

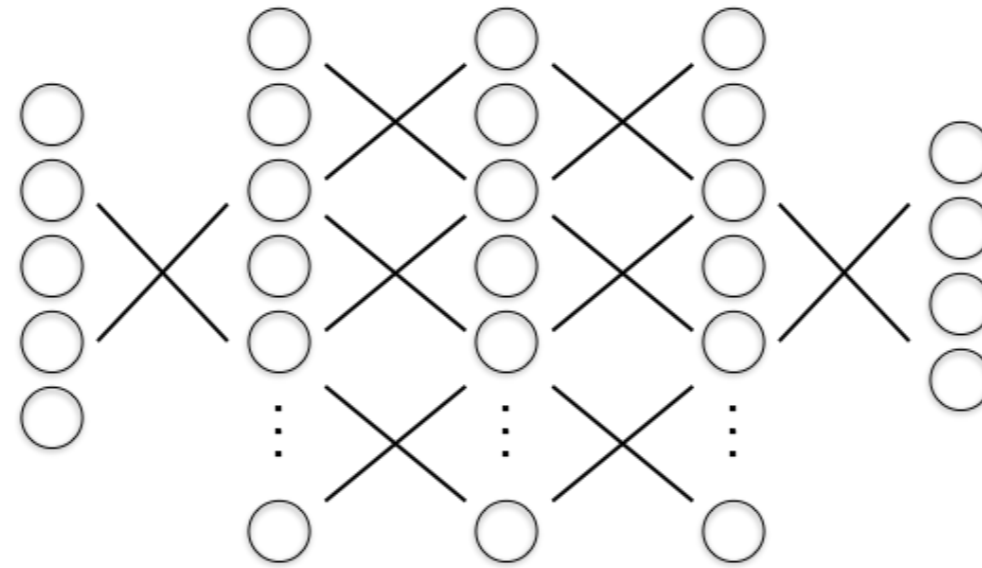
Feed-forward Neural Networks (Part 2: learning)



Outline (part 2)

- ▶ Learning feed-forward neural networks
- ▶ SGD and back-propagation

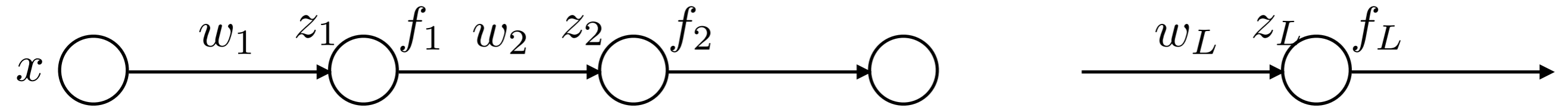
Learning neural networks





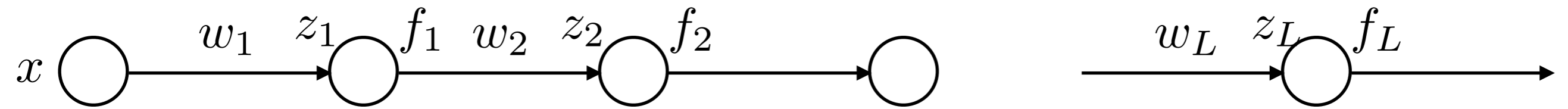
Simple example

- ▶ A long chain like neural network



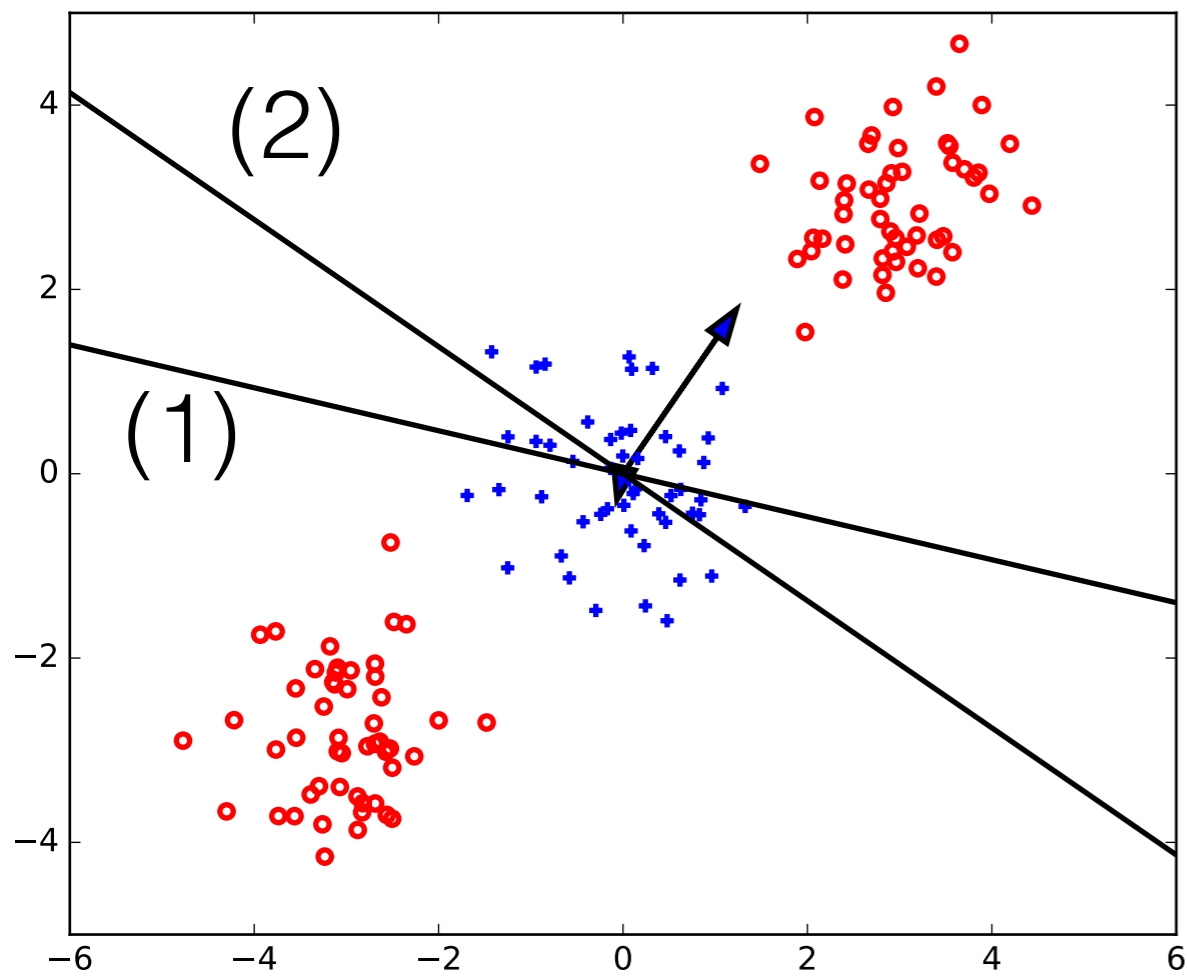


Back-propagation

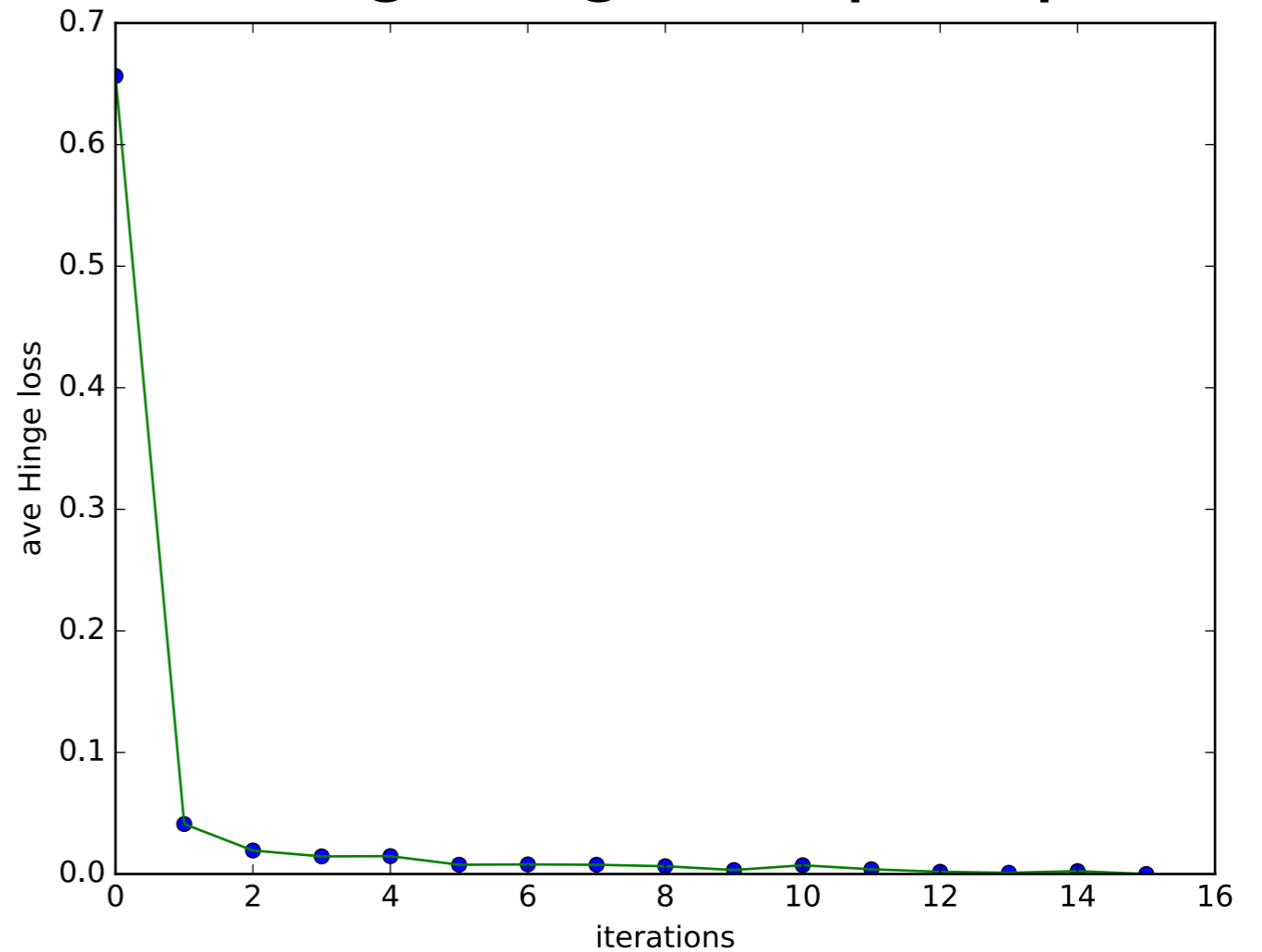


2 hidden units: training

Initial network (hidden units)



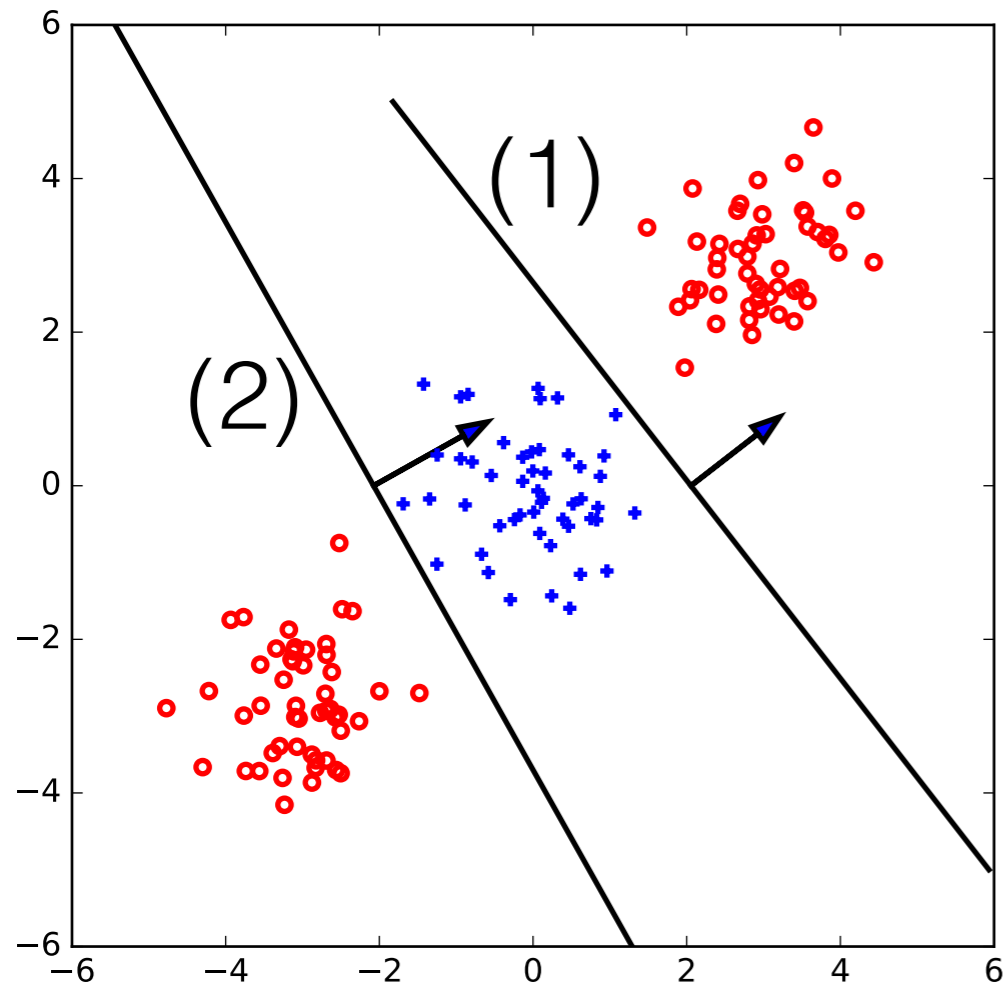
Average hinge loss per epoch



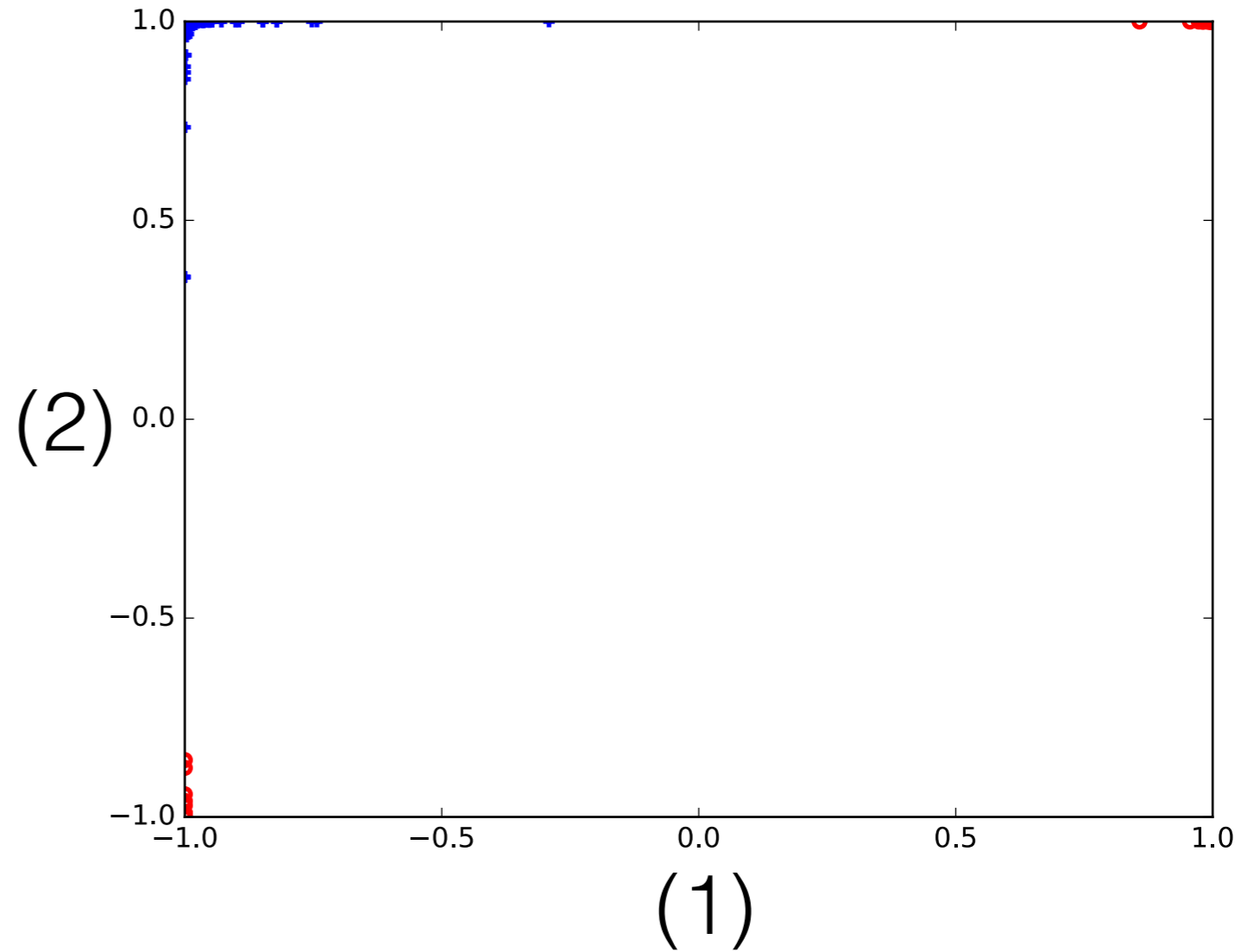


2 hidden units: training

- ▶ After ~ 10 passes through the data

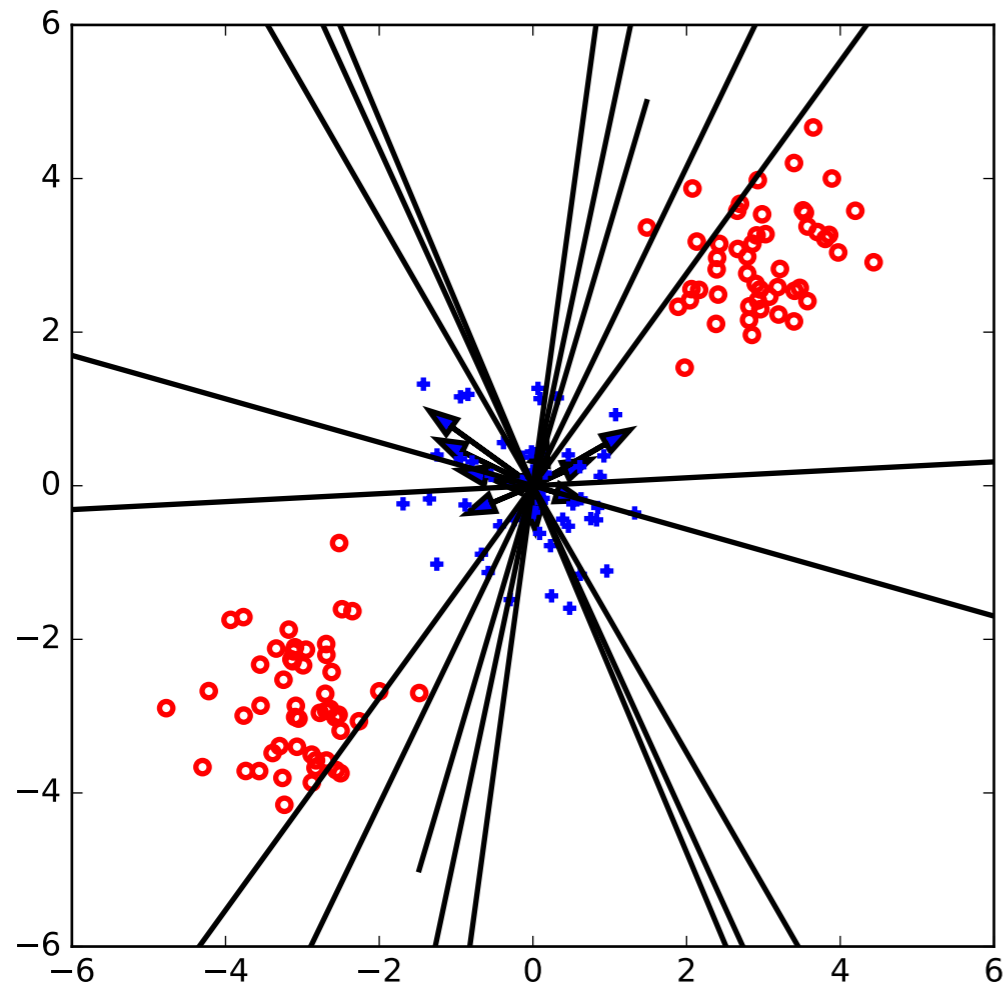


hidden unit activations



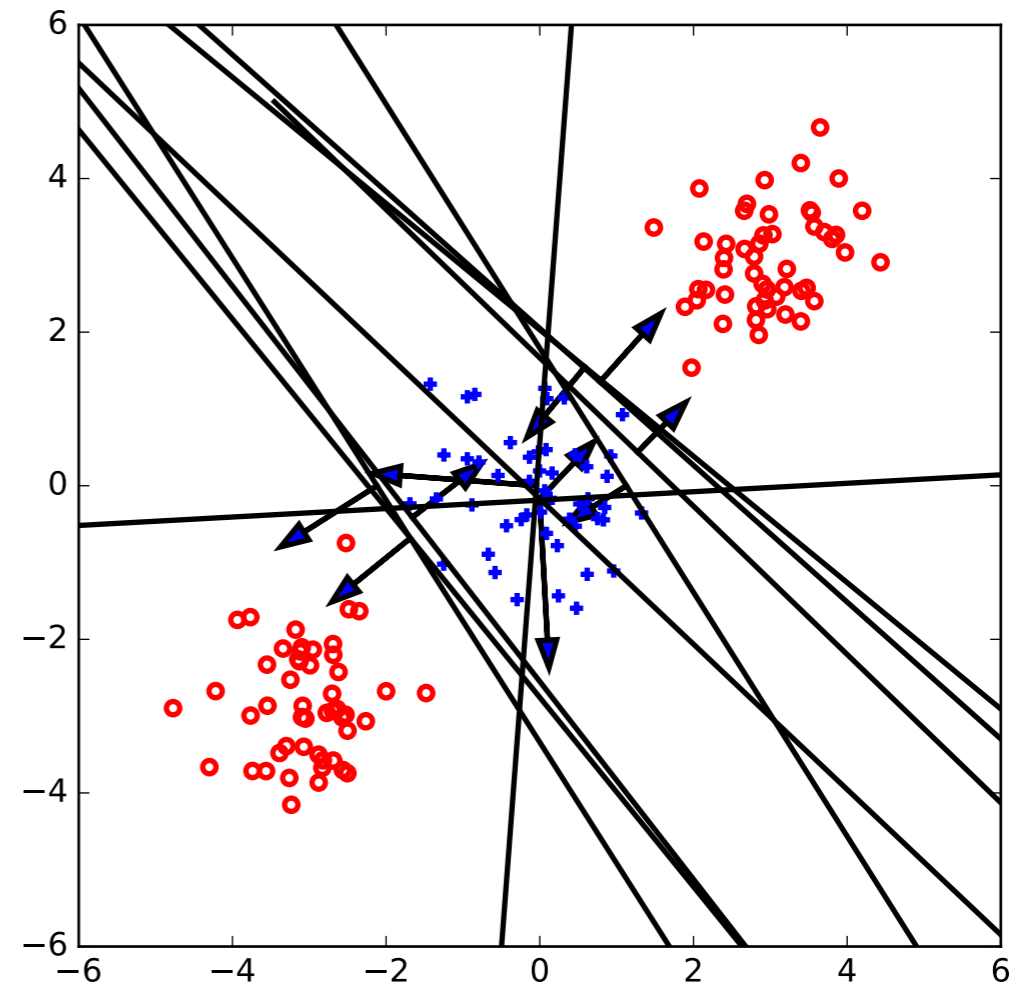
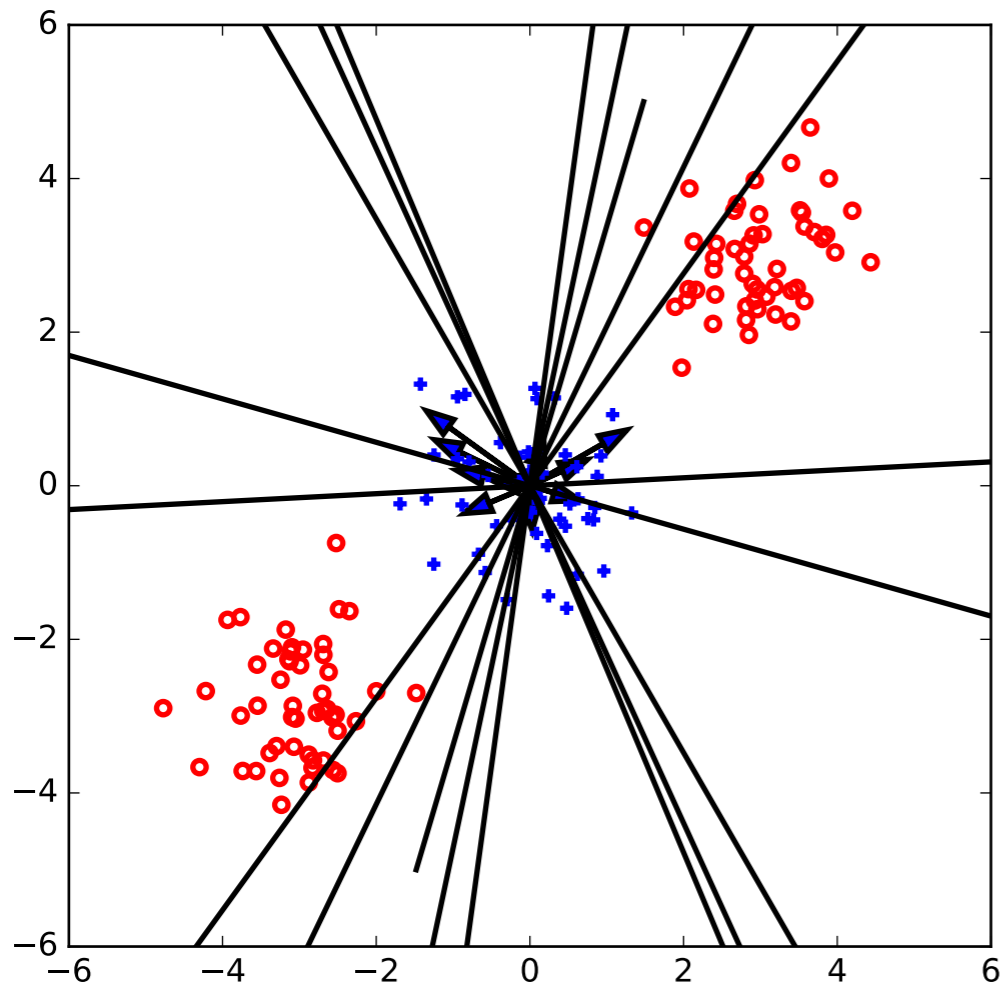
10 hidden units

- ▶ Randomly initialized weights (zero offset) for the hidden units



10 hidden units

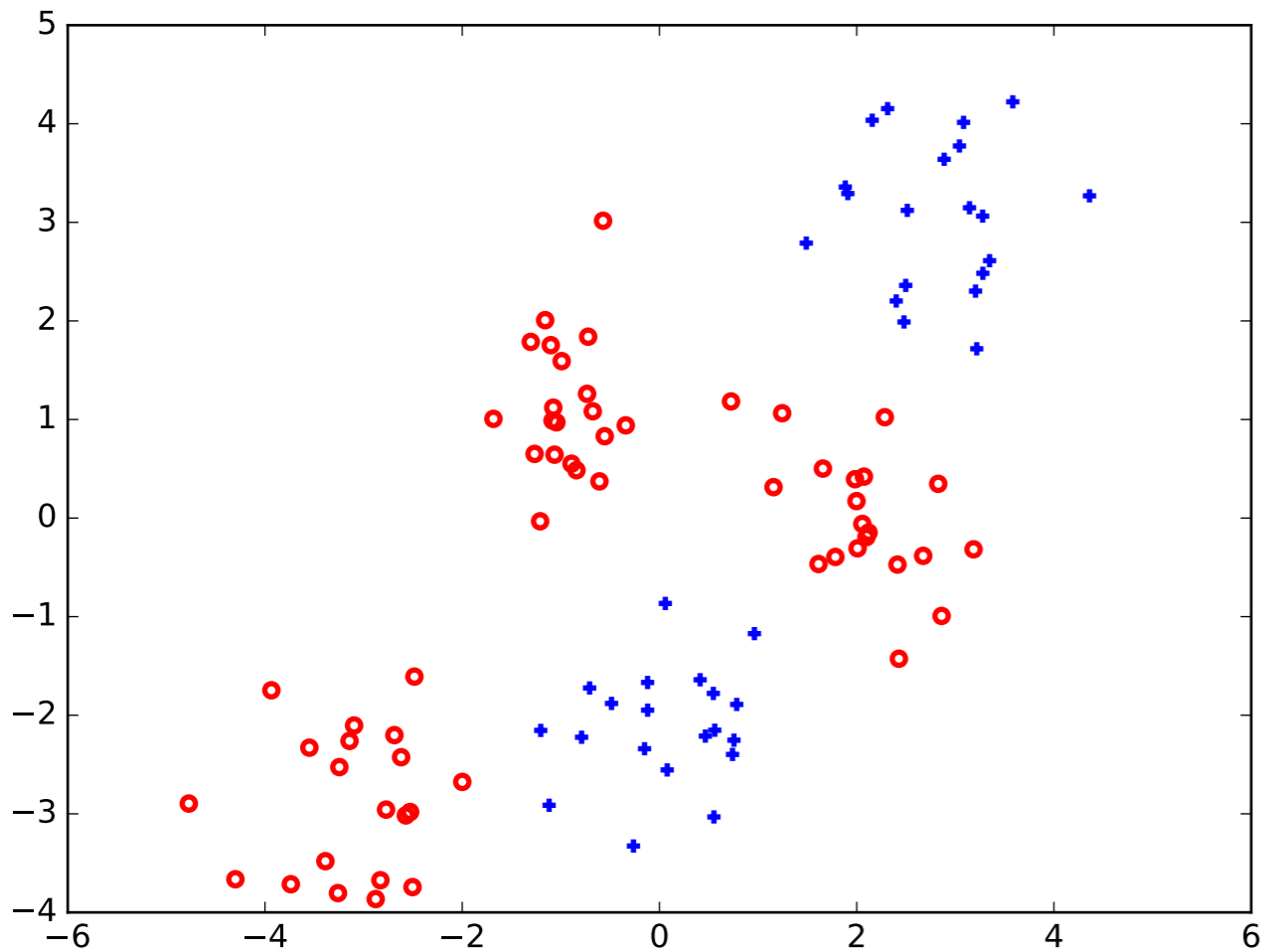
- ▶ After ~ 10 epochs the hidden units are arranged in a manner sufficient for the task (but not otherwise perfect)





Decisions (and a harder task)

- ▶ 2 hidden units can no longer solve this task

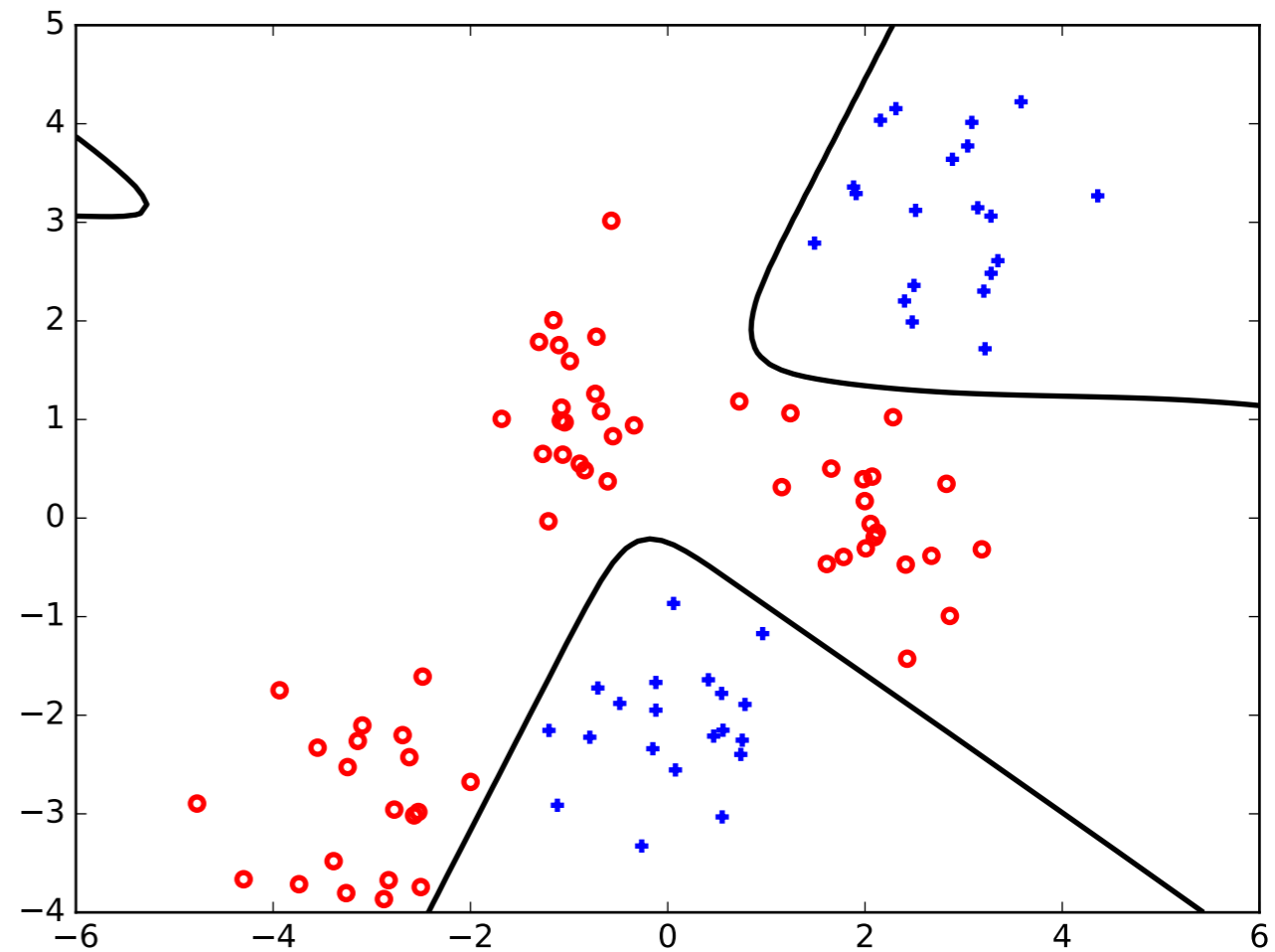
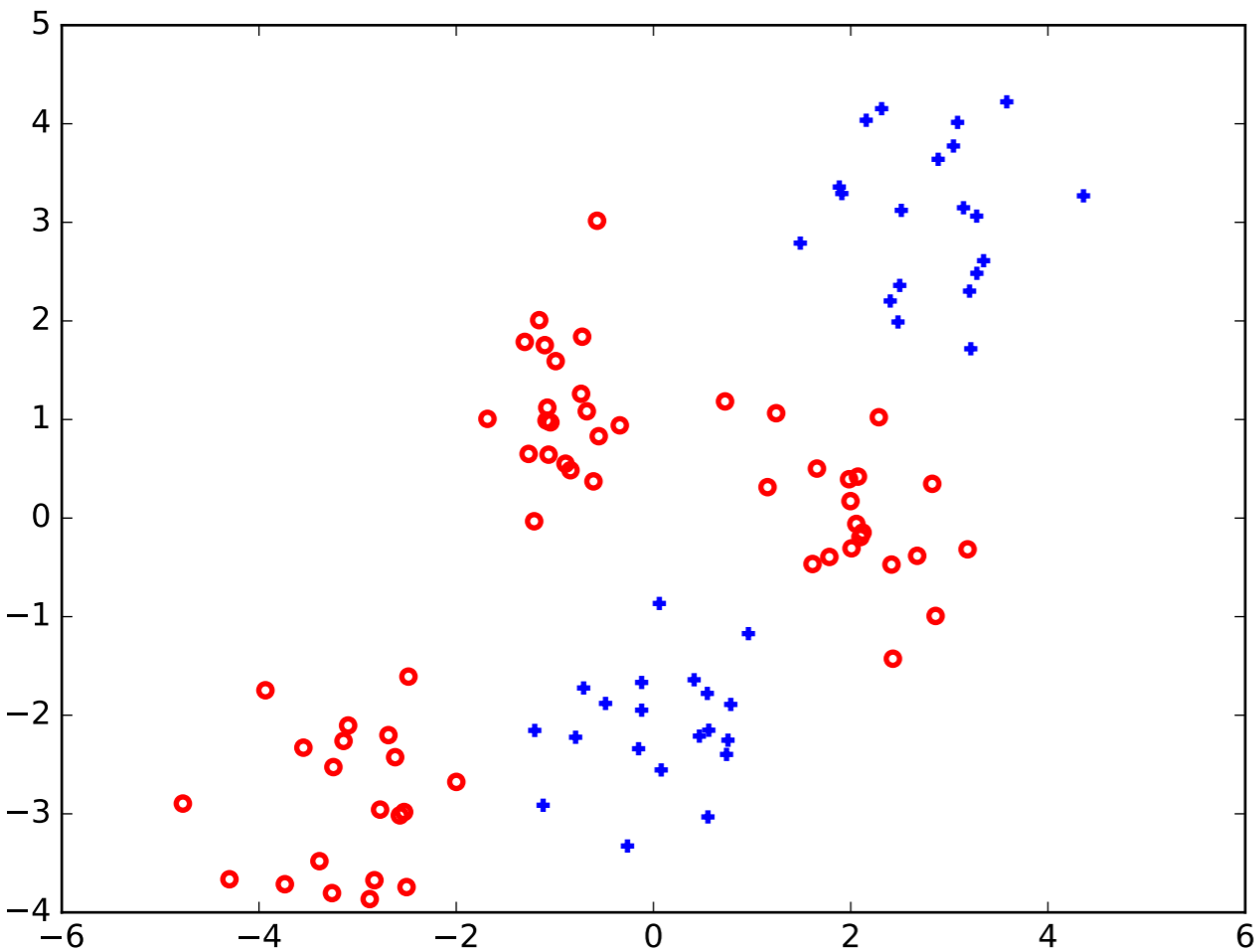




Decisions (and a harder task)

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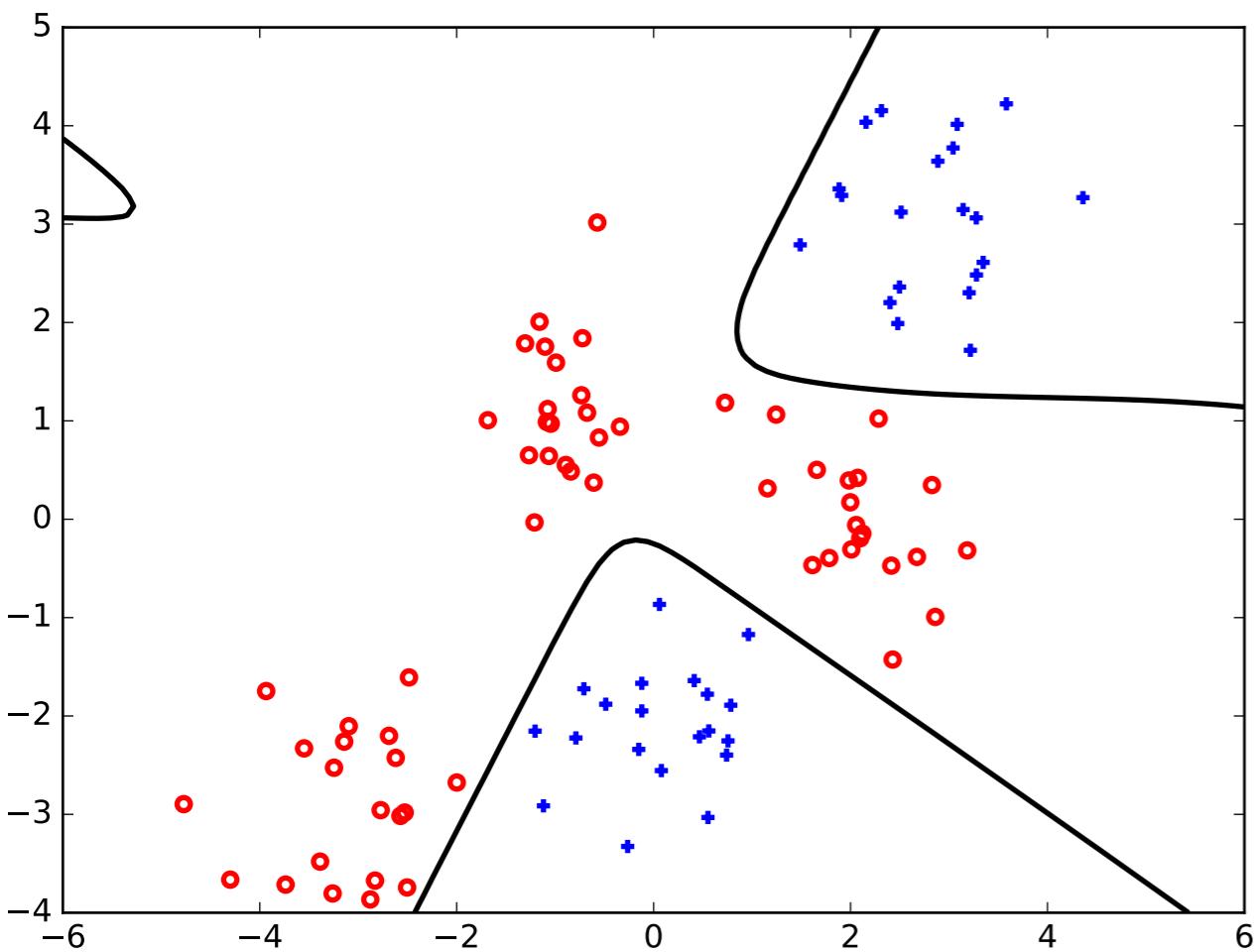
10 hidden units



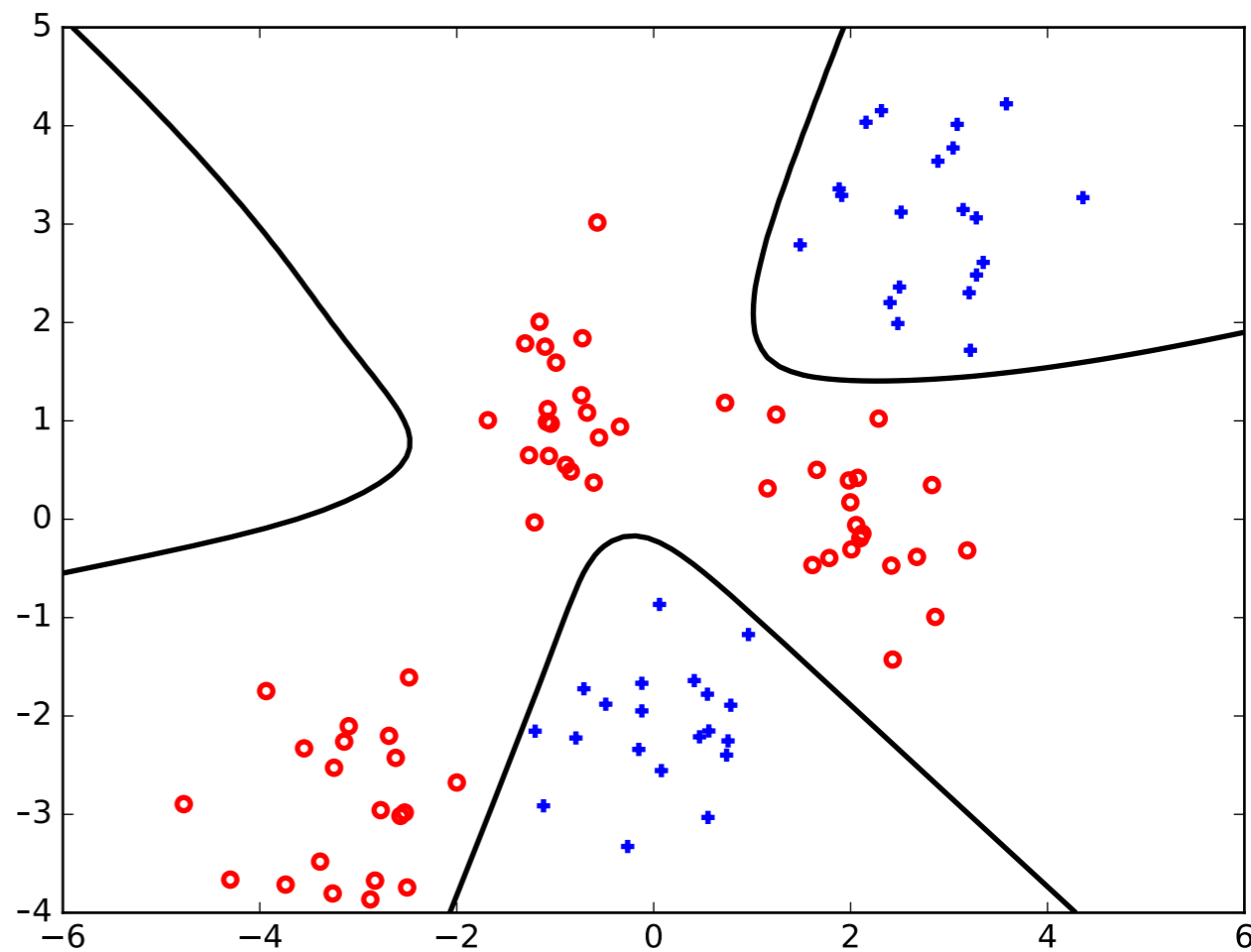


Decisions (and a harder task)

10 hidden units



100 hidden units

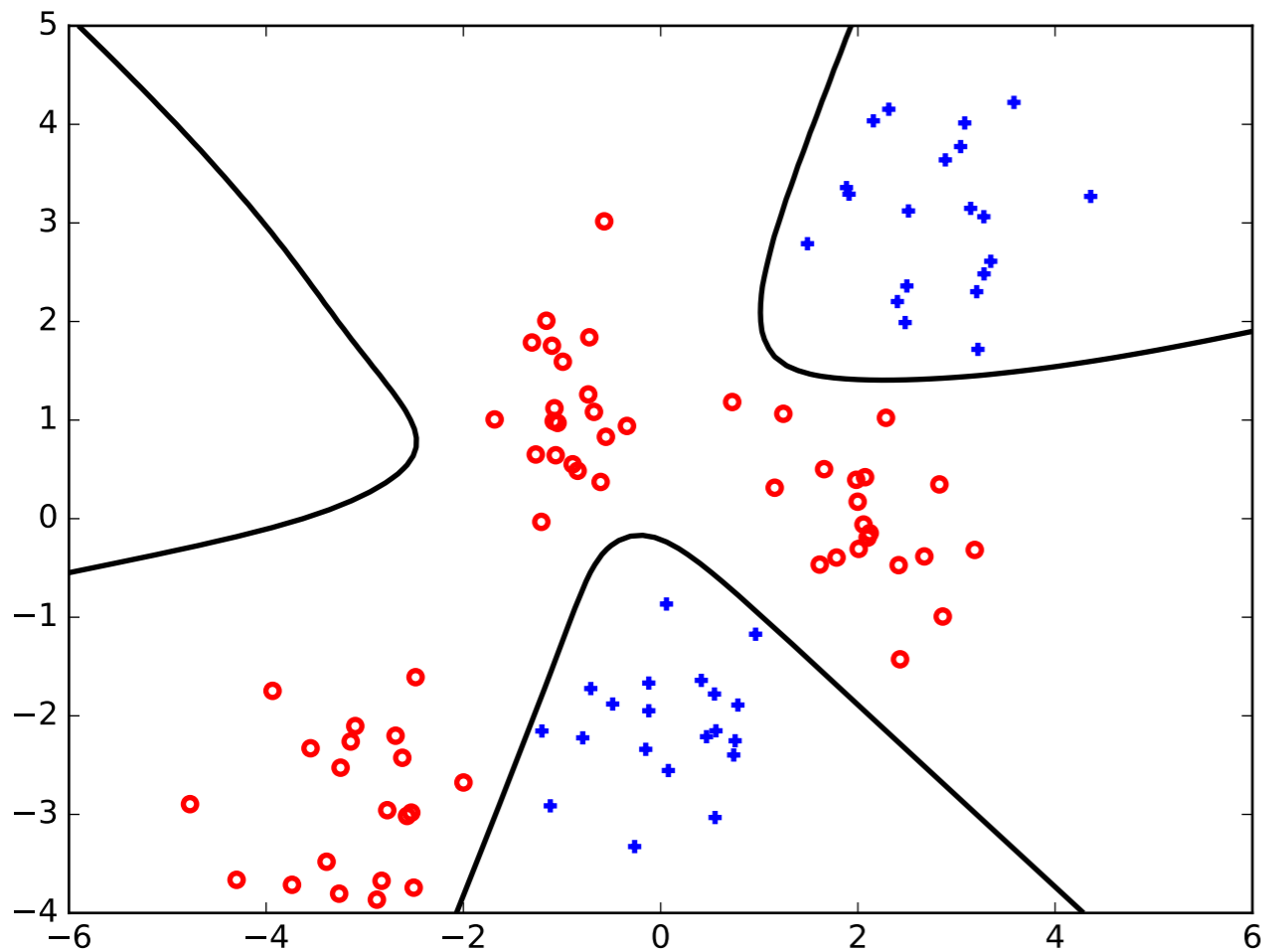




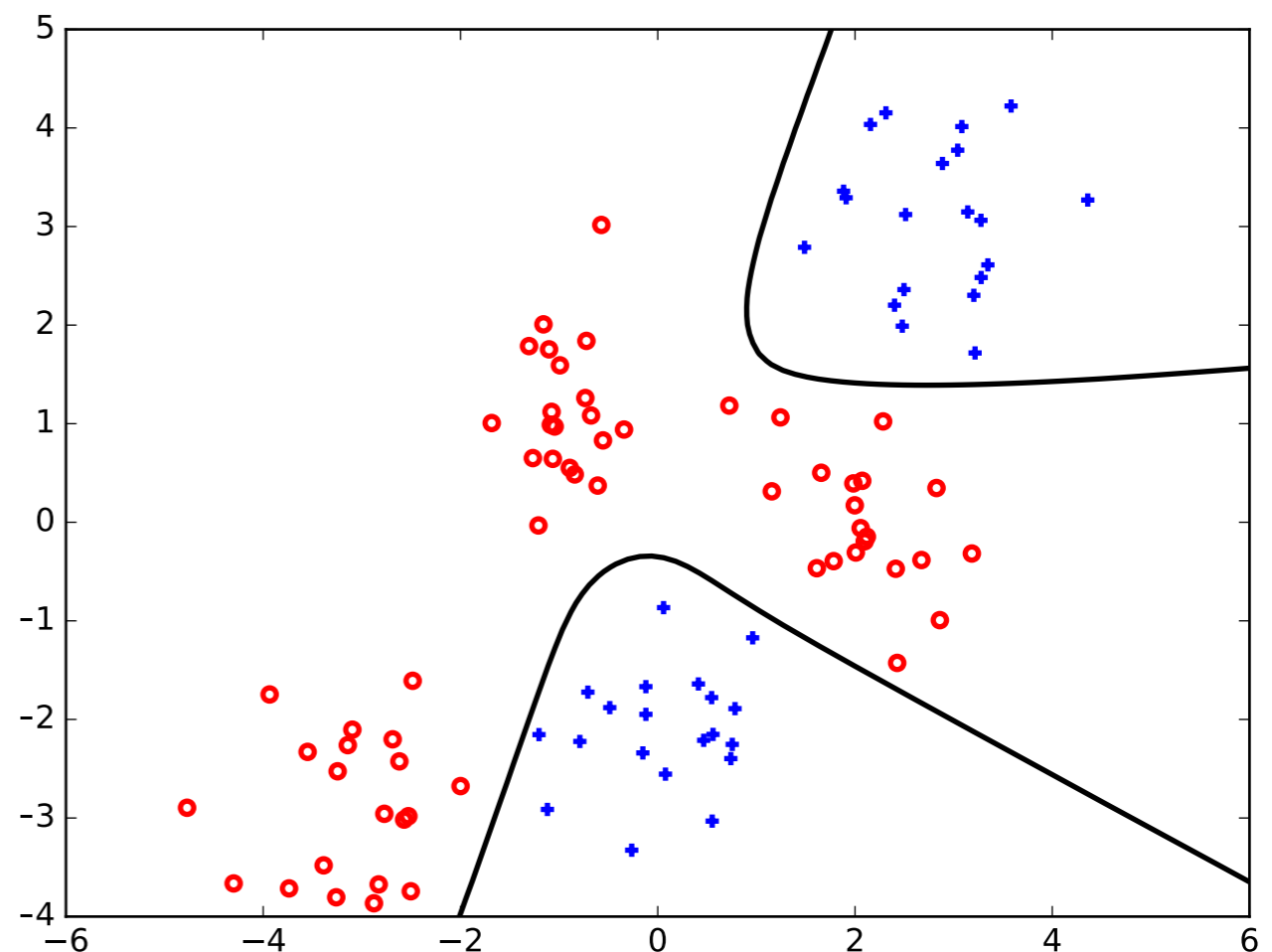
Decision boundaries

- ▶ Symmetries introduced in initialization can persist...

100 hidden units
(zero offset initialization)



100 hidden units
(random offset initialization)

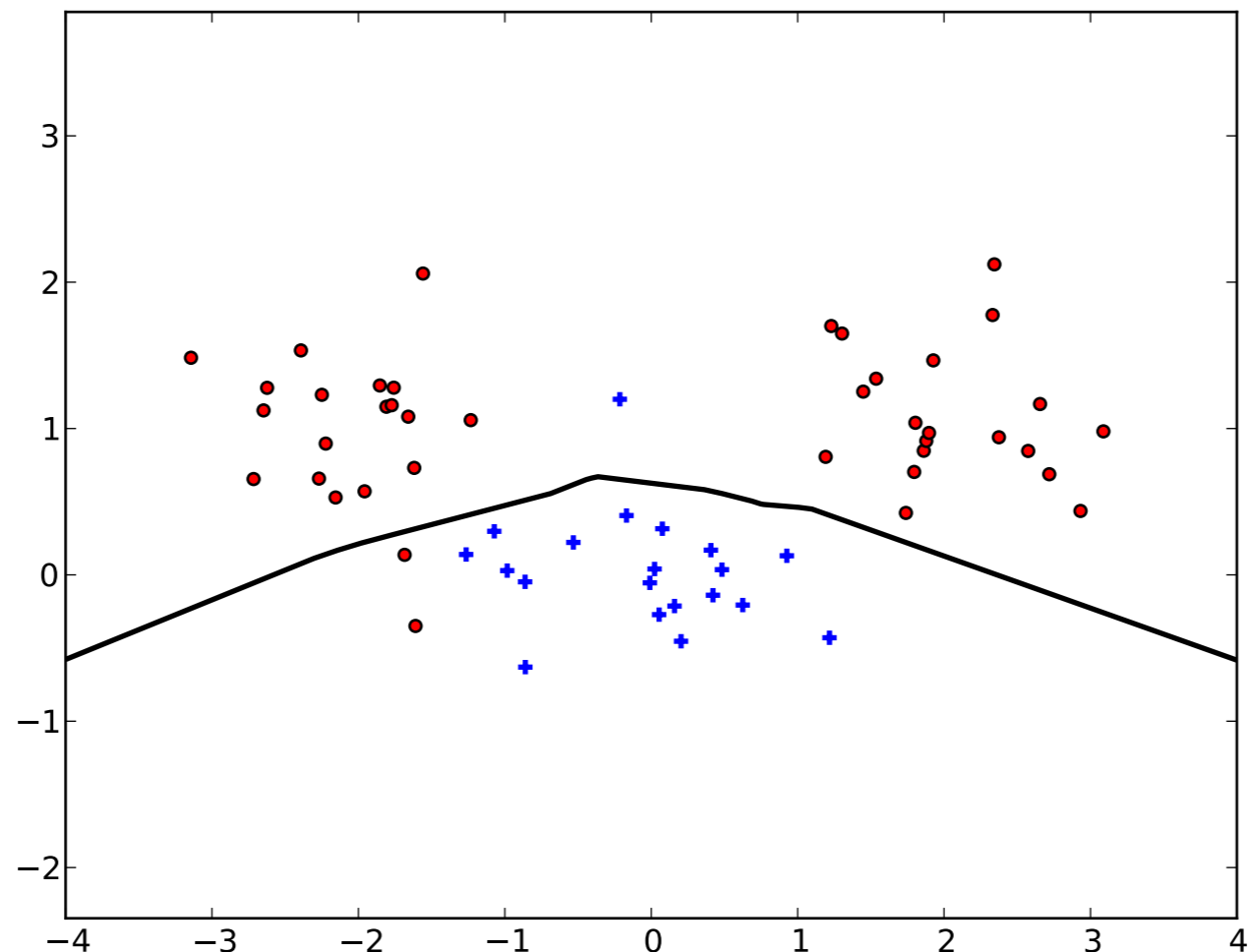




Size, optimization

- ▶ Many recent architectures use ReLU units (cheap to evaluate, sparsity)
- ▶ Easier to learn as large models...

10 hidden units

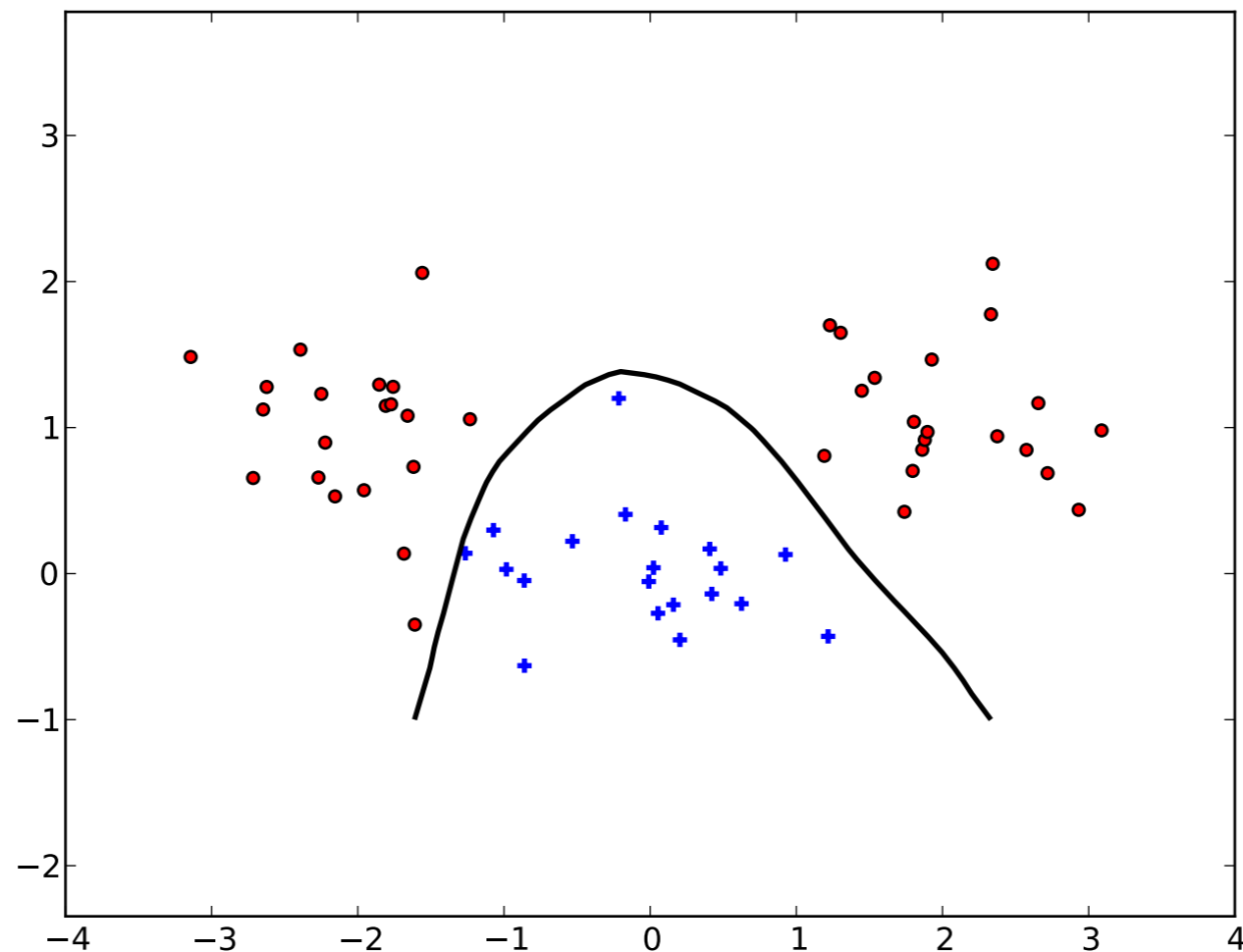




Size, optimization

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100 hidden units

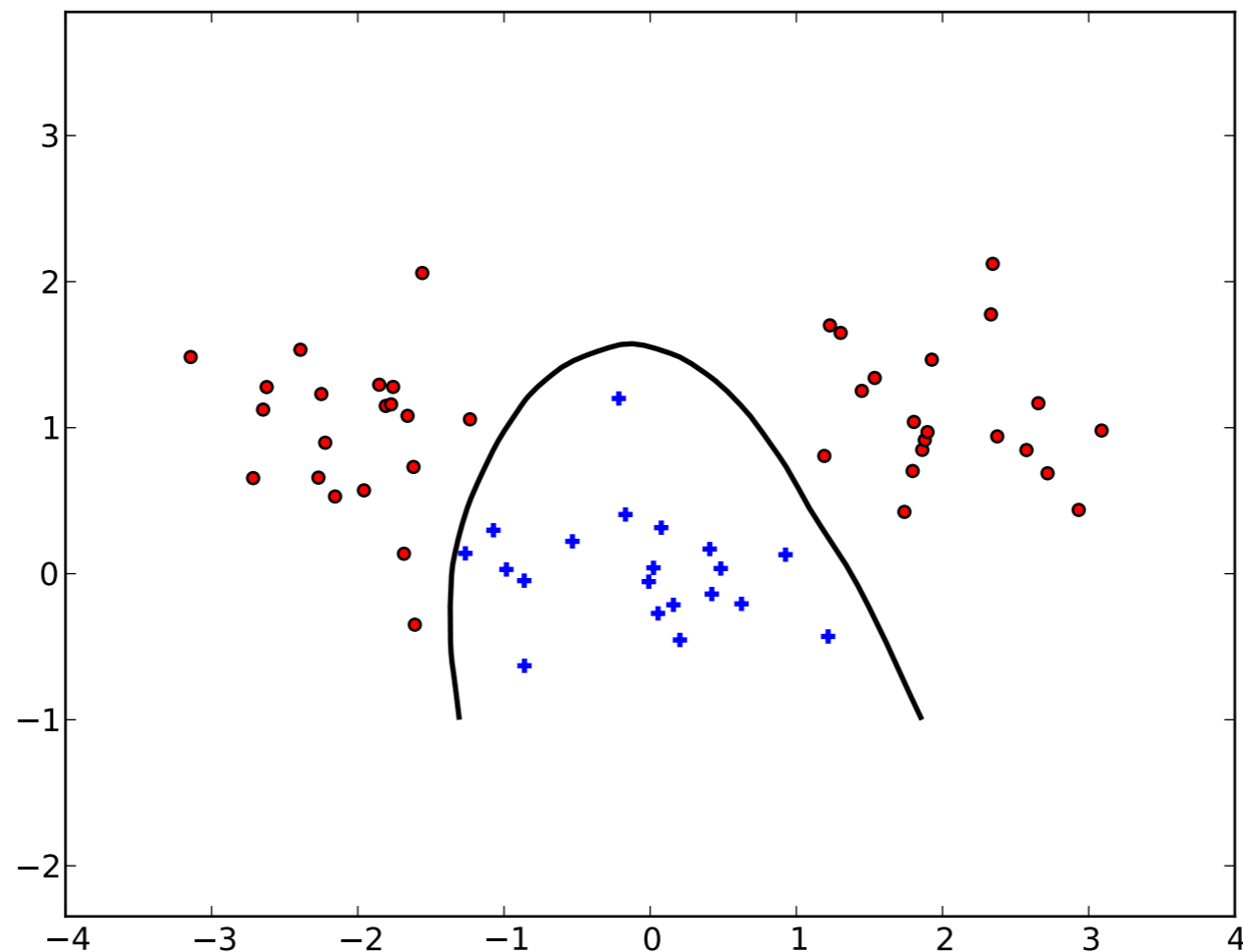




Size, optimization

- ▶ Many recent architectures use ReLU units (cheap to evaluate, sparsity)
- ▶ Easier to learn as large models...

500 hidden units





Summary (part 2)

- ▶ Neural networks can be learned with SGD similarly to linear classifiers
- ▶ The derivatives necessary for SGD can be evaluated effectively via back-propagation
- ▶ Multi-layer neural network models are complicated... we are no longer guaranteed to reach global (only local) optimum with SGD
- ▶ Larger models tend to be easier to learn ... units only need to be adjusted so that they are, collectively, sufficient to solve the task