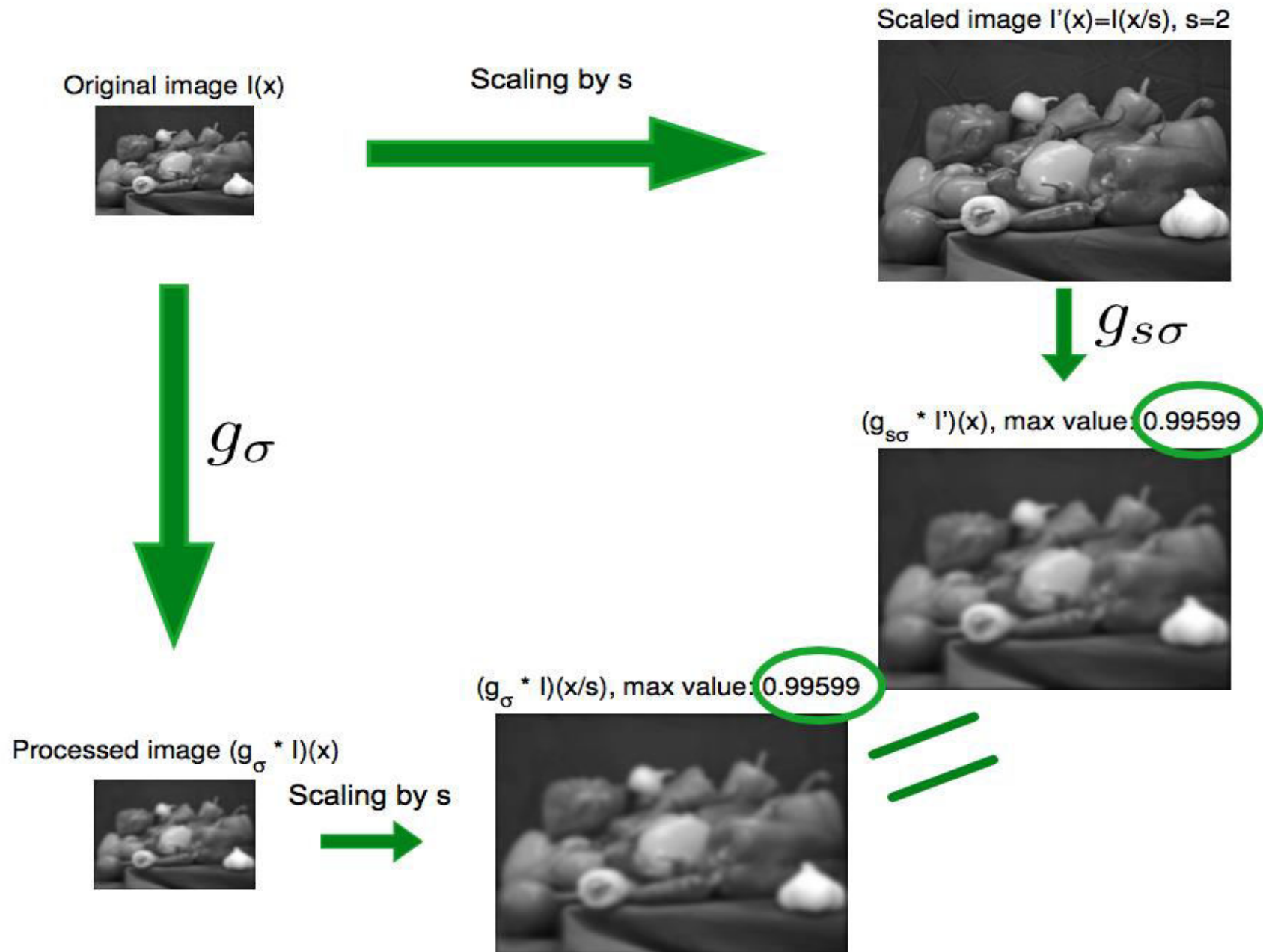


Why we need a scale normalization of the filter!

Assume a scaled version of the original signal $I'(x) = I\left(\frac{x}{s}\right)$ (twice as wide for $s=2$), then calculate the convolution with Gaussian:

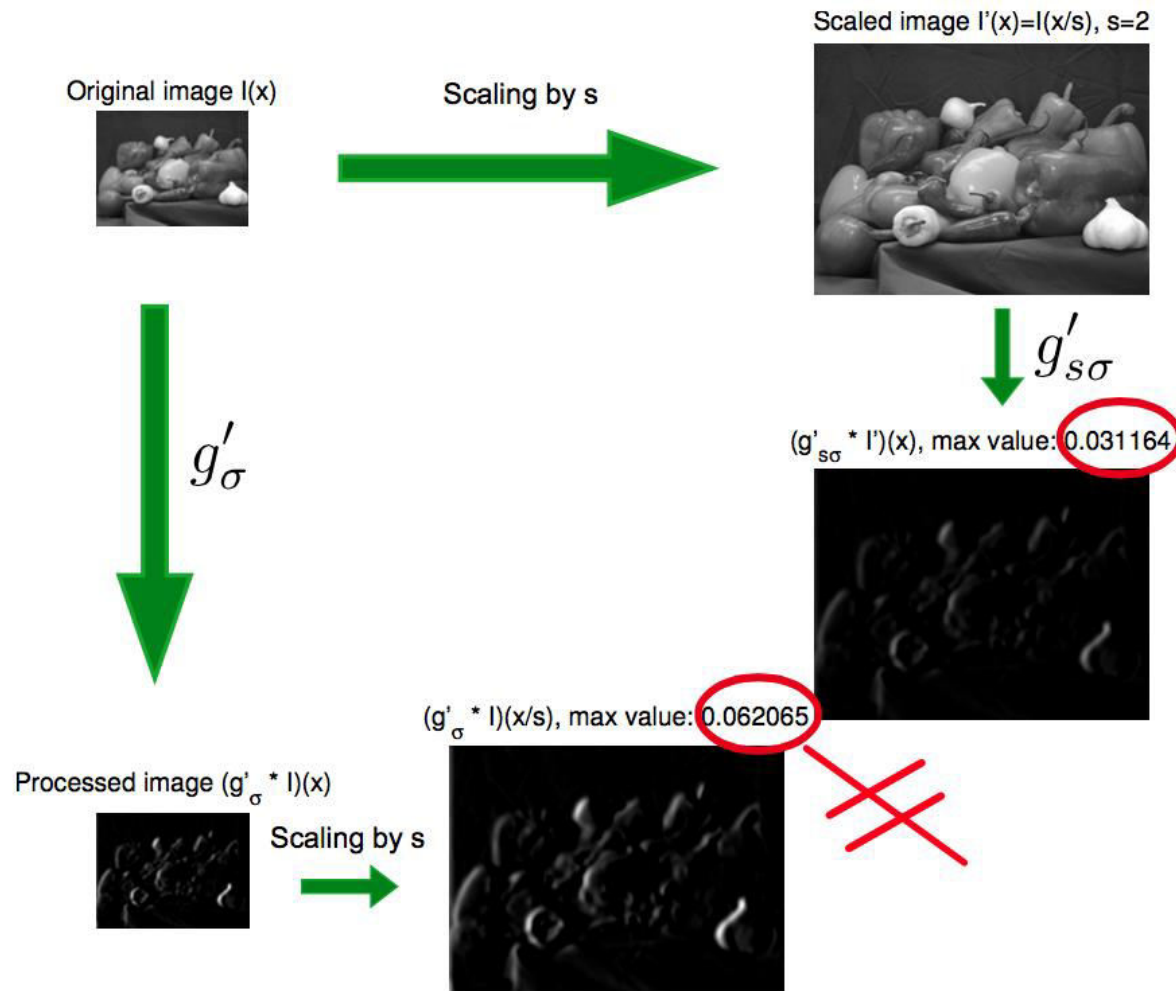
$$(I' \star g_{s\sigma})(x) = (I \star g_{\sigma})\left(\frac{x}{s}\right)$$

Scaling by s and convolving with **scaled** Gaussian is the same as applying a Gaussian and then **scaling** by s !!!

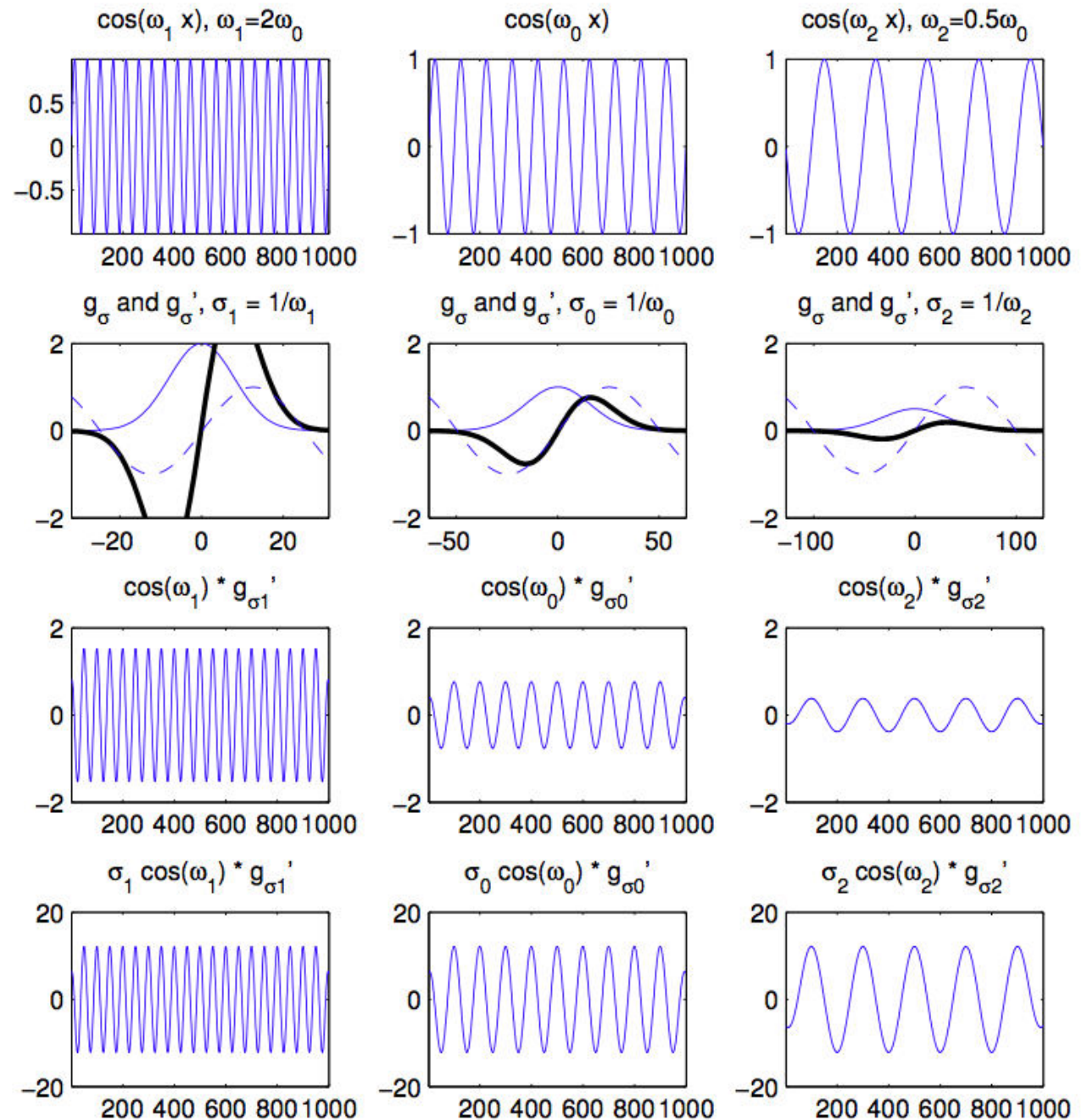


But this is not true for the
1st derivative!

$$(I' \star g'_{s\sigma})(x) = \frac{1}{s} (I \star g'_\sigma) \left(\frac{x}{s} \right)$$

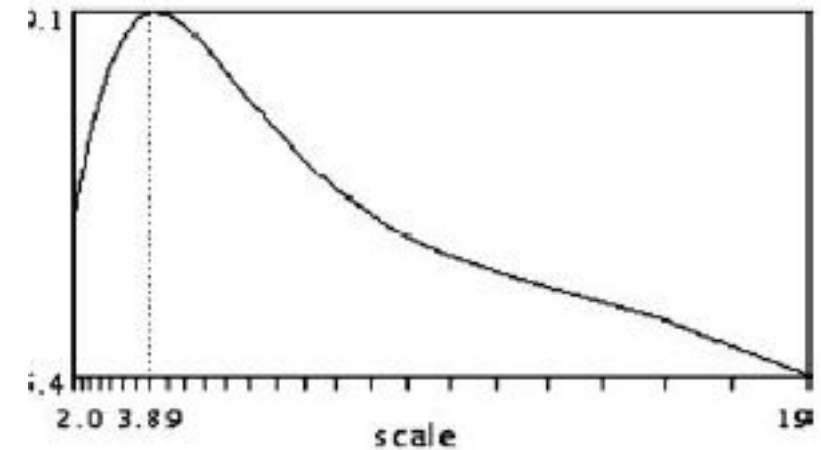
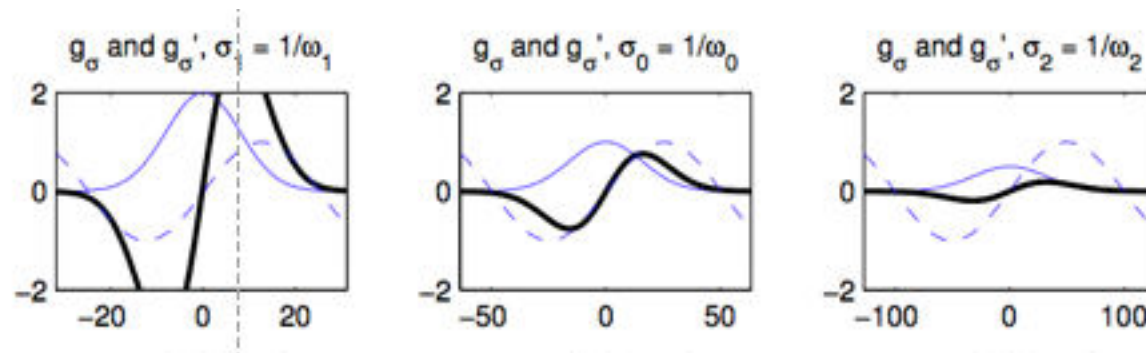


No matter what the scale of the feature, edge detector (1st Gaussian derivative) response should be the same when the filter matches the feature scale.



Can we find (select) the intrinsic image scale?

Yes, by taking the maximum over scale!





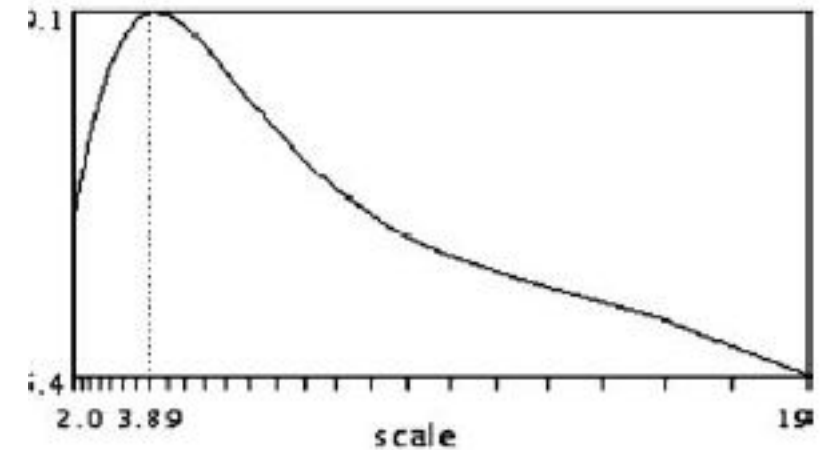
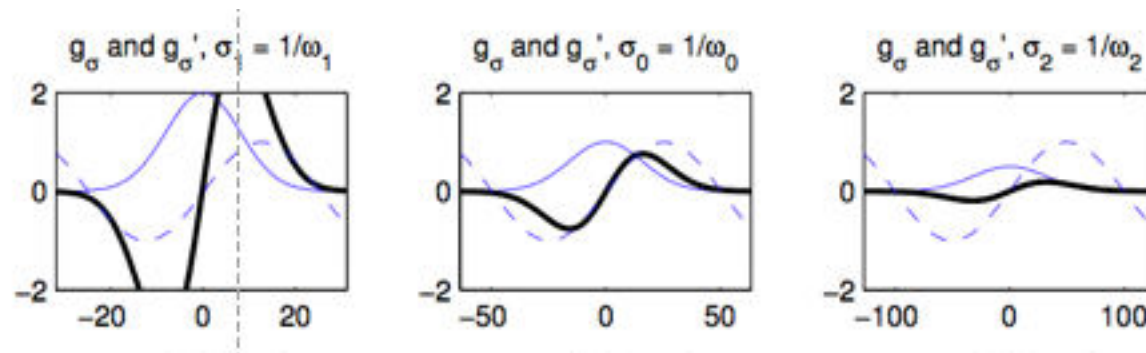
Video 4.3

Kostas Daniilidis

Scale Invariant Feature Transform (SIFT)

Can we find (select) the intrinsic image scale?

Yes, by taking the maximum over scale!



Scale selection and invariance



Tony Lindeberg

Feature detection with automatic scale selection

Authors	Tony Lindeberg
Publication date	1998/11/1
Journal	International Journal of Computer Vision
Volume	30
Issue	2

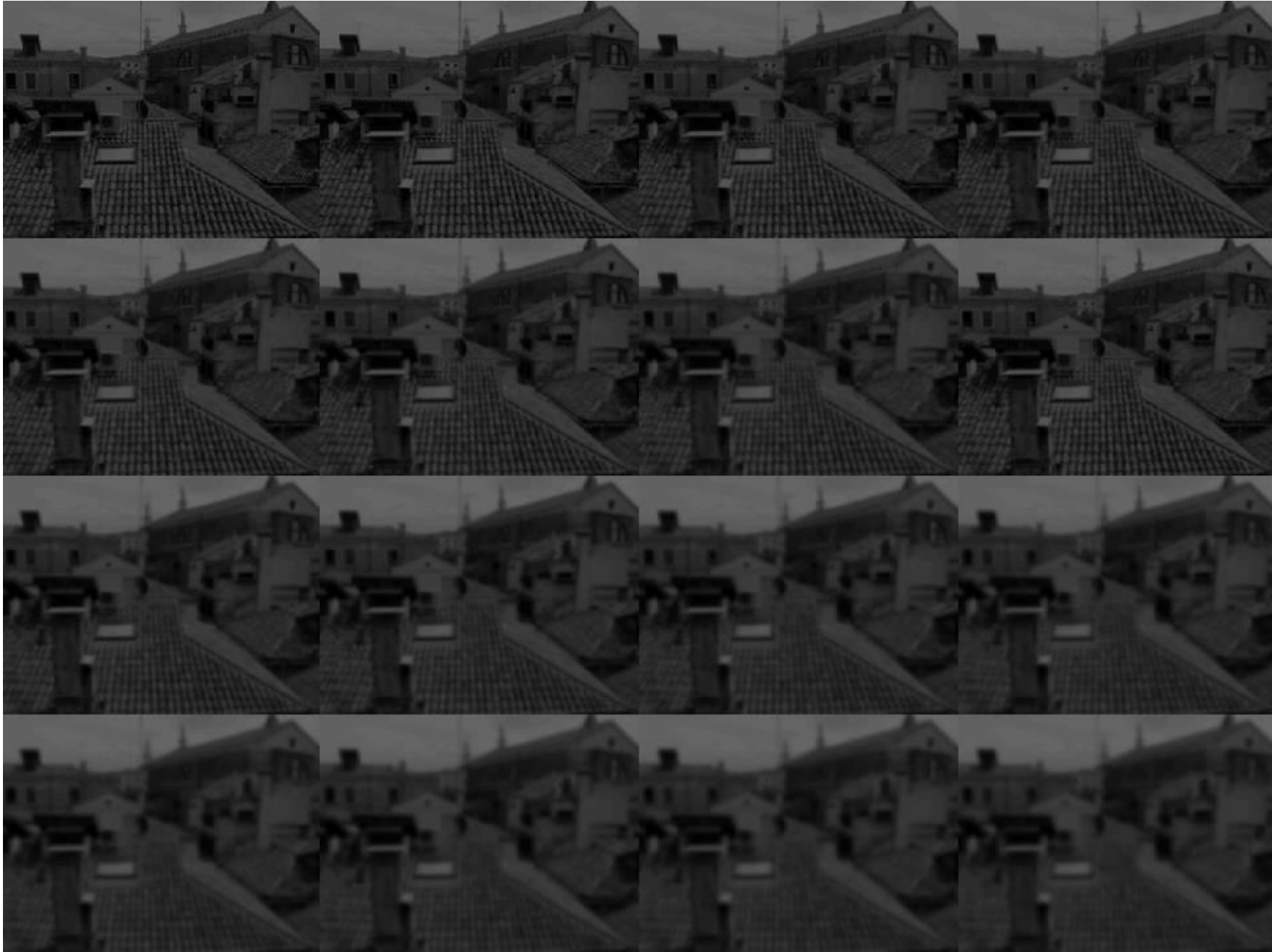


David Lowe

Distinctive image features from scale-invariant keypoints

Authors	David G Lowe
Publication date	2004/11/1
Journal	International journal of computer vision
Volume	60
Issue	2

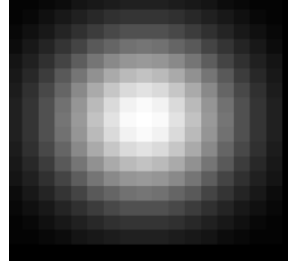
The notion of scale space



How is scale space built?



*

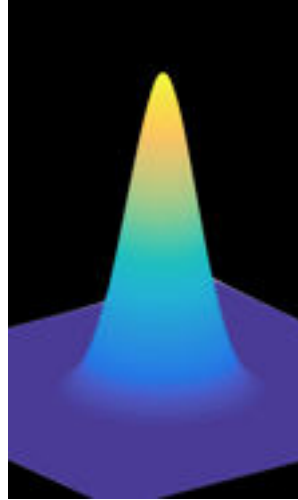


=



2D Gaussian

* means convolution



$$L(x, y, \sigma) = G(x, y, \sigma) * I(x, y)$$

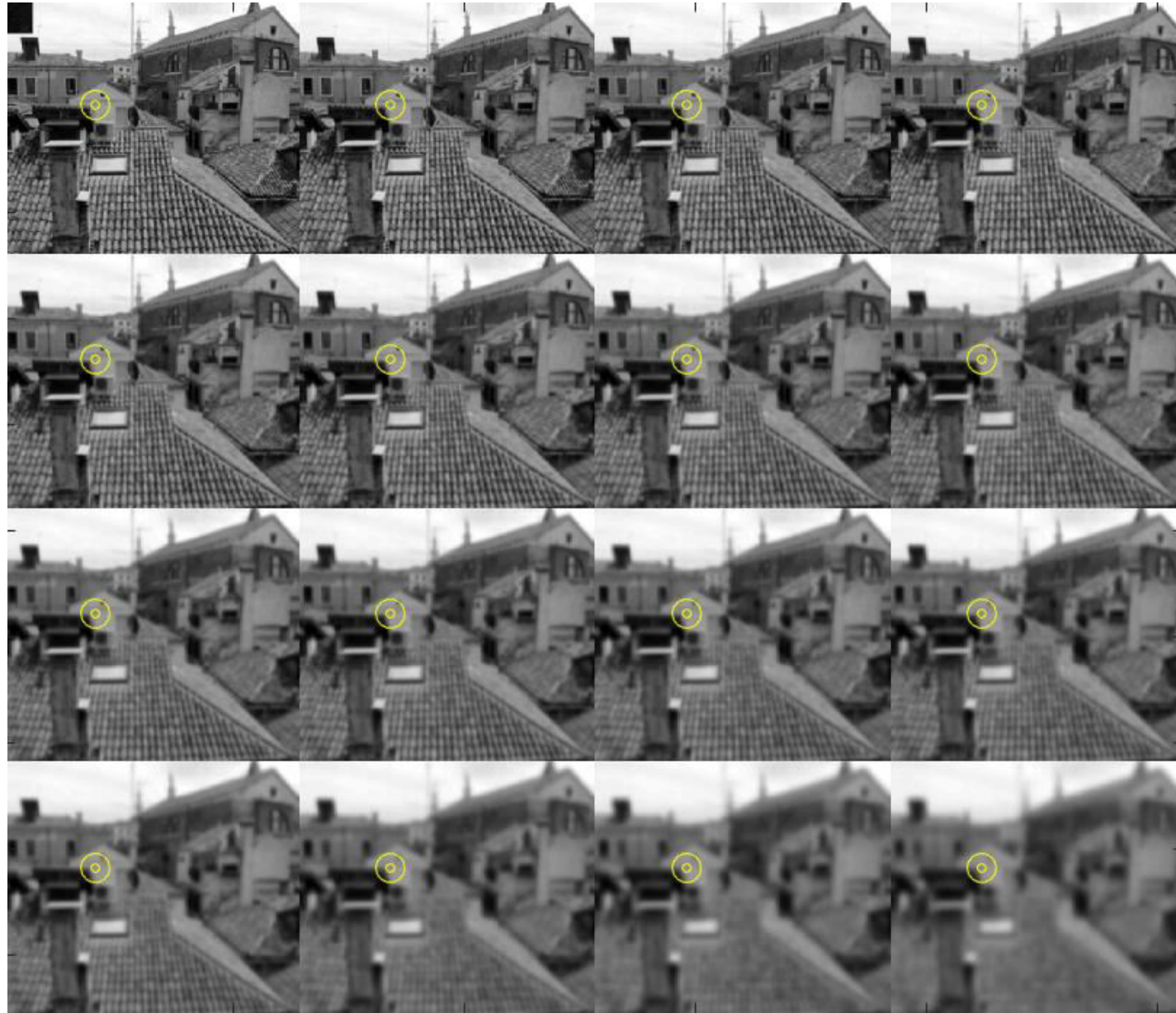
$$G(x, y, \sigma) = \frac{1}{2\pi\sigma^2} e^{-\frac{x^2+y^2}{2\sigma^2}}$$

The same scale but subsampled

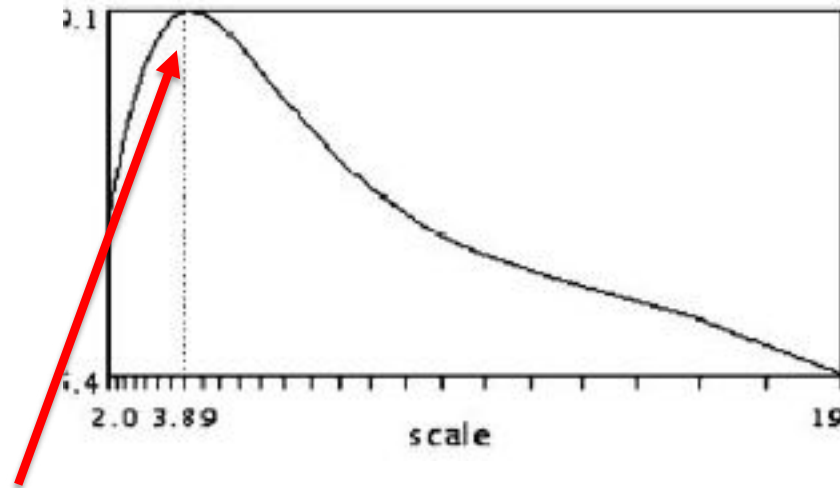


We subsampled it every time that the sigma of the Gaussian was doubled!

Now look at the same pixel across scale

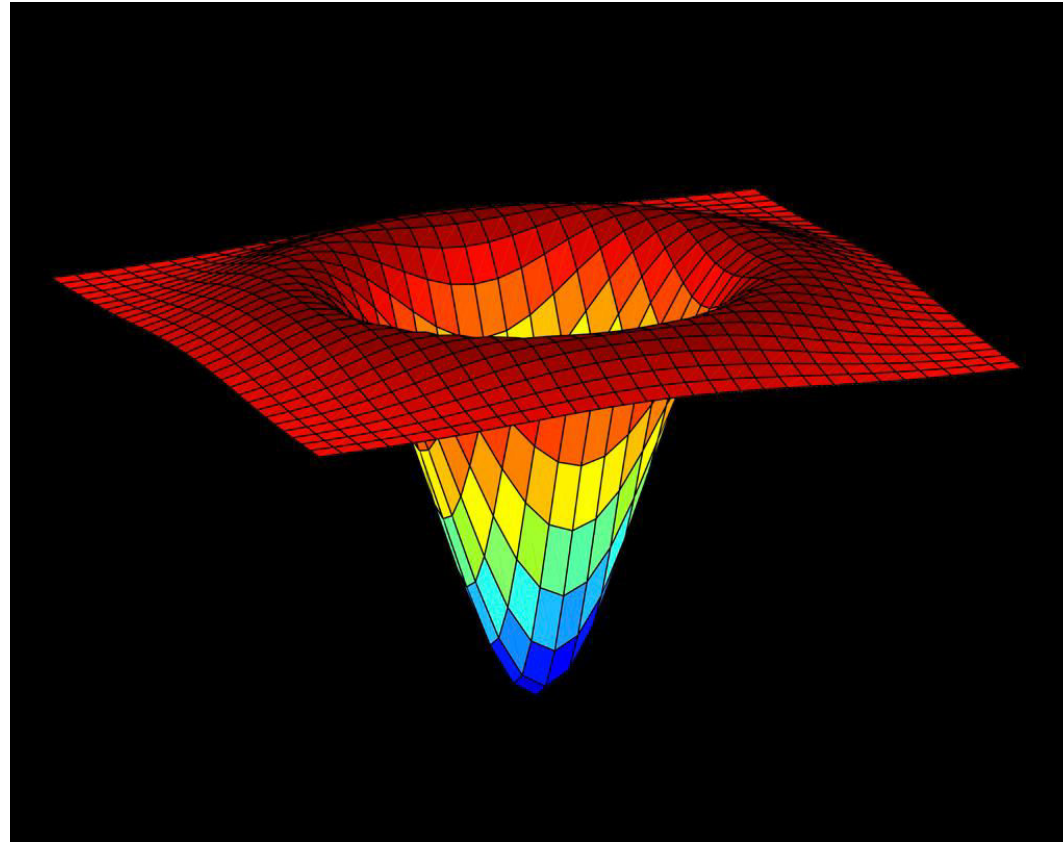


Scale selection



- The maximum across scale is the **intrinsic** scale of the image structure
- if the smoothed value is **scale normalized**.
- It turns out that only the derivatives of the Gaussian responses can be normalized.

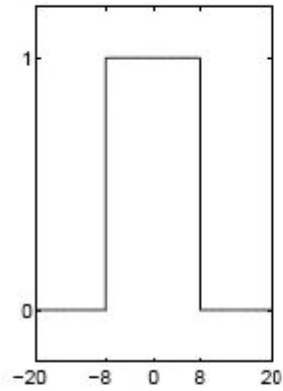
We choose the 2nd derivative (trace of Hessian) ,
called Laplacian of Gaussian (LoG)



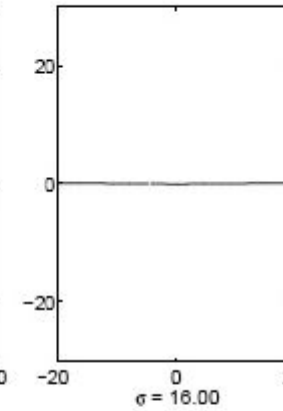
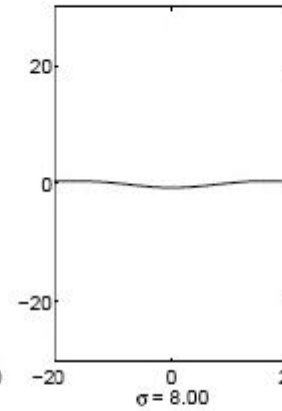
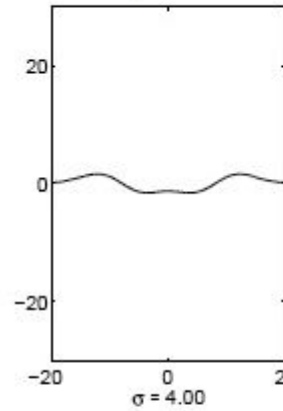
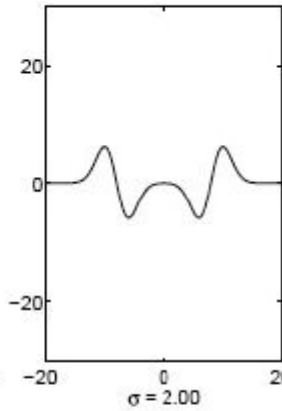
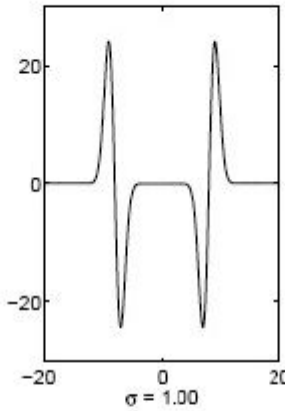
Which has the nice property that it can be
approximated as the difference of two Gaussians
and can detect blob like features!

Normalization of the 2nd Gaussian Derivative

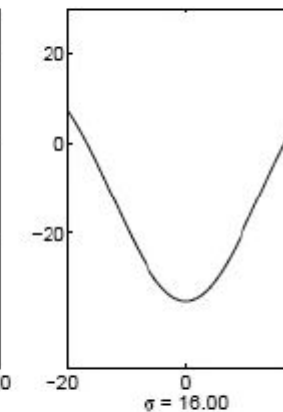
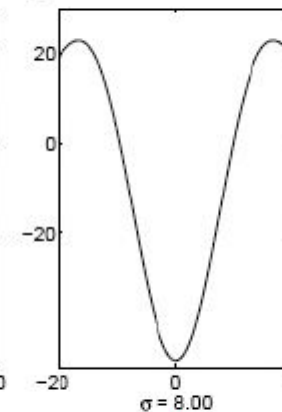
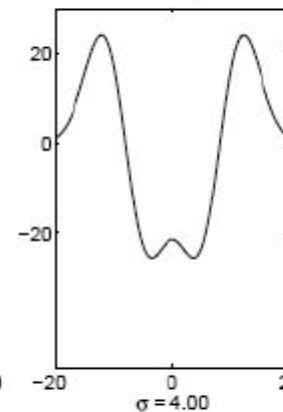
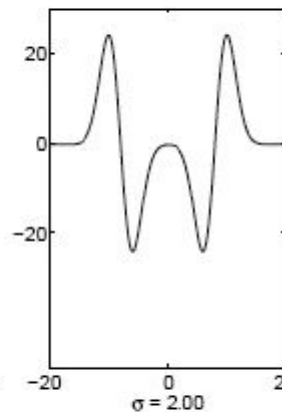
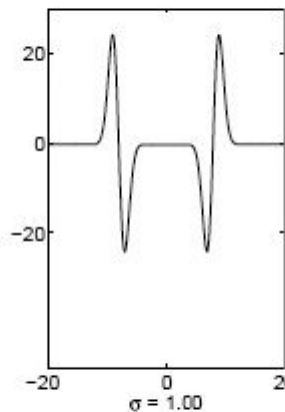
Original signal



Unnormalized Laplacian response



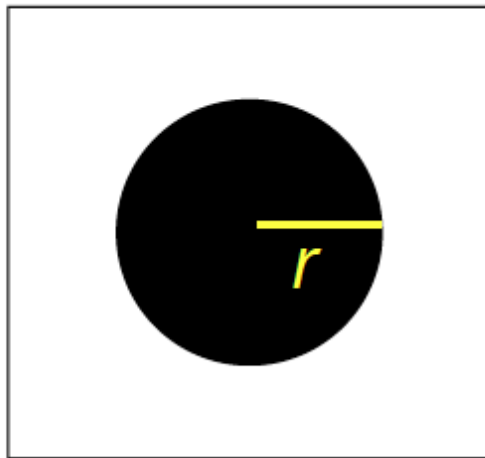
Scale-normalized Laplacian response



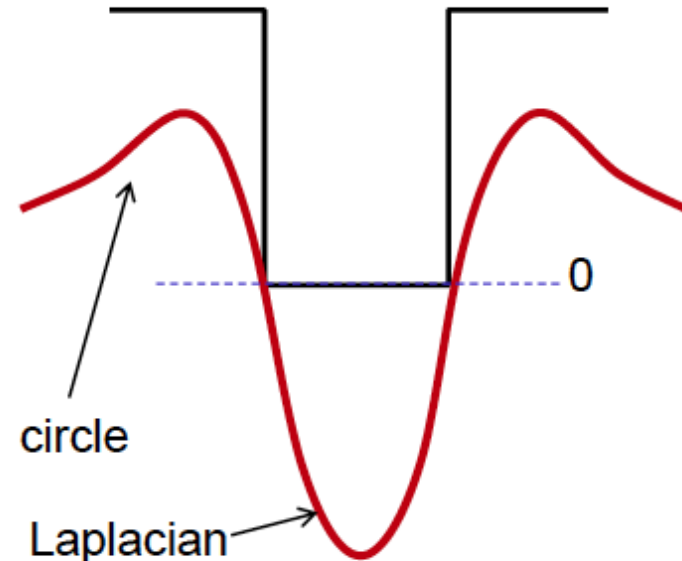
maximum

Scale selection

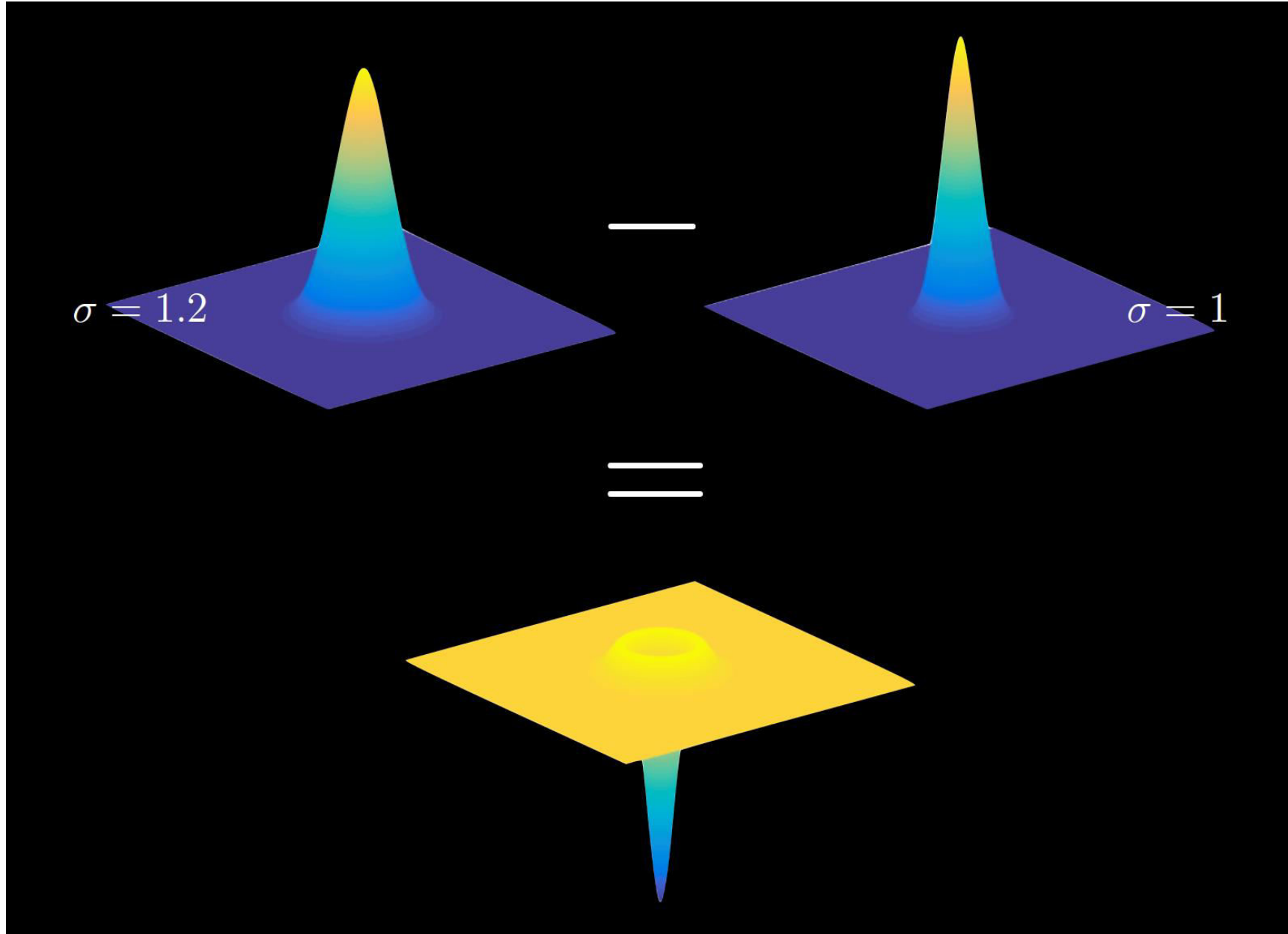
- At what scale does the Laplacian achieve a maximum response to a binary circle of radius r ?
- To get maximum response, the zeros of the Laplacian have to be aligned with the circle
- The Laplacian is given by (up to scale):
$$(x^2 + y^2 - 2\sigma^2) e^{-(x^2 + y^2)/2\sigma^2}$$
- Therefore, the maximum response occurs at $\sigma = r / \sqrt{2}$.



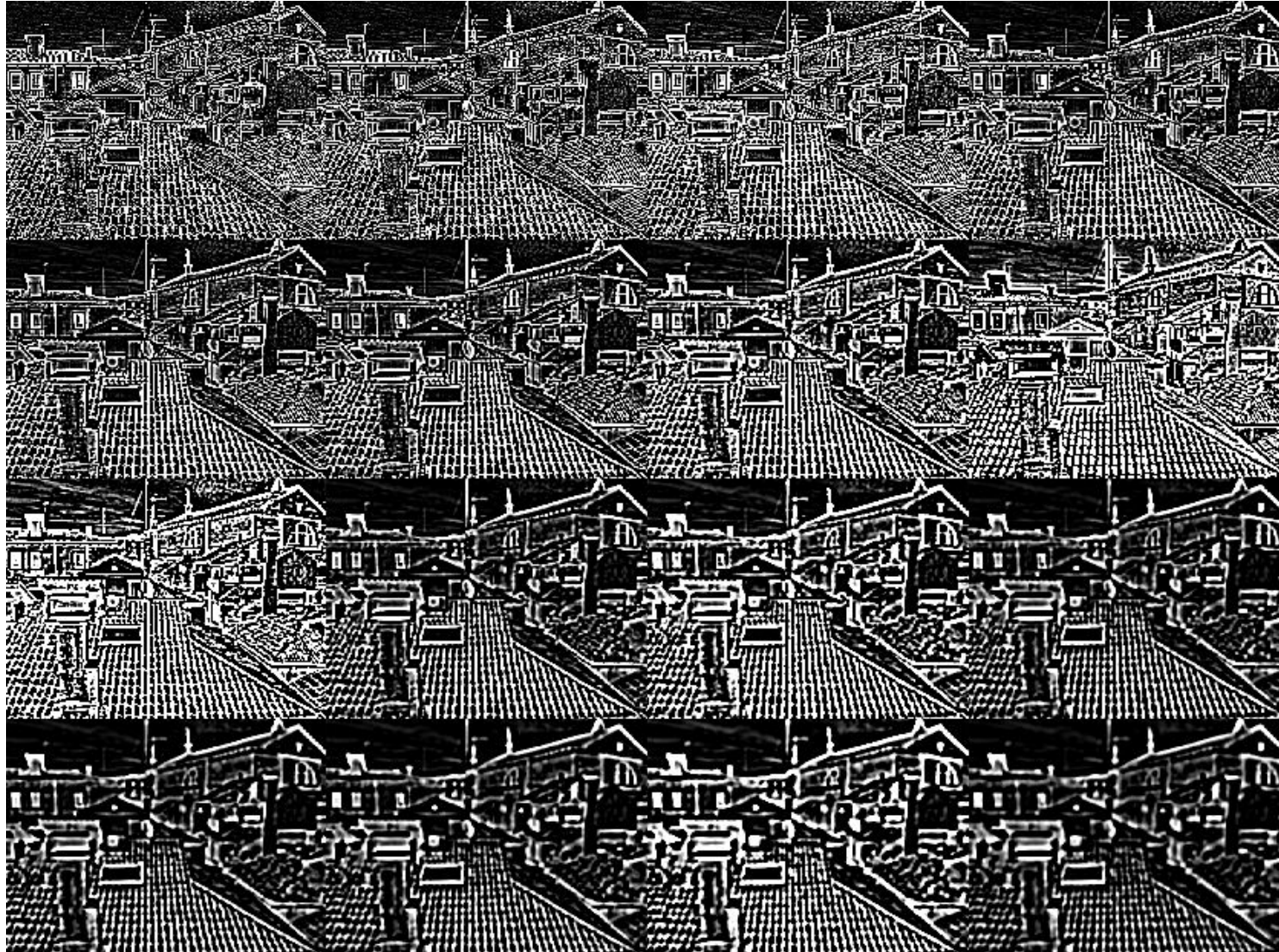
image



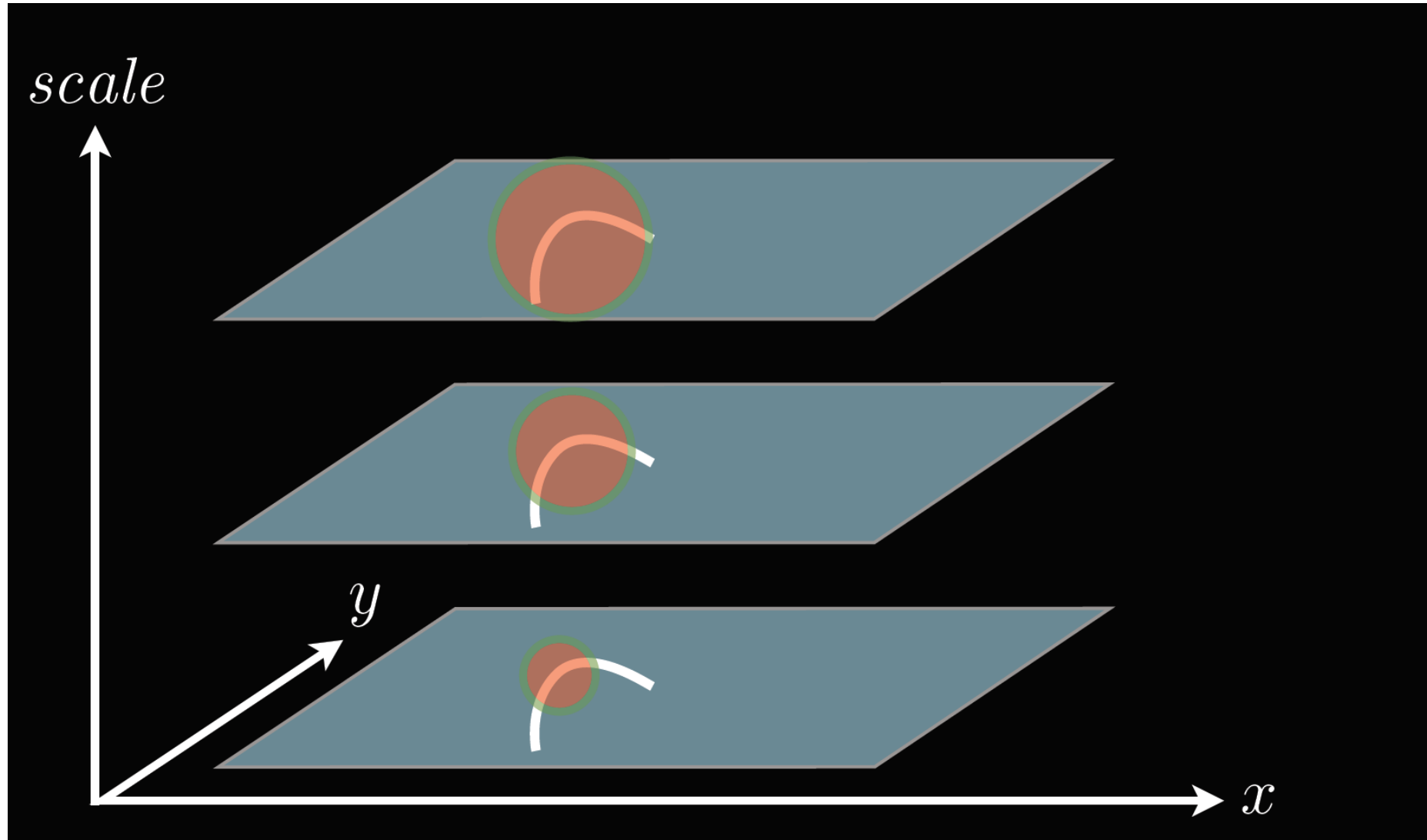
Difference of Gaussians (DoG)



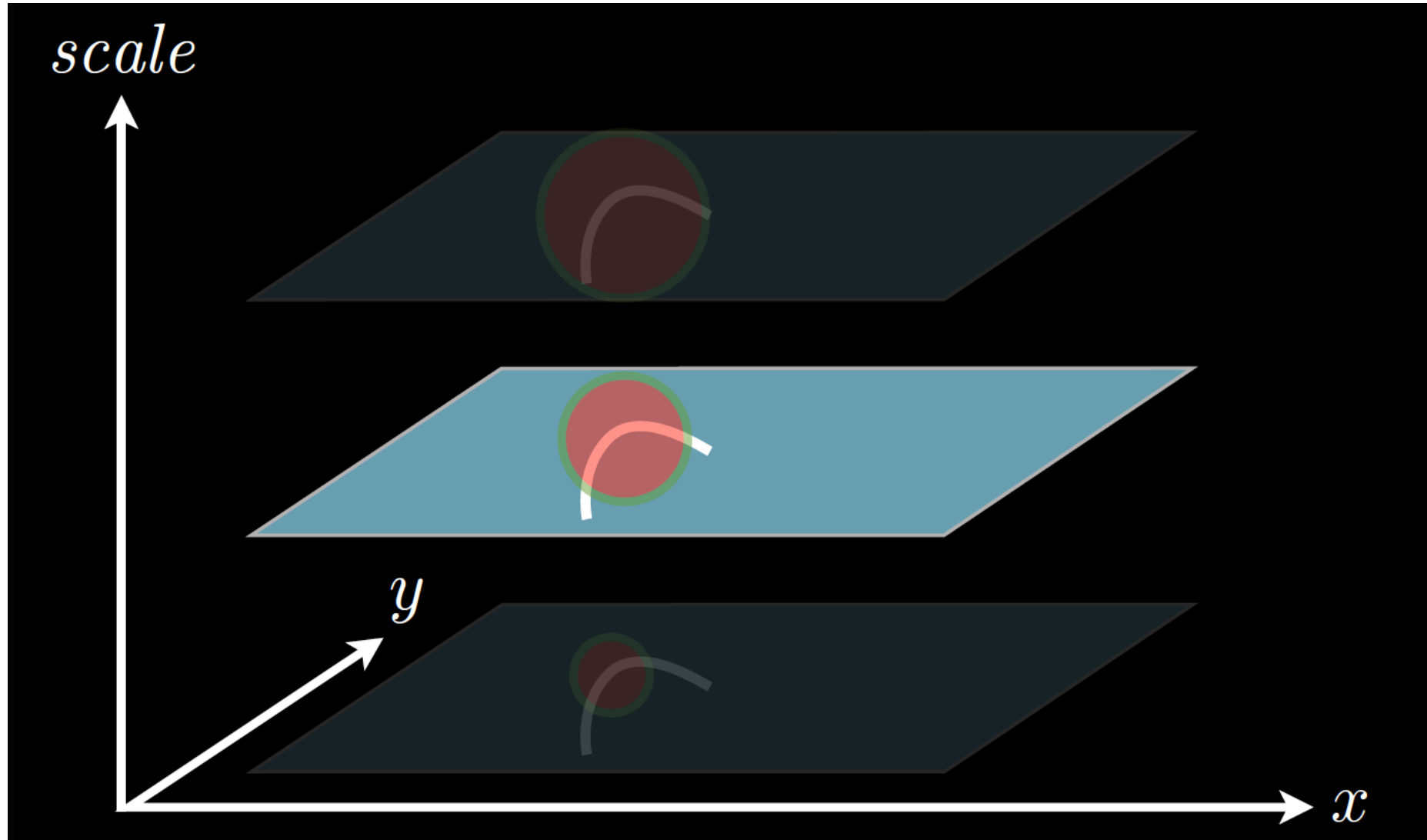
Laplacian Scale Space



We convolve DoG across space at different scales

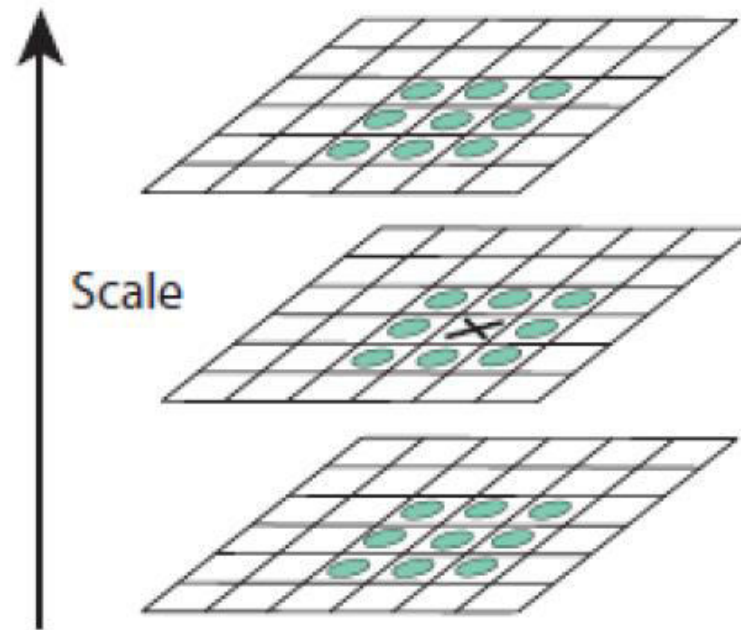


We convolve DoG across space at different scales
and detect maximum

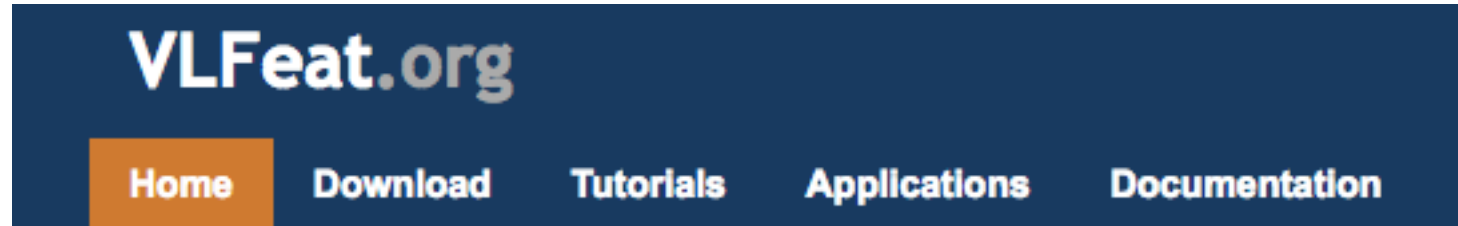


So, where is a SIFT keypoint?

- Definition of a keypoint: Maximum in the $3 \times 3 \times 3$ (x, y, σ) region of the point.



Vedaldi's vlfeat



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[Visual Geometry Group](#) ([directions](#))

Tel. +44 1865 273 127

[Résumé](#) [Google Scholar](#)

Selected σ is visualized with a circle



Denoting the support region of the feature

Detector is rotation invariant



Because Laplacian is isotropic and a maximum in (x, y, σ) is invariant to rotations.

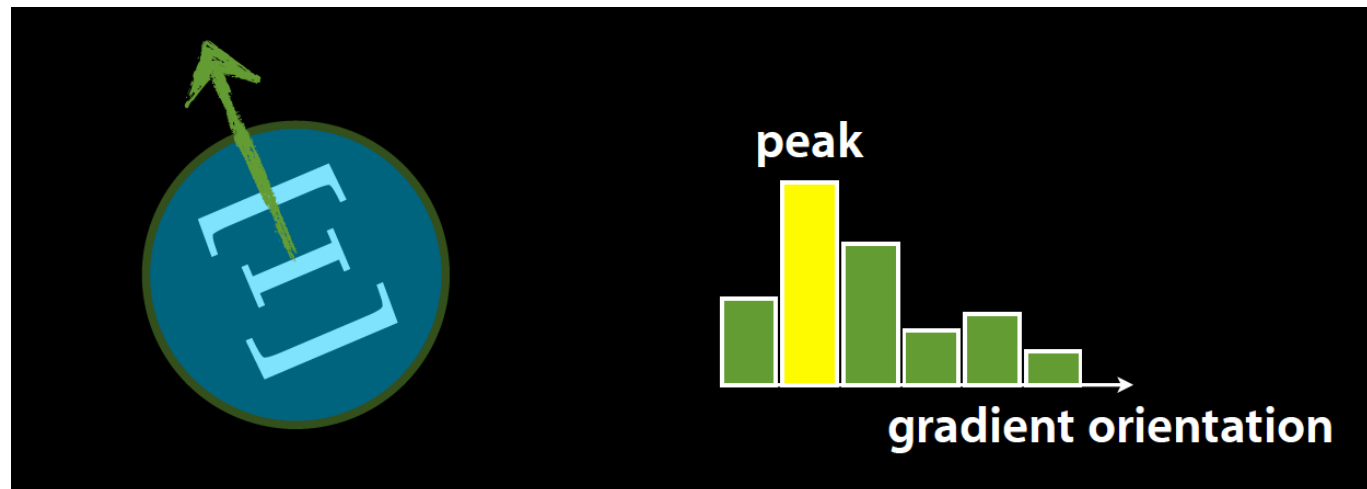
Descriptor invariance

- Since the intrinsic scale is detected (circle size) all circles will be normalized to a 16x16 region.



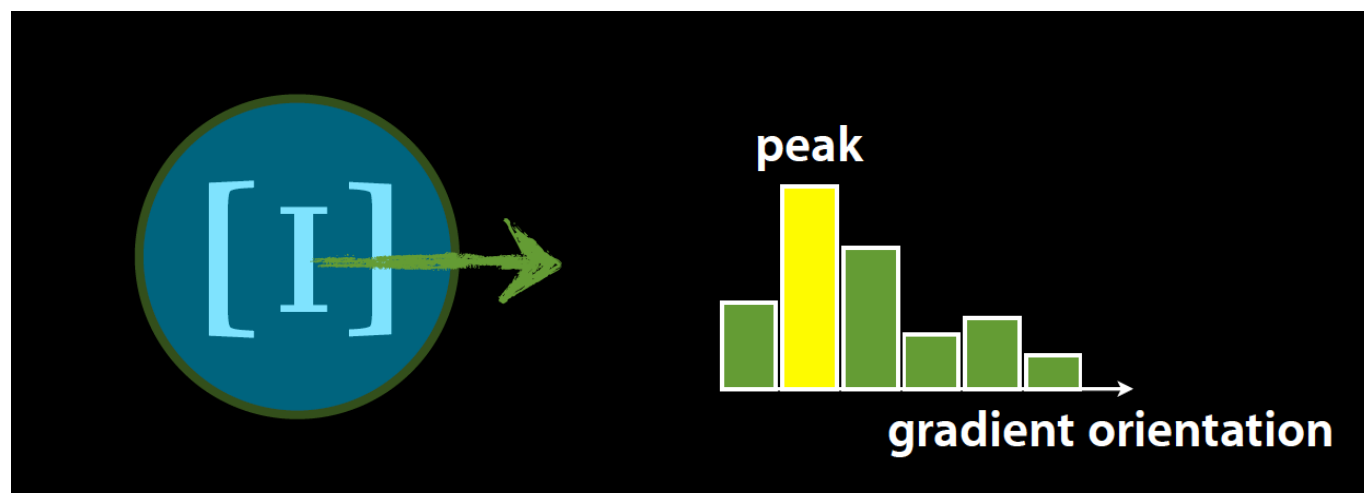
The descriptor should be also **rotation** invariant

- 1st Step: Find dominant orientation for the patch



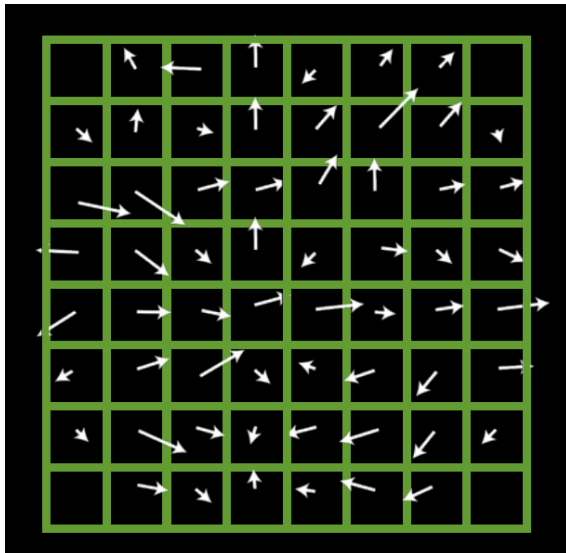
The descriptor should be rotation invariant

- 1st Step: Find dominant orientation for the patch
- 2nd Step: Rotate patch to point along x-axis



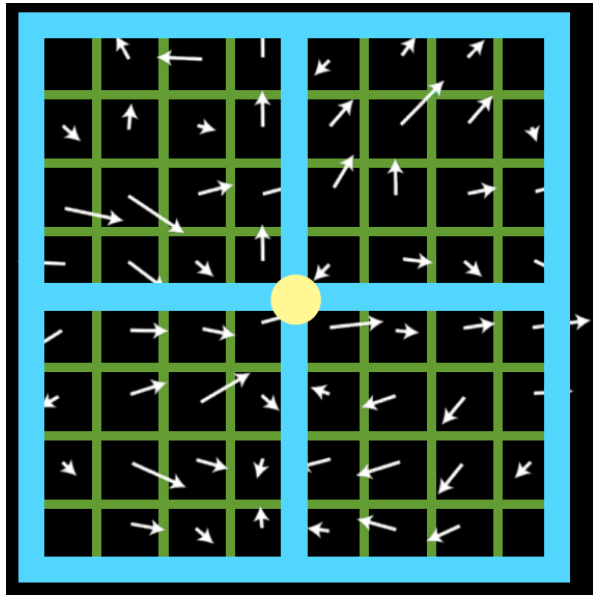
To extract a feature descriptor from a cell

- Compute Image Gradients



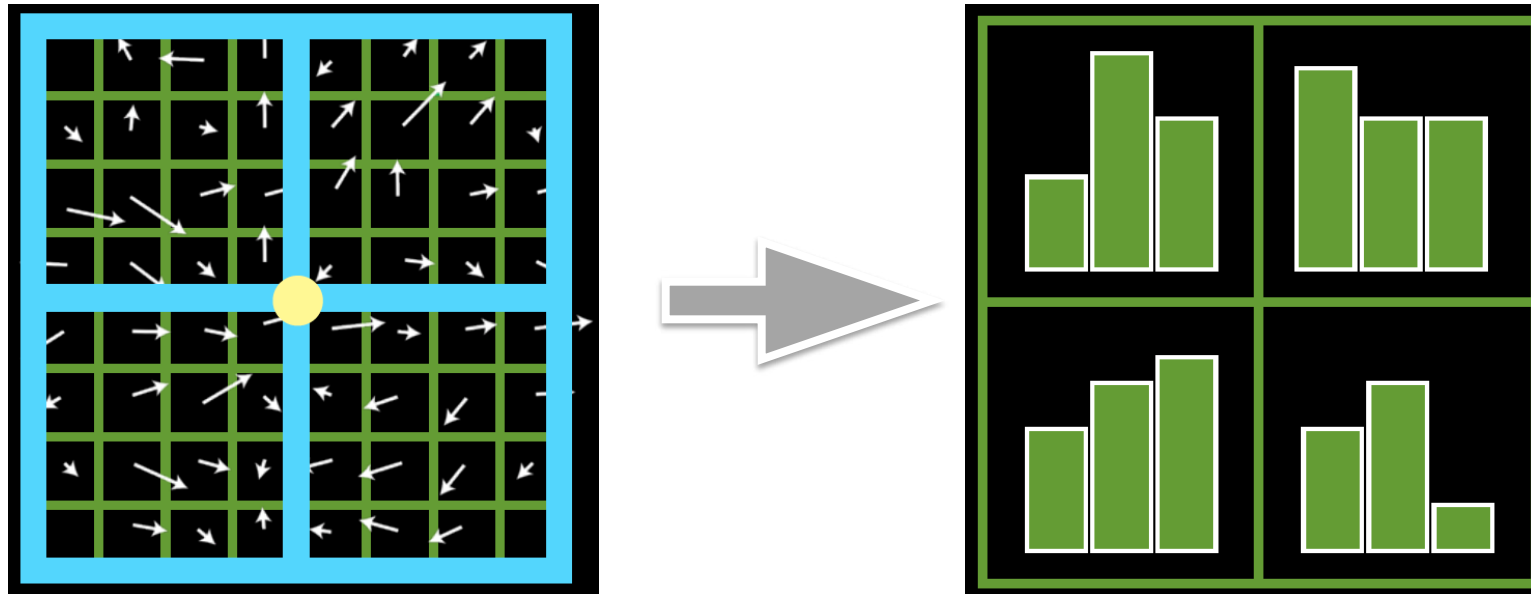
To extract a feature descriptor from a cell

- Compute Image Gradients
- Accumulate gradients along cells



To extract a feature descriptor from a cell

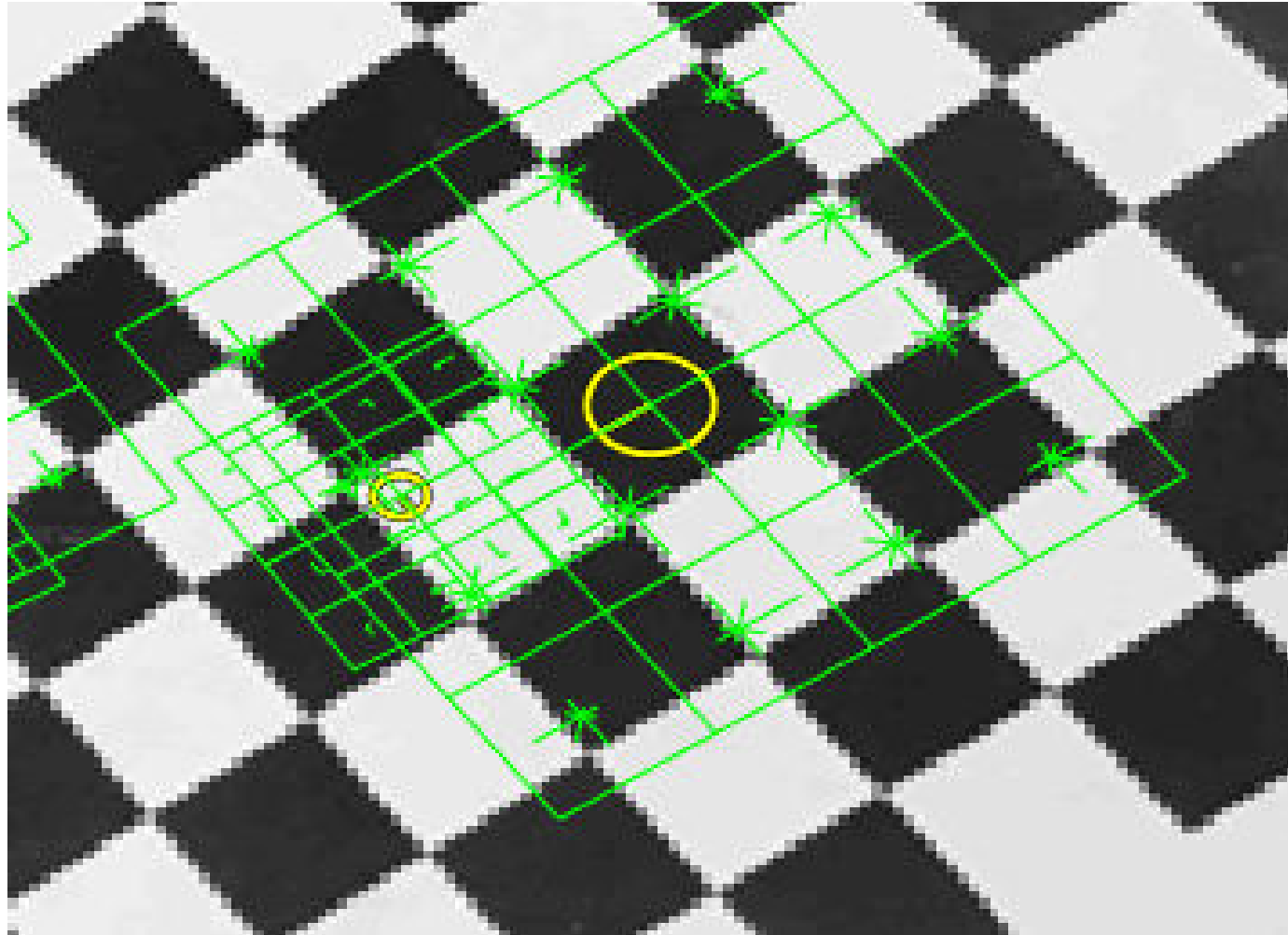
- Compute Image Gradients
- Accumulate gradients along cells
- Form image descriptor



As a matter of fact it is
a 4x4 grid of histograms at each keypoint



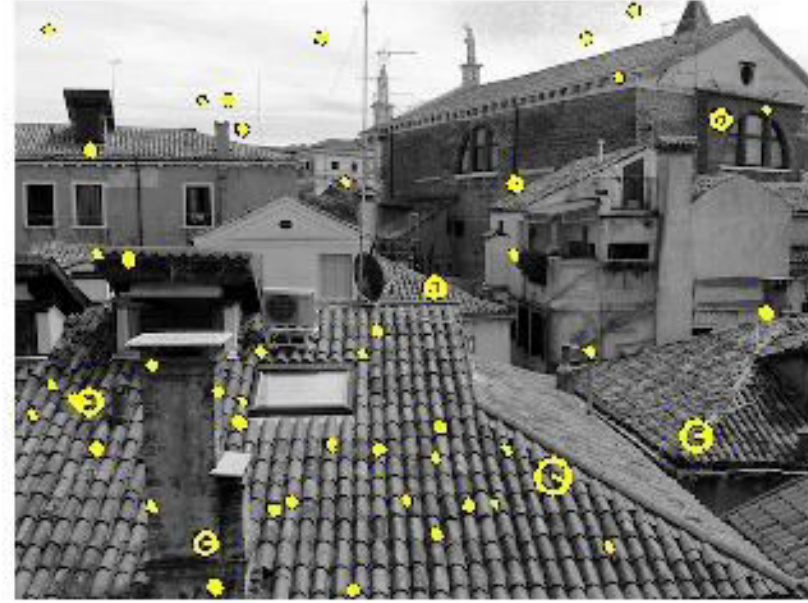
The descriptor is an 128×1 vector which together with σ, θ characterize the keypoint.



Example of SIFT detections and feature extraction



Input Image



Example Detections

Example of SIFT detections and feature extraction



Input Image



Example Detections

Extracted Feature Descriptors



Using SIFT for image matching

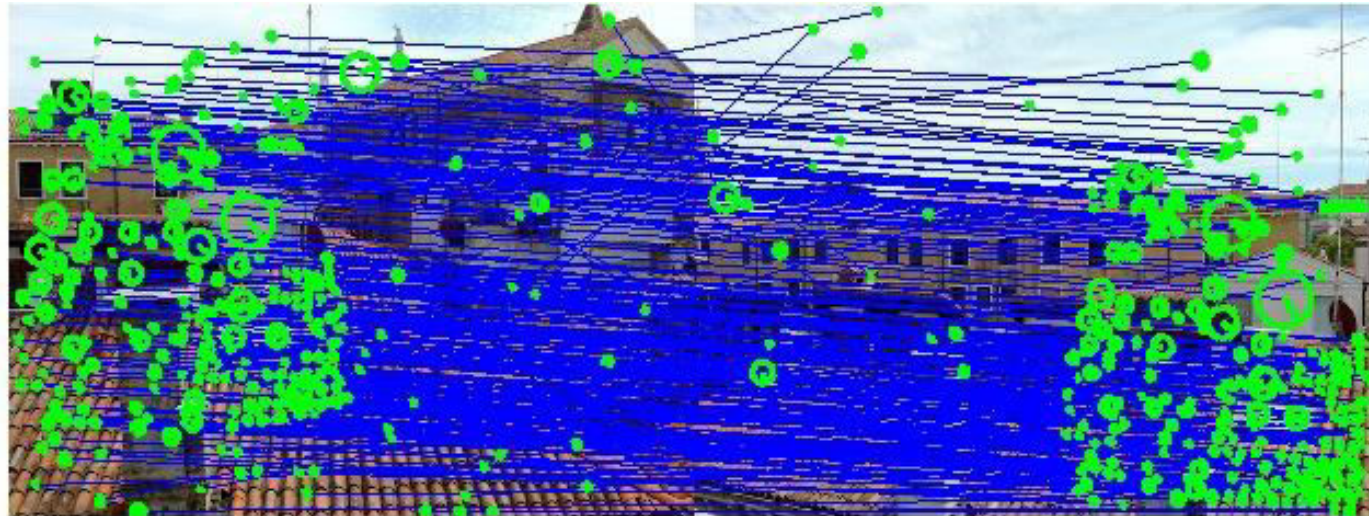


Original Image Pair

Using SIFT for image matching



Original Image Pair

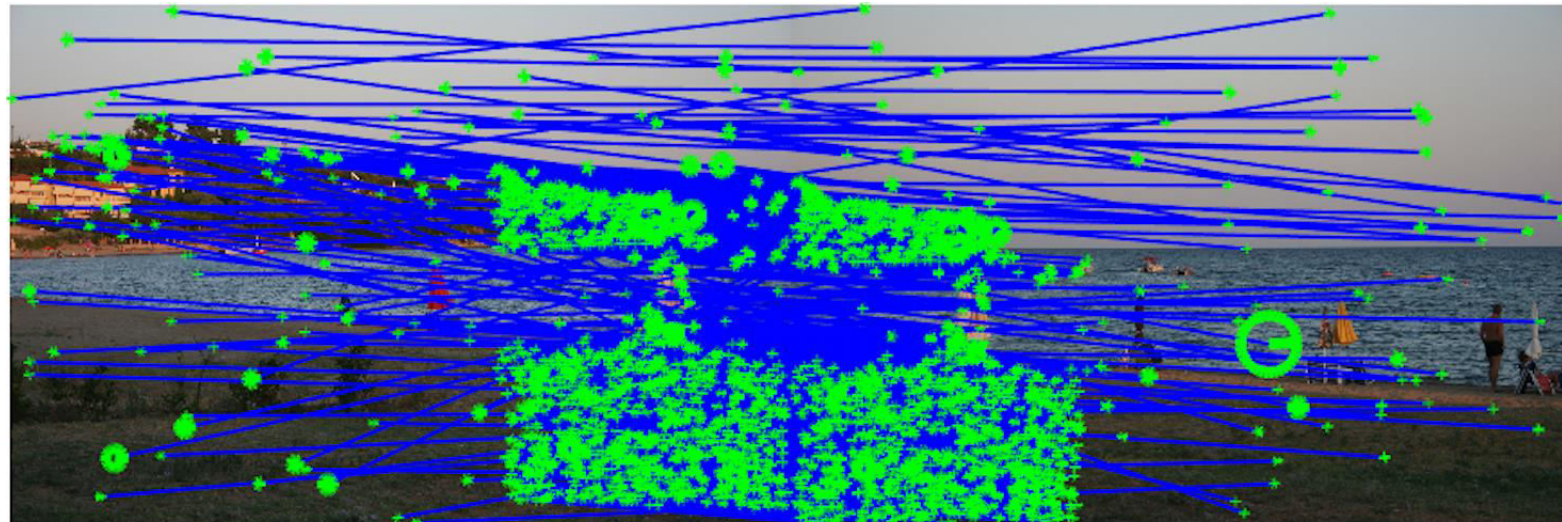


Matched features

Create Image Mosaic



1. Get an image pair



2. Establish correspondences between matching features
Property of Penn Engineering, Kostas Daniilidis

Create Image Mosaic



3. Keep only consistent matches (inliers)



4. Compute homography and warp 2nd image
Property of Penn Engineering, Kostas Daniilidis

Create Image Mosaic



5. Repeat to extend the mosaic



Find Location



Query Image

We want to find a match in a dataset of
given images

Pe



Pe



Find Location



Query Image



Good Matches



Medium Matches



Bad Matches

Find Location



Good Match



Medium Match



Bad Match

Property of Penn Engineering, Kostas Daniilidis

SIFT Features

- SIFT detector can automatically
 - Select scale
 - Compute dominant rotation
- SIFT descriptor
 - Is a grid of histogram of gradient orientations
 - On a region normalized with respect to scale and rotation



Video 4.4

Kostas Daniilidis

Image features

Why do we want features?

- As an image representation for
 - Matching two images
 - Image Statistics
- For what purpose?
 - AR tracking
 - Mosaicking
 - 3D models
 - Visual odometry
 - Video tracking



What is a good feature?

- A feature that enables matching when image undergoes
 - Geometric deformations
 - Photometric changes
 - Intra-class changes
- but at the same time is distinctive
- can be computed efficiently requires low storage

A set of features is an image representation!

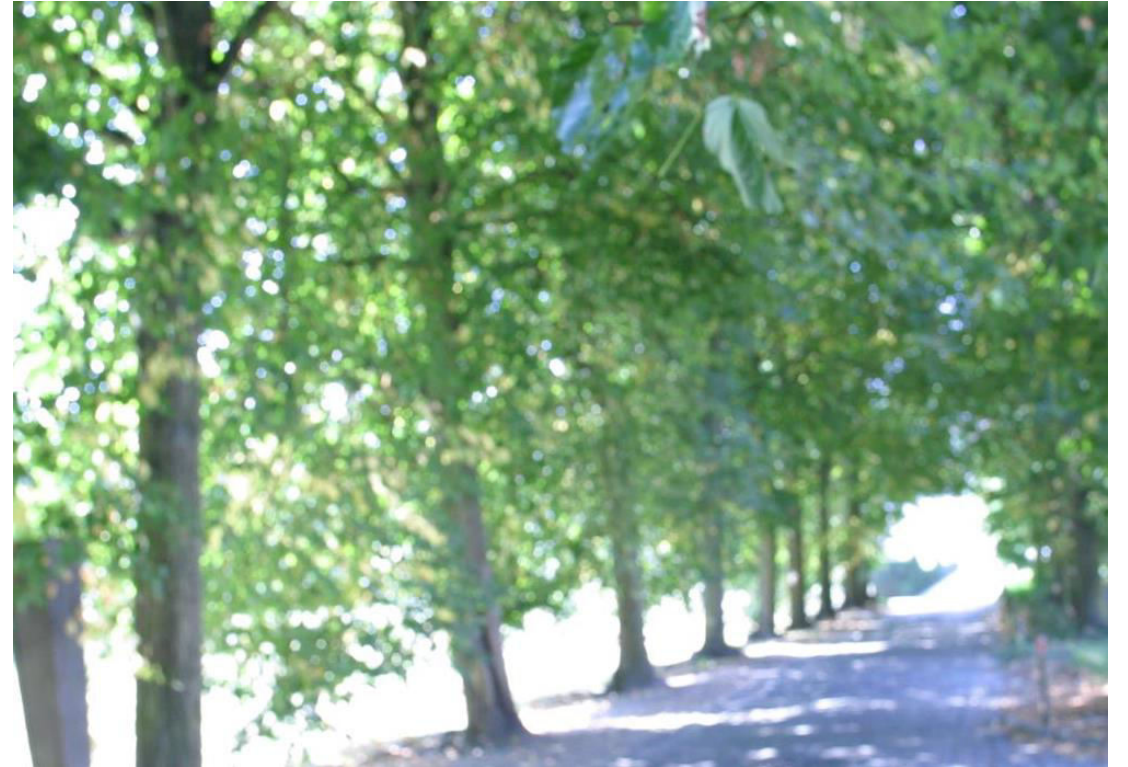
Geometry: zoom and rotation



Photometry: Light and Color Changes



Photometry: Blurring



Intra-class changes



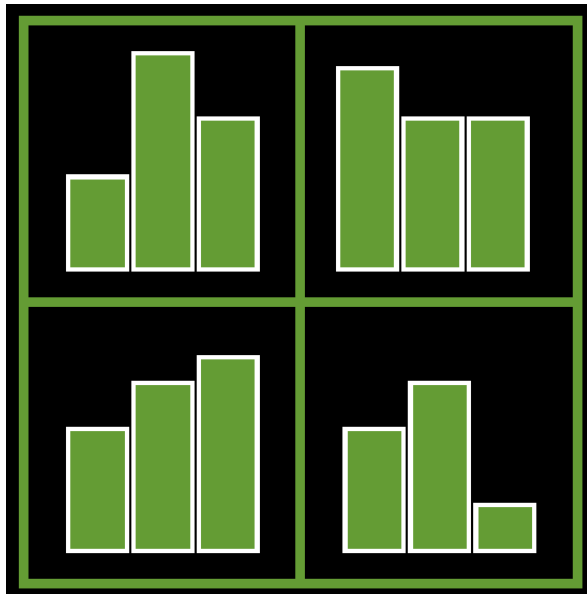
Detector and Descriptor

- Output of a **detector** are
 - Location
 - And possibly scale, orientation, affine, and other geometrics parameters



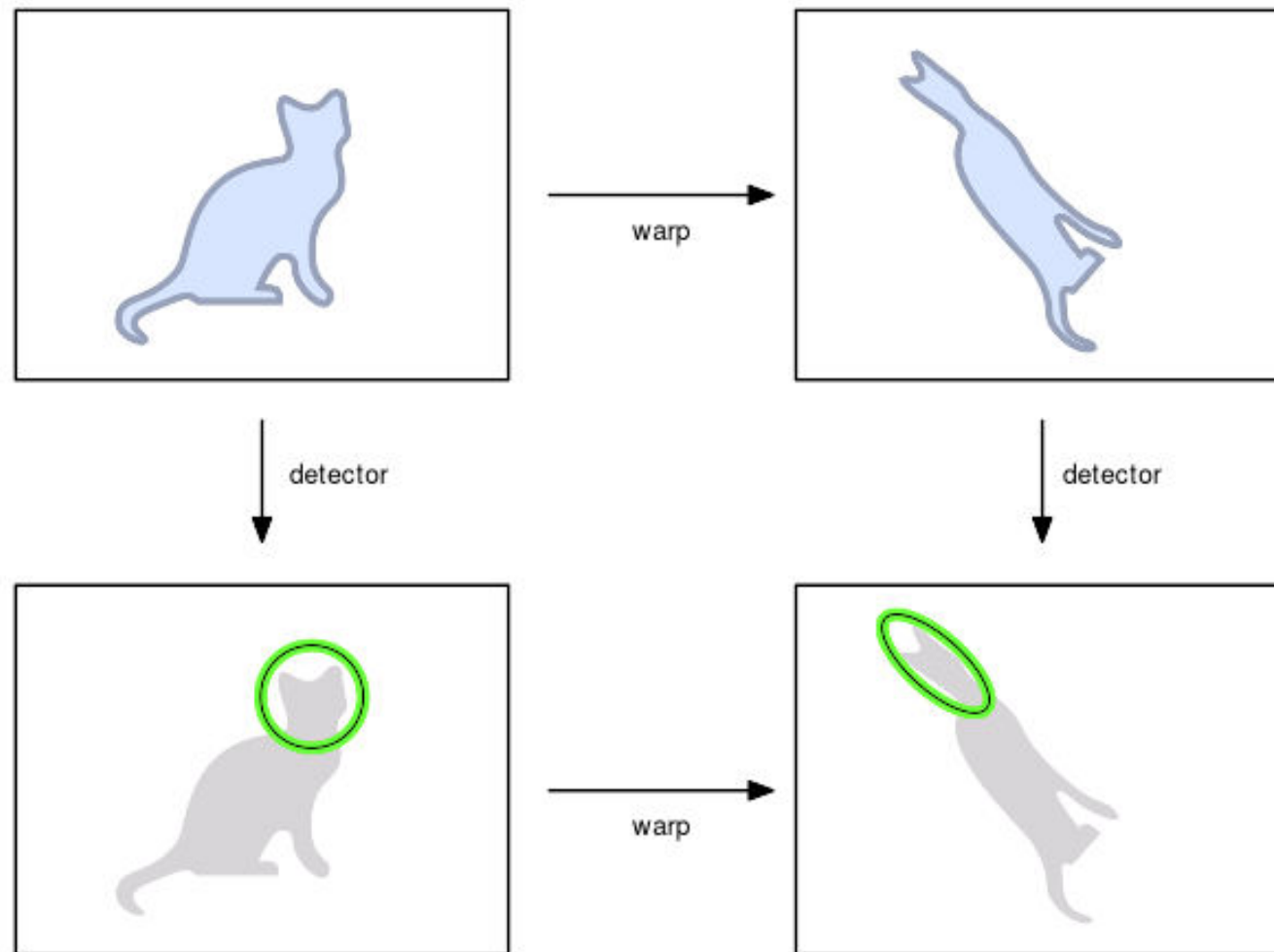
Detector and Descriptor

- Output of a **descriptor** is
 - A vector describing the neighborhood
 - For example a histogram!



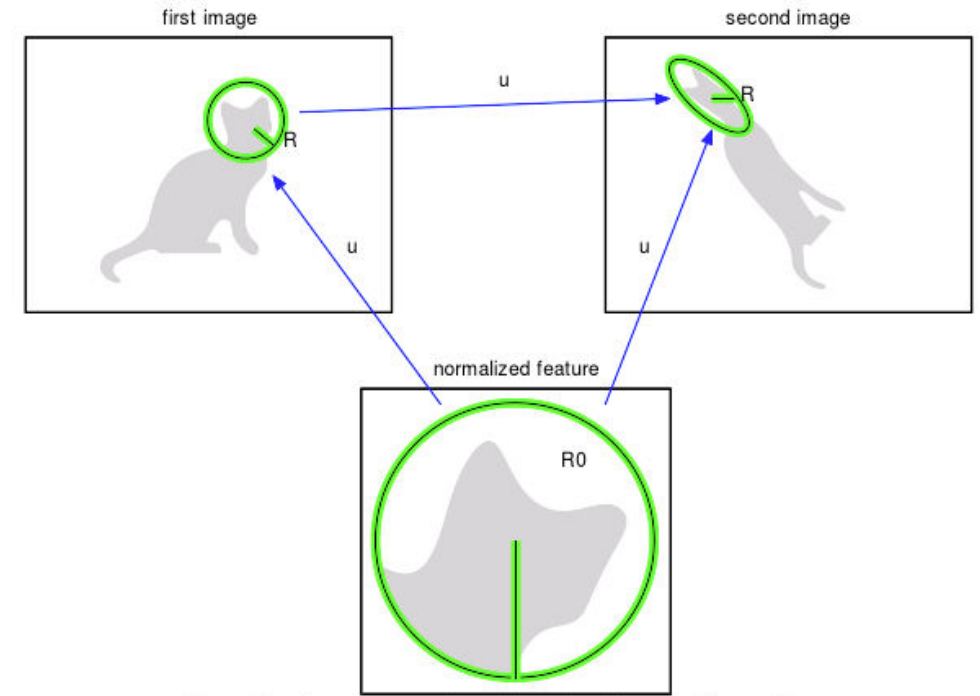
Geometric deformations: equivariance

- A feature has to be **equivariant** to deformations



Geometric deformations: invariance

A feature is **invariant** to deformations if its descriptor remains the same detected .



If the feature is equivariant, then invariance can be achieved with **normalization**.



Video 4.5

Kostas Daniilidis

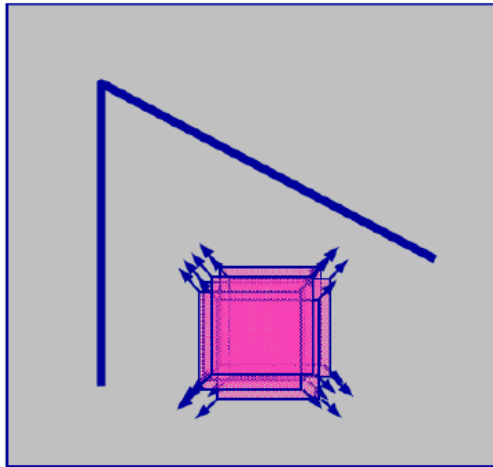
Harris Corners

A COMBINED CORNER AND EDGE DETECTOR

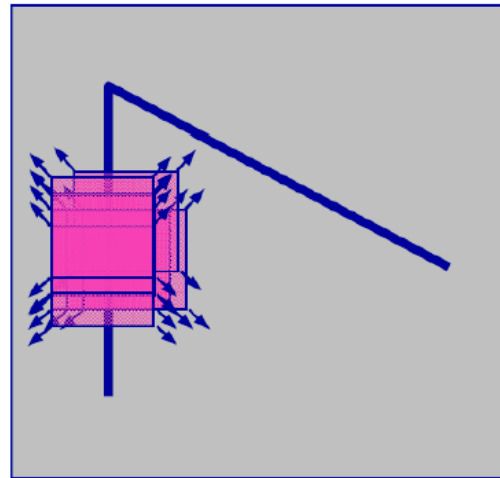
Chris Harris & Mike Stephens

Plessey Research Roke Manor, United Kingdom
© The Plessey Company plc. 1988

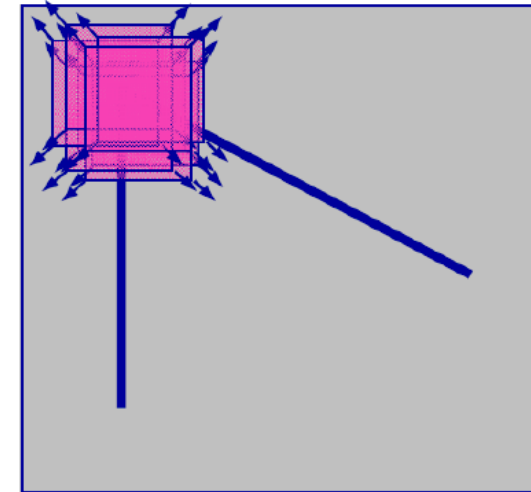
Harris corner detector: basic idea



flat region:
no change in any direction



edge:
no change along
the edge direction



corner:
change in all directions

Harris corner detector: derivation

Variation of intensity (expressed as weighted sum of squared distances) for a shift Δx around a fixed point x_0 , using first order Taylor expansion:

$$\begin{aligned} E(\Delta x) &= \sum_{x \in \mathcal{N}(x_0)} w(x) [I(x + \Delta x) - I(x)]^2 \\ &\approx \sum_{x \in \mathcal{N}(x_0)} w(x) [(I(x) + \nabla I(x)^T \Delta x) - I(x)]^2 \\ &= \sum_{x \in \mathcal{N}(x_0)} w(x) [\nabla I(x)^T \Delta x]^2 \\ &= \sum_{x \in \mathcal{N}(x_0)} w(x) \Delta x^T \nabla I(x) \nabla I(x)^T \Delta x \\ &= \Delta x^T A \Delta x \end{aligned}$$

where A is the autocorrelation matrix, w is a weighting function (e.g. Gaussian centered at x_0) and $\mathcal{N}(x_0)$ a neighborhood of x_0 .

Harris corner detector: autocorrelation matrix

The autocorrelation matrix A (evaluated at x_0) captures the variation of the gradients within the local patch. It can be rewritten as

$$\begin{aligned} A(x_0) &= \sum_{x \in \mathcal{N}(x_0)} w(x) \nabla I(x) \nabla I(x)^T \\ &= \sum_{x \in \mathcal{N}(x_0)} w(x) \begin{pmatrix} I_x(x) \\ I_y(x) \end{pmatrix} \begin{pmatrix} I_x(x) & I_y(x) \end{pmatrix} \\ &= \sum_{x \in \mathcal{N}(x_0)} w(x) \begin{pmatrix} I_x(x)^2 & I_x(x)I_y(x) \\ I_x(x)I_y(x) & I_y(x)^2 \end{pmatrix} \end{aligned}$$

where $I_x = \partial I / \partial x$ and $I_y = \partial I / \partial y$.

Harris corner detector: autocorrelation matrix

By replacing the weighted summations with discrete convolutions with the weighting kernel w , the autocorrelation matrix can be written as a convolution:

$$A = w * \begin{pmatrix} I_x^2 & I_x I_y \\ I_x I_y & I_y^2 \end{pmatrix}$$

where $*$ denotes convolution. Observe that A is positive semidefinite since

$$\Delta x^T A \Delta x = E(\Delta x) \geq 0$$

for all $\Delta x \in \mathbb{R}^2$ since E is a sum of square distances.

But why do we care if A is positive semidefinite after all? (*Hint*: think of eigenvalues!)

Harris corner detector: autocorrelation matrix

Since $A \succeq 0$ it follows that it can be decomposed as following:

$$A = Q\Lambda Q^T$$

where $Q = [q_1 \mid q_2]$ is the matrix with columns the eigenvectors of A and $\Lambda = \text{diag}(\lambda_1, \lambda_2)$ where λ_1, λ_2 are the two *nonnegative* eigenvalues of A .

$$\begin{aligned} E(\Delta x) &= \Delta x^T A \Delta x \\ &= \Delta x^T Q \Lambda Q^T \Delta x \\ &= \Delta y^T \Lambda \Delta y \\ &= \frac{\Delta y_1^2}{(1/\sqrt{\lambda_1})^2} + \frac{\Delta y_2^2}{(1/\sqrt{\lambda_2})^2} \end{aligned}$$

where $\Delta y = Q^T \Delta x$. Note that $\Delta y_1 = q_1^T \Delta x$ and $\Delta y_2 = q_2^T \Delta x$.

Harris corner detector: autocorrelation matrix

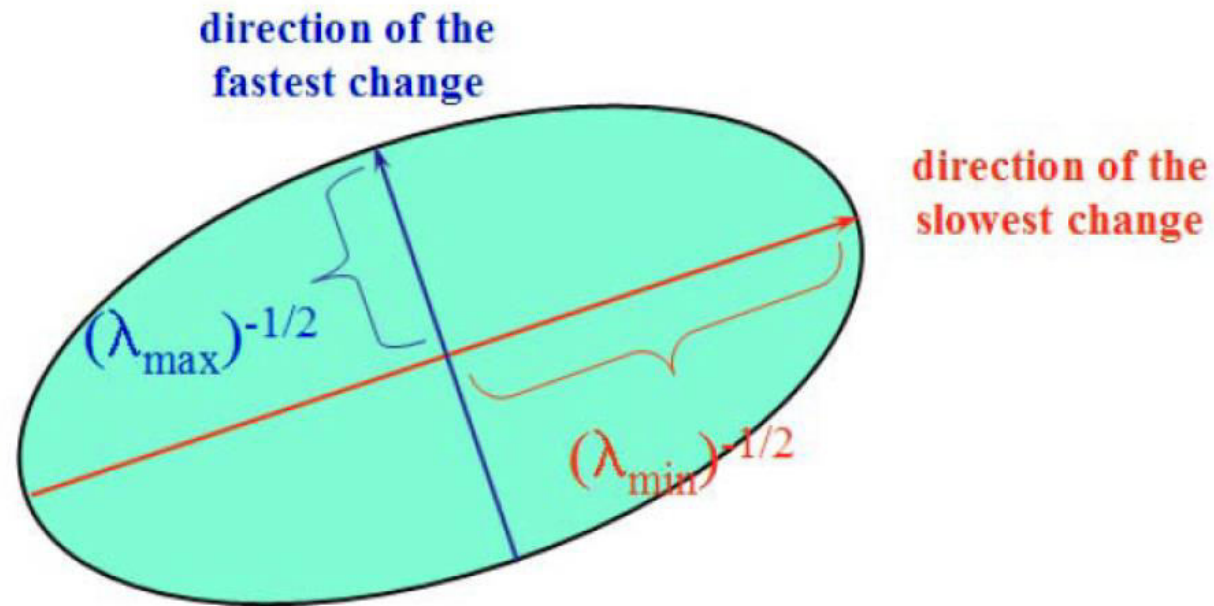
Note that always Q can be a rotation matrix in the spectral decomposition of A . Why? (Hint: the negated version of an eigenvector is an eigenvector too.) Let

$$Q = R_\theta = \begin{pmatrix} \cos \theta & -\sin \theta \\ \sin \theta & \cos \theta \end{pmatrix}$$

Since $\Delta y = Q^T \Delta x$ it follows that the directions Δy_1 and Δy_2 result from Δx_1 and Δx_2 by a rotation of θ .

Harris corner detector

What does the above formula of $E(\Delta x)$ in terms of Δy_1 and Δy_2 reminds you of? Yes, an ellipse!



Uncertainty ellipse corresponding to an eigenvalue analysis of the autocorrelation matrix A .

Harris corner detector

Observations:

- ① If λ_1, λ_2 are very small, then a large shift does not produce a significant variation of intensity and thus, the patch corresponds to a flat region.
- ② If $\lambda_1 \gg \lambda_2$, then a shift along the direction Δy_1 produces a significant variation of intensity and thus, the patch corresponds to an edge.
- ③ If λ_1, λ_2 are large, then a shift along any direction produces a significant variation of intensity and thus, the patch corresponds to a corner.

Harris corner detector

How can we quantify the above observations?

$$\begin{aligned} R &= \det(A) - k \cdot \text{trace}(A)^2 \\ &= \lambda_1 \lambda_2 - k \cdot (\lambda_1 + \lambda_2)^2 \end{aligned}$$

where $k = 0.06$ is an empirical constant.

- ❶ If λ_1, λ_2 are very small, then R is very small eliminating flat regions.
- ❷ If $\lambda_1 \gg \lambda_2$, then R is very small eliminating edge responses.
- ❸ If λ_1, λ_2 are large, R is large as desired.

Is the Harris “autocorrelation matrix” an equivariant feature?

$$\sum_{x \in \mathcal{N}(x_0)} w(x) \begin{pmatrix} I_x(x)^2 & I_x(x)I_y(x) \\ I_x(x)I_y(x) & I_y(x)^2 \end{pmatrix}$$

Rotation: If the image is rotated will the matrix rotate as well?

Yes! And the eigendecomposition will yield rotation.

Scaling: If the image is rotated will the matrix scale as well?

Yes but the detection threshold will have to be adapted.

Only the descriptor matrix is equivariant.

Harris corner detector: implementation sketch

- 1 Read input image and turn it to grayscale if necessary.
- 2 Smooth input image with a gaussian filter.
- 3 Convolve input image with filter $h = \begin{bmatrix} 1/2 & 0 & -1/2 \end{bmatrix}$ to obtain the first order derivatives:

$$I_x = I * h \quad I_y = I * h^T$$

- 4 Compute images A, B, C at pixel (u, v) as defined below:

$$A(u, v) = I_x(u, v)^2 \quad B(u, v) = I_y(u, v)^2 \quad C(u, v) = I_x(u, v) \cdot I_y(u, v)$$

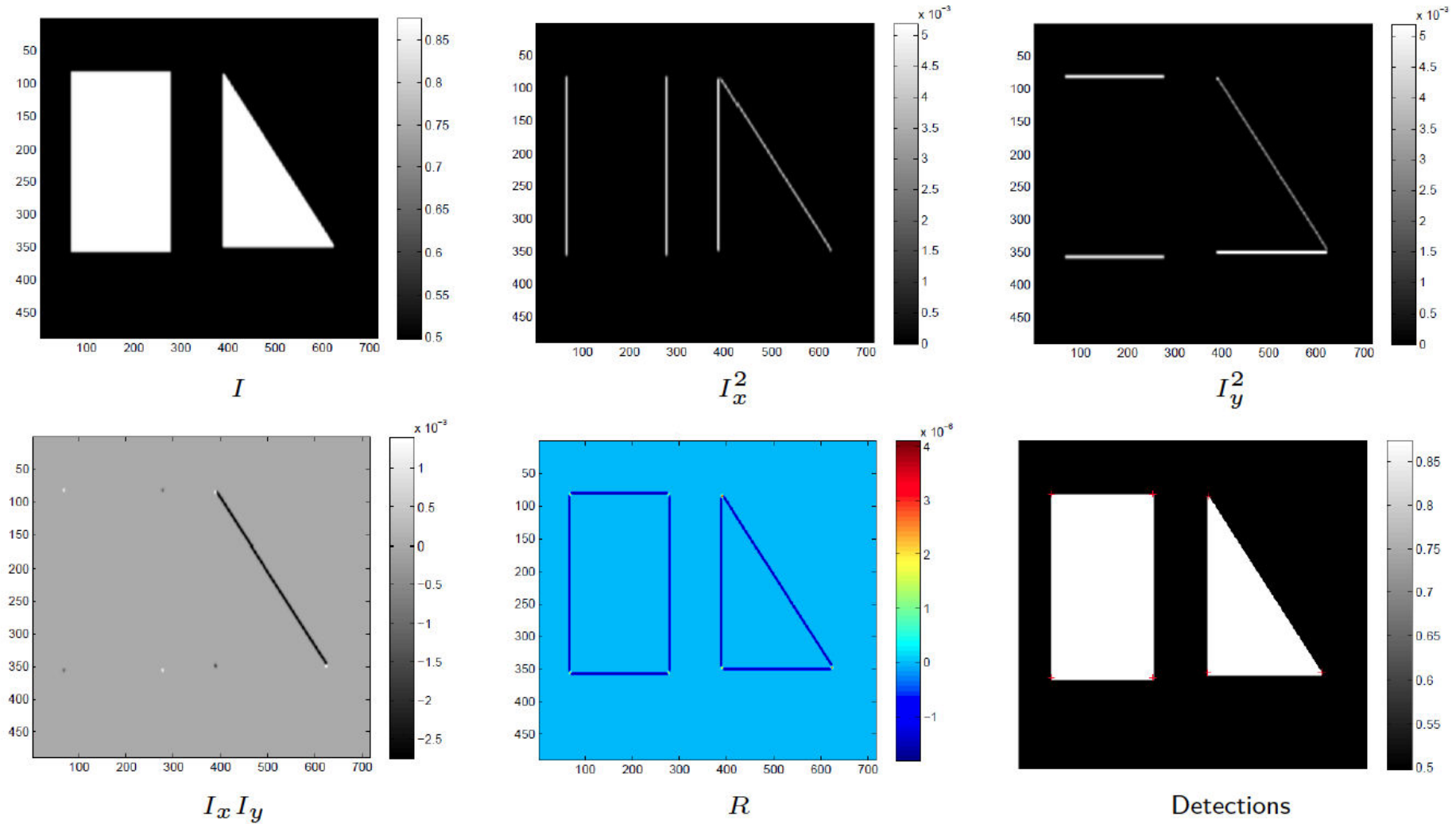
- 5 Filter A, B, C with a gaussian filter.
- 6 Compute corner response at each pixel (u, v)

$$R(u, v) = (A(u, v) \cdot B(u, v) - C(u, v)^2) - k(A(u, v) + B(u, v))^2$$

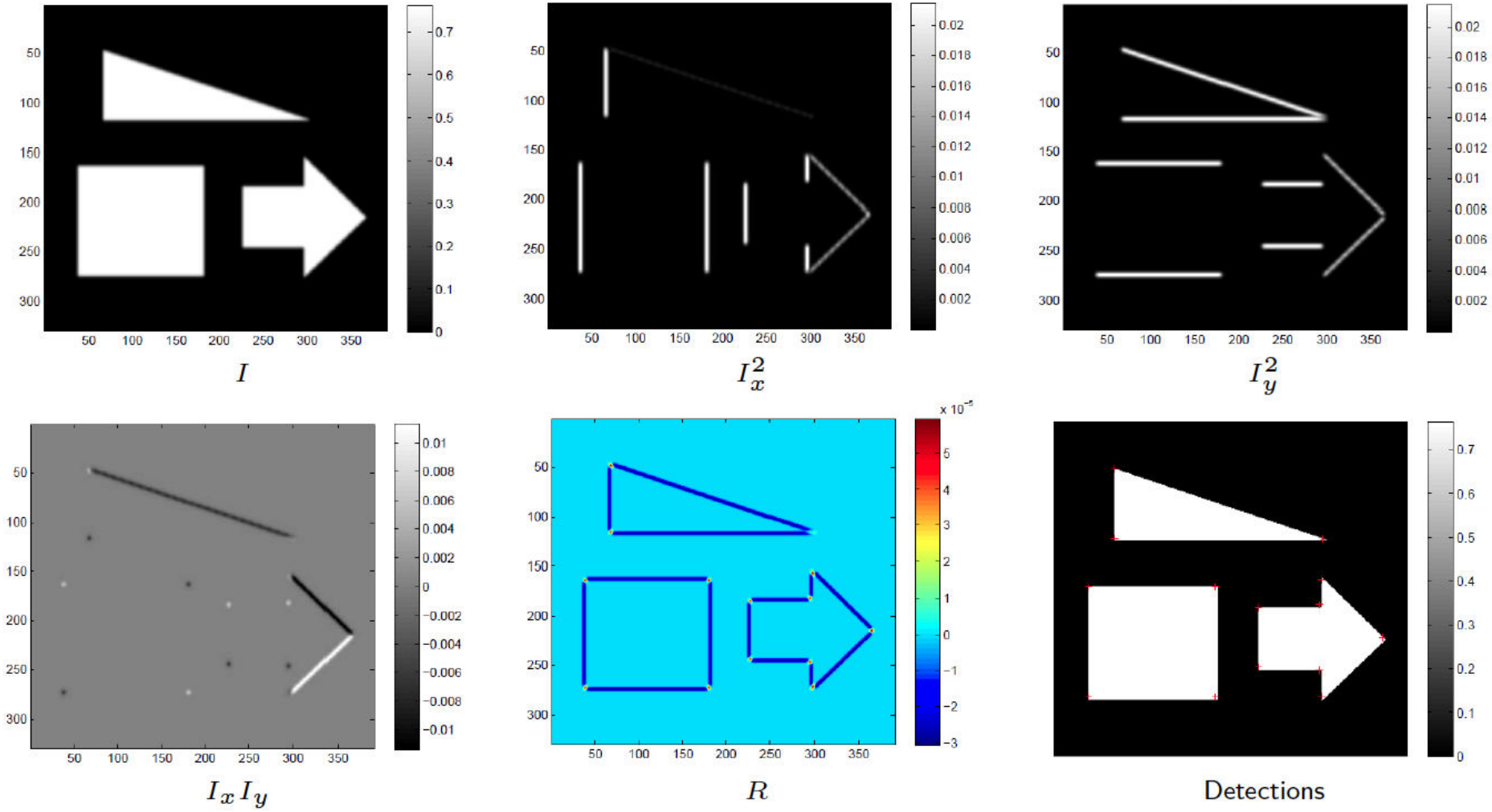
with $k = 0.06$.

- 7 Detect local maxima of R .
- 8 Keep local maxima of R whose values are above a threshold.

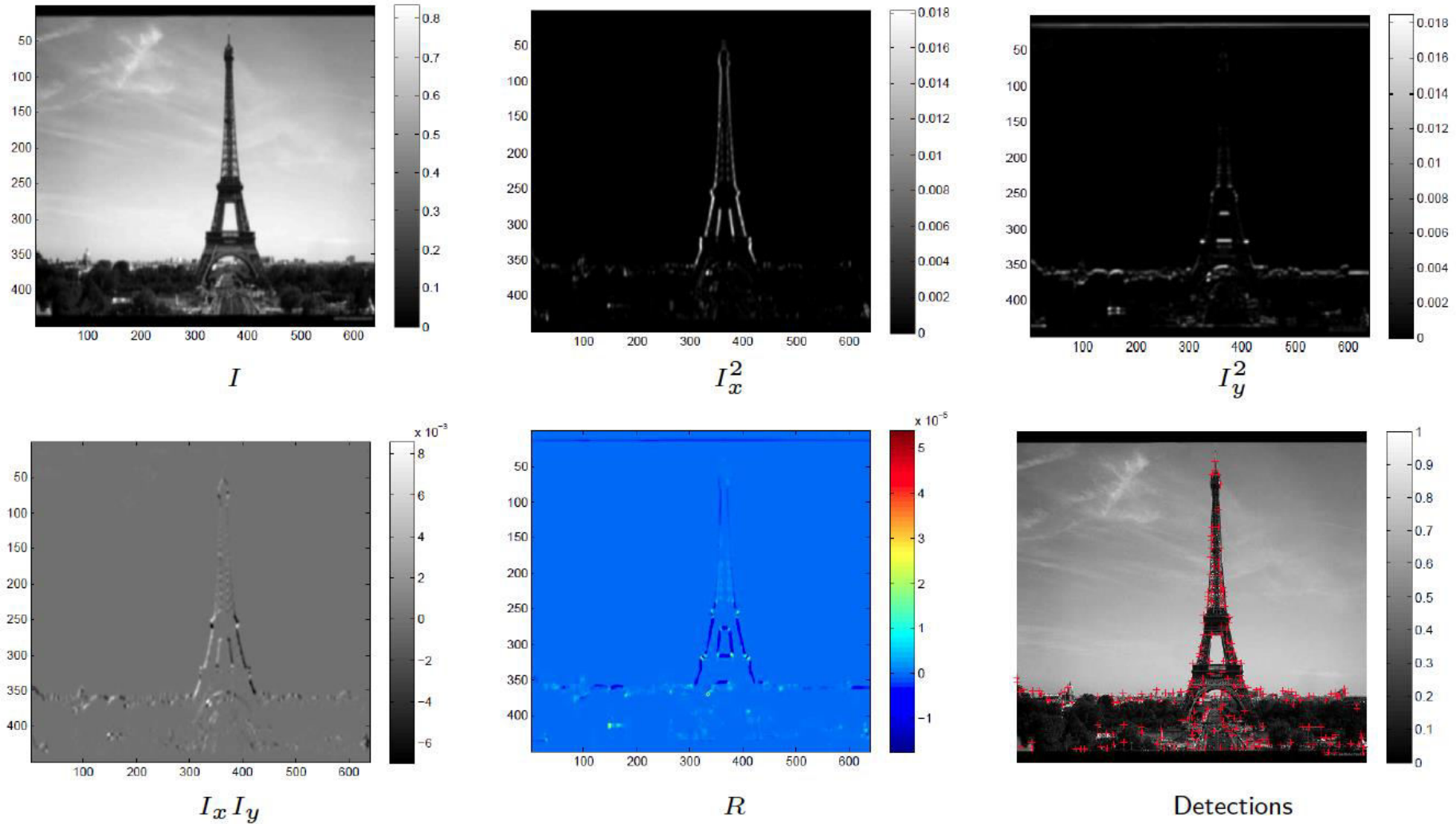
Harris corner detector: visualization



Harris corner detector: visualization



Harris corner detector: visualization





Video 4.6

Kostas Daniilidis

MSER: Maximally Stable Extremal Regions, Matas et al. 2001

Robust wide-baseline stereo from maximally stable extremal regions

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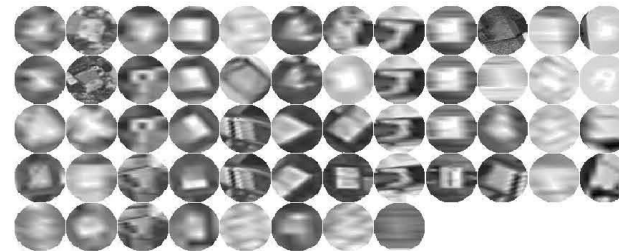
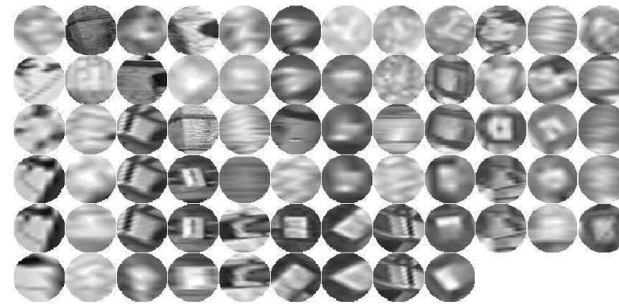
Received 12 March 2003; received in revised form 11 February 2004; accepted 12 February 2004

MSER: Maximally Stable Extremal Regions, Matas et al. 2001

“uniform blobs”



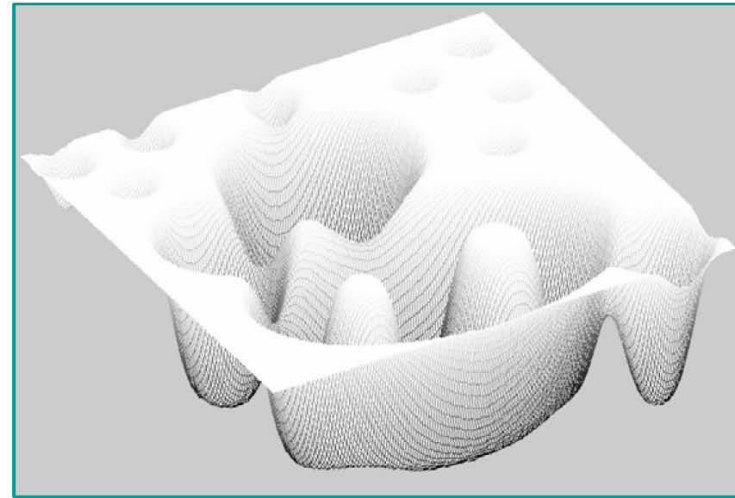
Regions unchanged over many thresholds



MSER Construction (1)



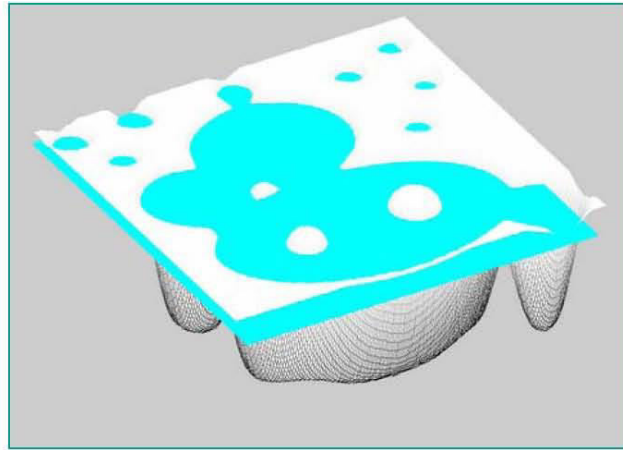
intensity image



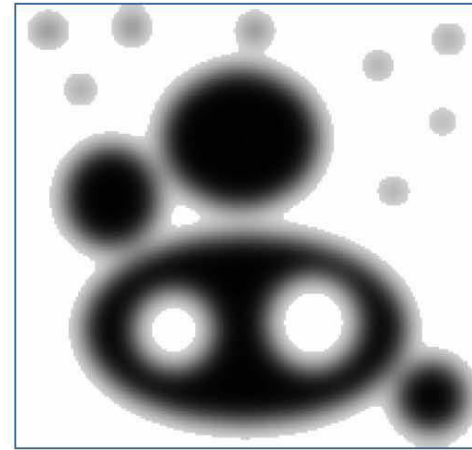
shown as a surface function

Watershed segmentation algorithms come from the concept of filling a basin with water to different levels.

MSER Construction (2)



Threshold simulation



Extremal Regions (represented by their original lumiance values)



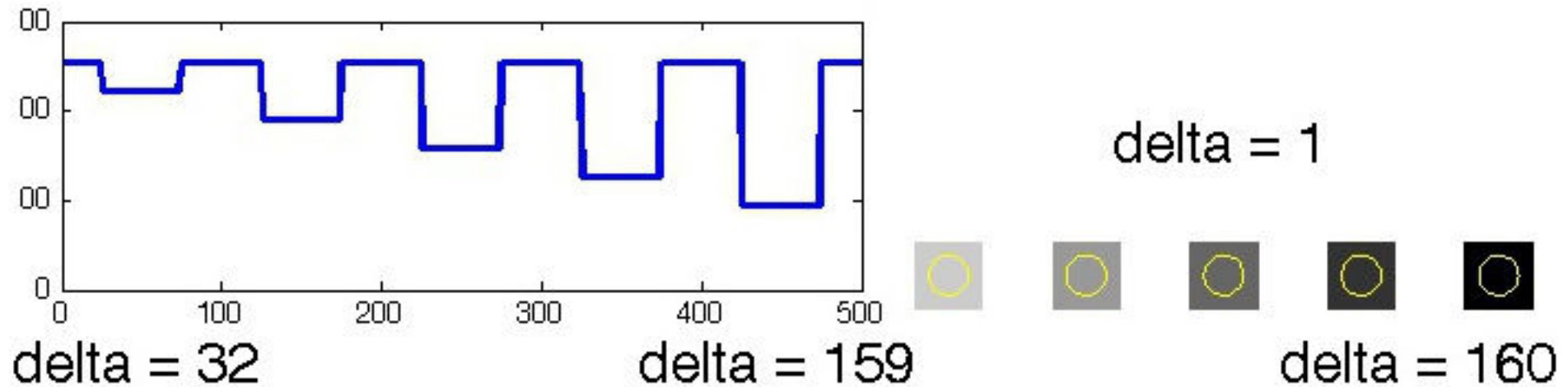
For each region, and for each threshold value, the region area is saved.



MSER Computation (3)

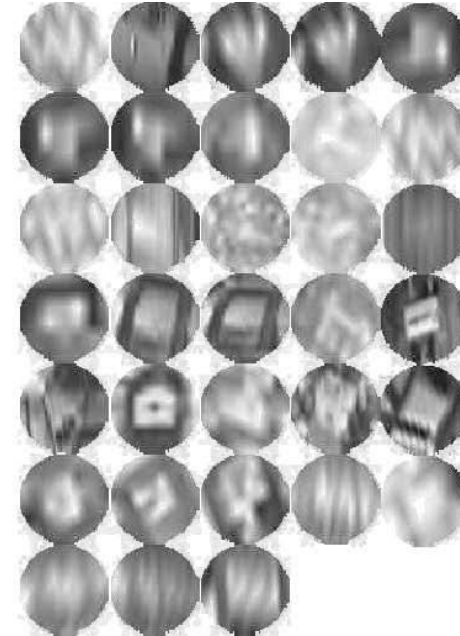
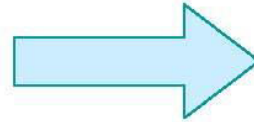
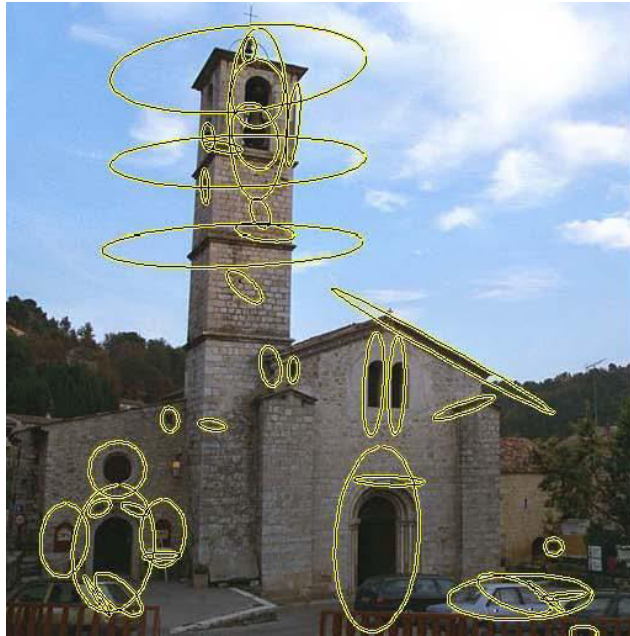
- For each threshold, compute the connected binary regions.
- Compute a function, **area $A(i)$** , at each threshold value i .
- Analyze this function for each potential region to determine those that **persist with similar function value over multiple thresholds**.

A single threshold

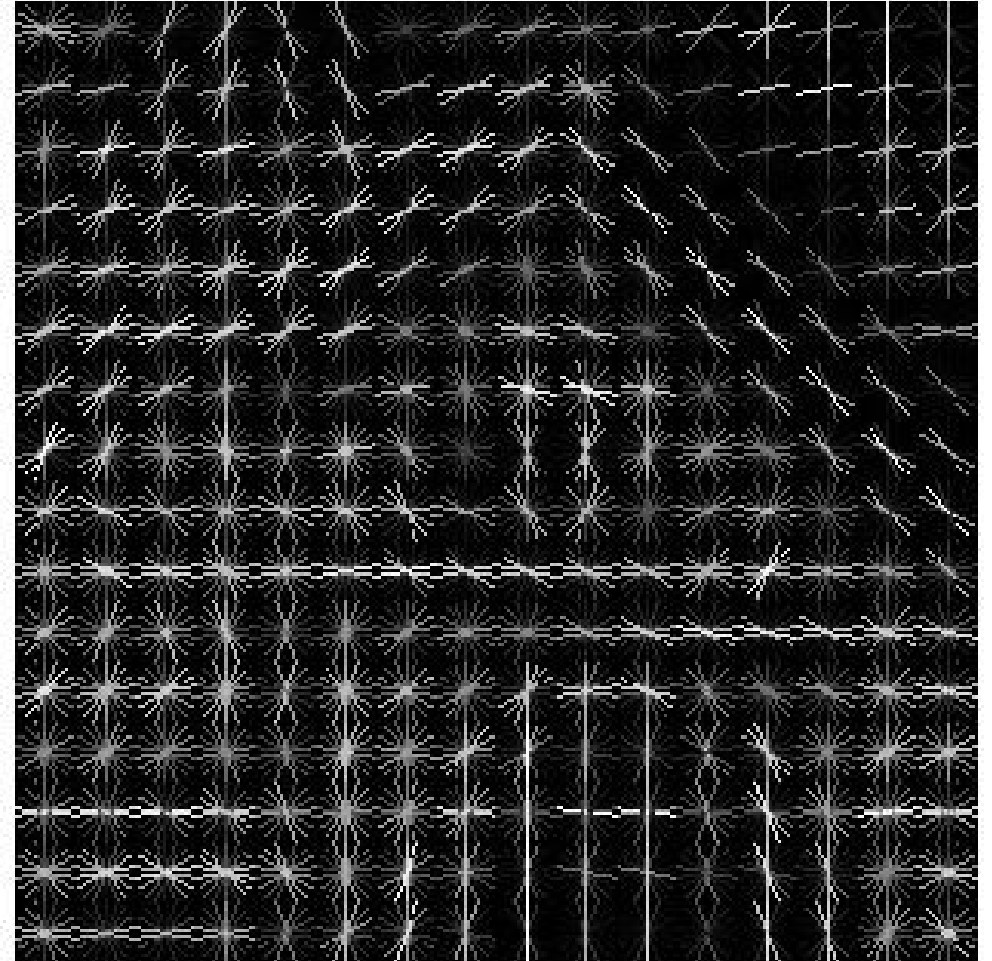


Effect of Δ . We start with a synthetic image which has an intensity profile as shown. The bumps have heights equal to 32, 64, 96, 128 and 160. As we increase Δ , fewer and fewer regions are detected until finally at $\Delta=160$ there is no region R which is stable at $R(+\Delta)$.

Affine transformation from ellipses to circular regions plus intensity normalization



Histogram of gradients (HOG) descriptor (Dalal and Triggs)



Histogram of gradients (HOG) descriptor

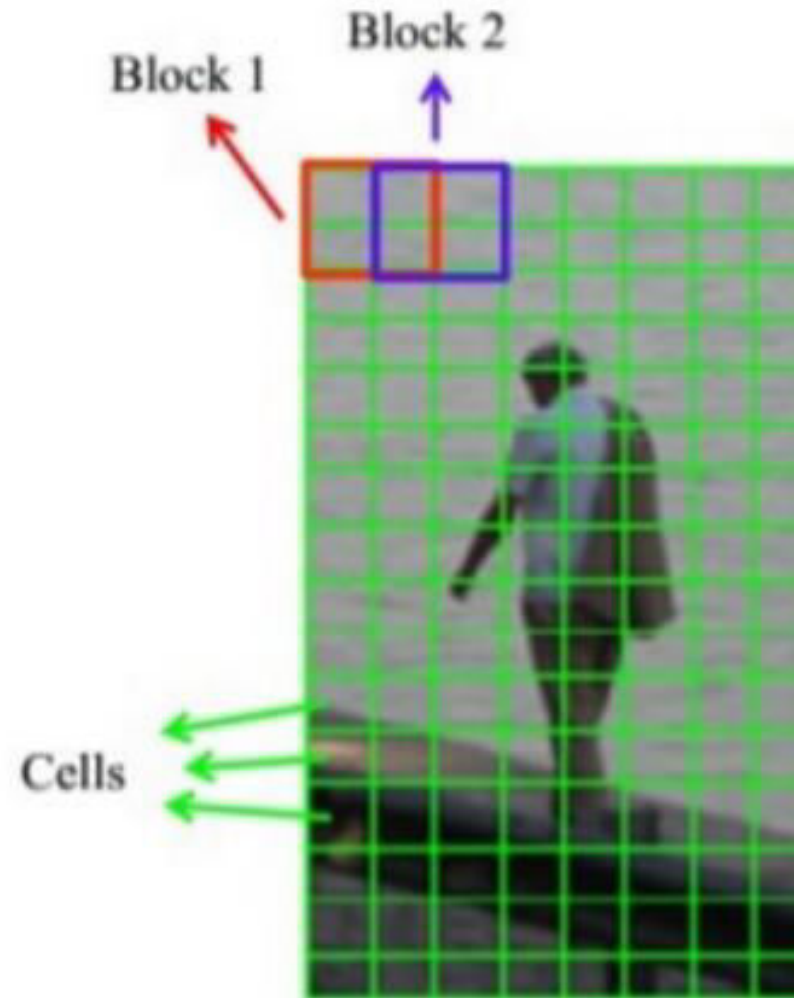
Histograms of Oriented Gradients for Human Detection

Navneet Dalal and Bill Triggs

INRIA Rhône-Alps, 655 avenue de l'Europe, Montbonnot 38334, France
{Navneet.Dalal,Bill.Triggs}@inrialpes.fr, <http://lear.inrialpes.fr>

Image is split in overlapping blocks of cells

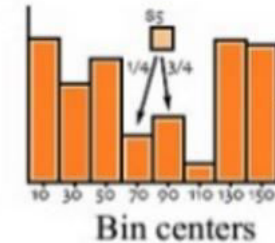
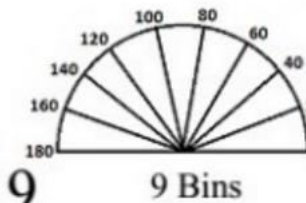
- Each **block** is 16x16
- 50% overlap
- Each block has 2x2 **cells**
- Each cell is 8x8



Histogram quantization

Tri-linear Interpolation

- Each block consists of 2x2 cells with size 8x8
- Quantize the gradient orientation into 9 bins (0-180)



- The vote is the gradient magnitude
- Interpolate votes linearly between neighboring bin centers.
 - Example: if $\theta=85$ degrees.
 - Distance to the bin center Bin 70 and Bin 90 are 15 and 5 degrees, respectively.
 - Hence, ratios are $5/20=1/4$, $15/20=3/4$.
- The vote can also be weighted with Gaussian to downweight the pixels near the edges of the block.

The **VLFeat** [open source](#) library implements popular computer vision algorithms specializing in image understanding and local features extraction and matching. Algorithms include Fisher Vector, VLAD, SIFT, MSER, k-means, hierarchical k-means, agglomerative information bottleneck, SLIC superpixels, quick shift superpixels, large scale SVM training, and many others. It is written in C for efficiency and compatibility, with interfaces in MATLAB for ease of use, and detailed documentation throughout. It supports Windows, Mac OS X, and Linux. The latest version of VLFeat is **0.9.20**.

[ACM OpenSource
Award](#)

Download

- [VLFeat 0.9.20](#) (Windows, Mac, Linux)
- [Source code and installation](#)
-  [git repository, bug tracking](#).

Documentation

- [MATLAB commands](#)
- [C API](#) with algorithm descriptions
- [Command line tools](#)

Tutorials

- Features: [Covariant detectors](#), [HOG](#), [SIFT](#), [MSER](#), [Quick shift](#), [SLIC](#)
- Clustering: [IKM](#), [HIKM](#), [AIB](#)
- Matching: [Randomized kd-trees](#)
- [All tutorials](#)

Example applications

- [Caltech-101 classification](#)
- [SIFT matching for auto-stitching](#)
- [All example applications](#)

Citing

```
@misc{vedaldi08vlfeat,  
  Author = {A. Vedaldi and B. Fulkerson},  
  Title = {{VLFeat}: An Open and Portable Library  
           of Computer Vision Algorithms},  
  Year = {2008},  
  Howpublished = {\url{http://www.vlfeat.org/}}
```

Acknowledgments

PASCAL2
Image Analysis, Speech and Machine Learning

UCLA Vision Lab Oxford VGG.



A Comparison of Affine Region Detectors

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Received August 20, 2004; Revised May 3, 2005; Accepted May 11, 2005

First online version published in January, 2006